

大西洋热盐环流多百年际振荡与人类文明演变史 Self-Sustained Multi-Centennial Oscillation of Atlantic Thermohaline Circulation

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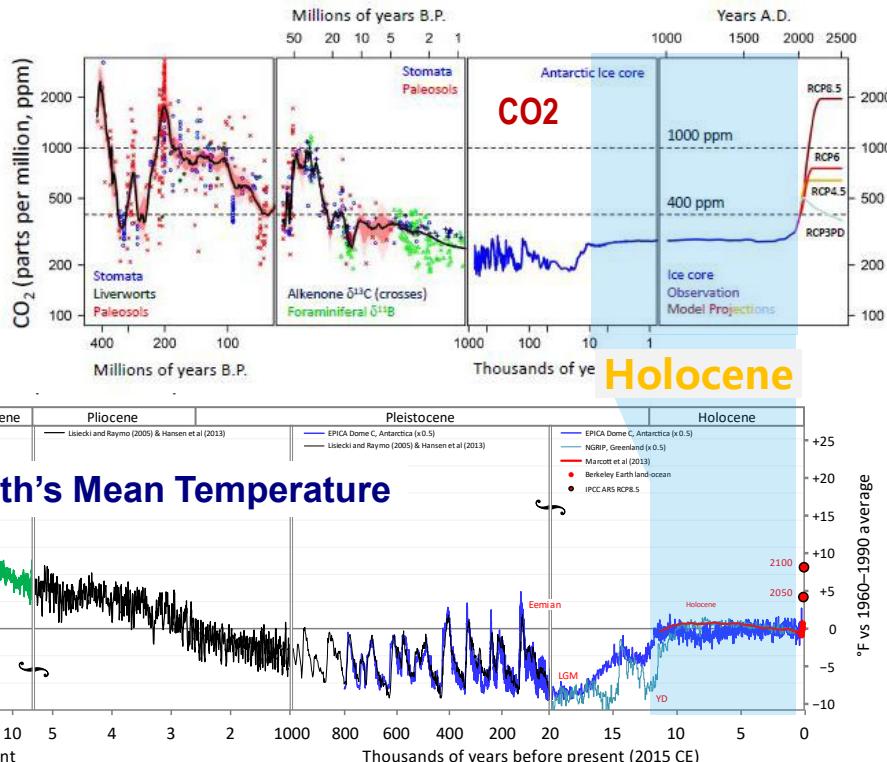
LaCOAS
北京大学气候与海-气实验室

500±300 Years

1. *Natural Centennial-Millennial oscillation* in climate system?
地球气候系统是否存在百年-千年尺度自然振荡?
2. Connection to the *evolution of human civilization*?
这种振荡与人类文明演化是否有关系?

Background: Stable Holocene Climate

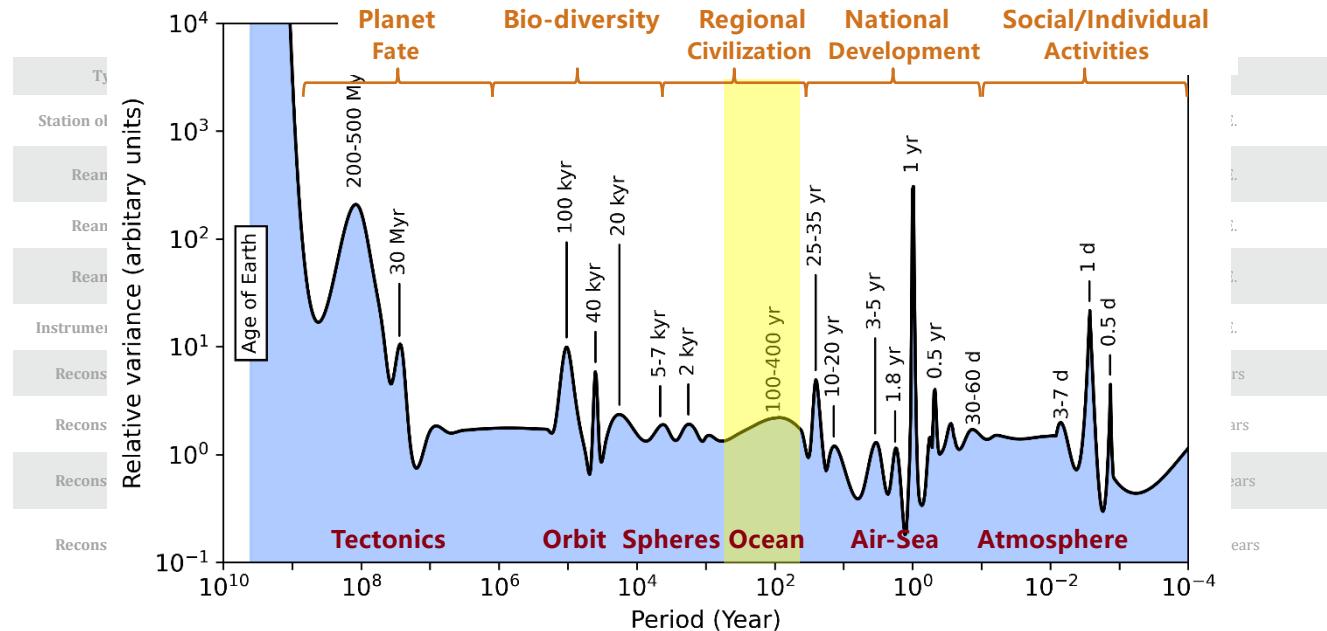
- Holocene: Since 10ka
- Stable external forcing
- Natural variability
(500 ± 300) (?) years



https://earth.org/data_visualization/a-brief-history-of-co2/

Background: Timescales of Climate Variabilities

Spectrum of Earth's Climate Variability



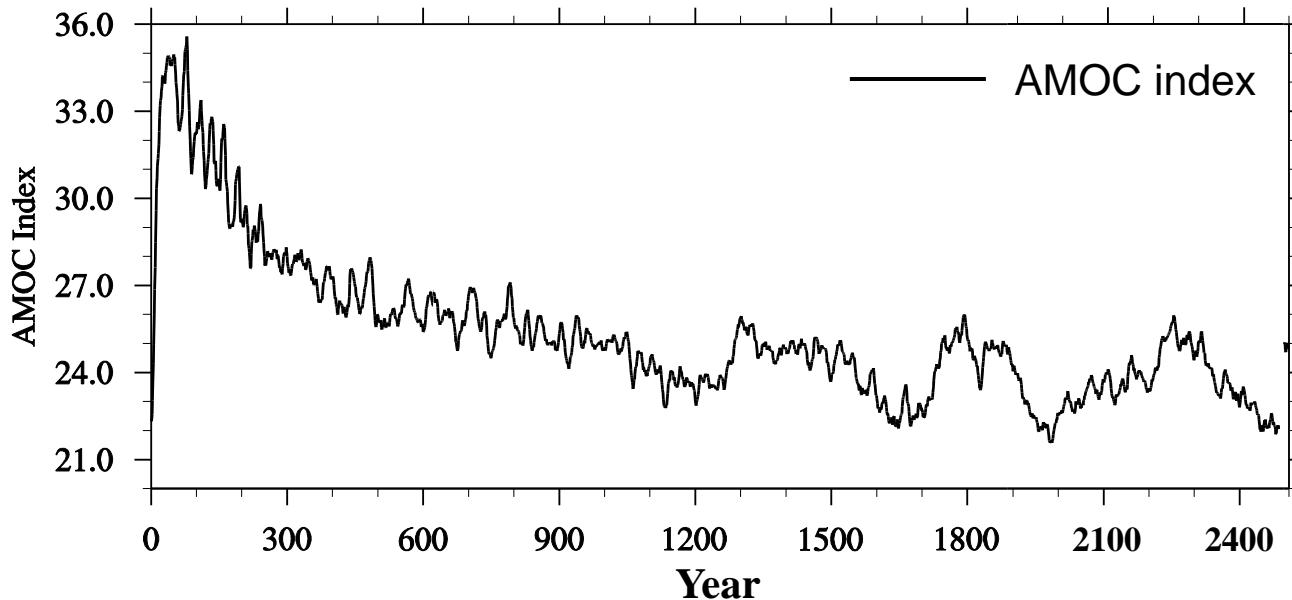
Based on multiply sources of “prewhitened” temperature records

Mitchell, 1976; Stocker and Mysak, 1992; Ghil, 2001; Heydt, 2021;

1. Motivation
2. Observations and Modeling Results
3. Theory
4. Our Modelings

Motivation

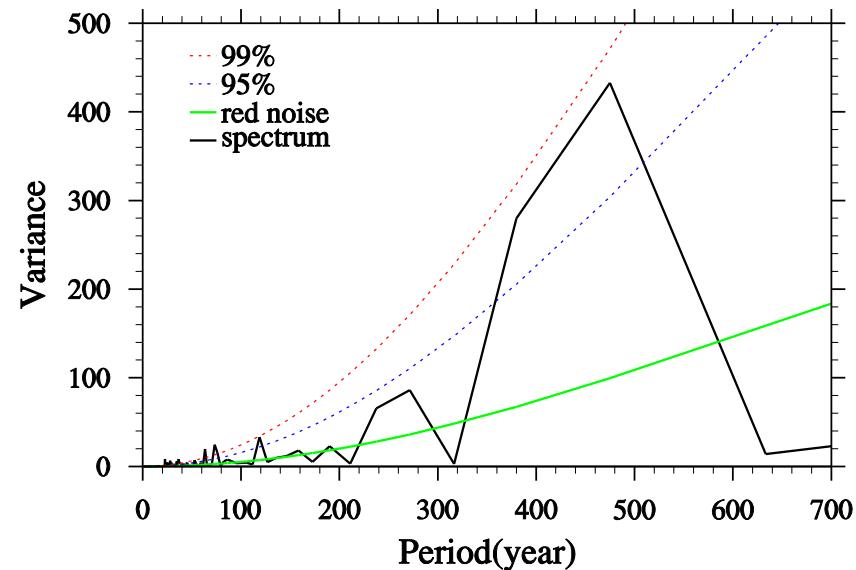
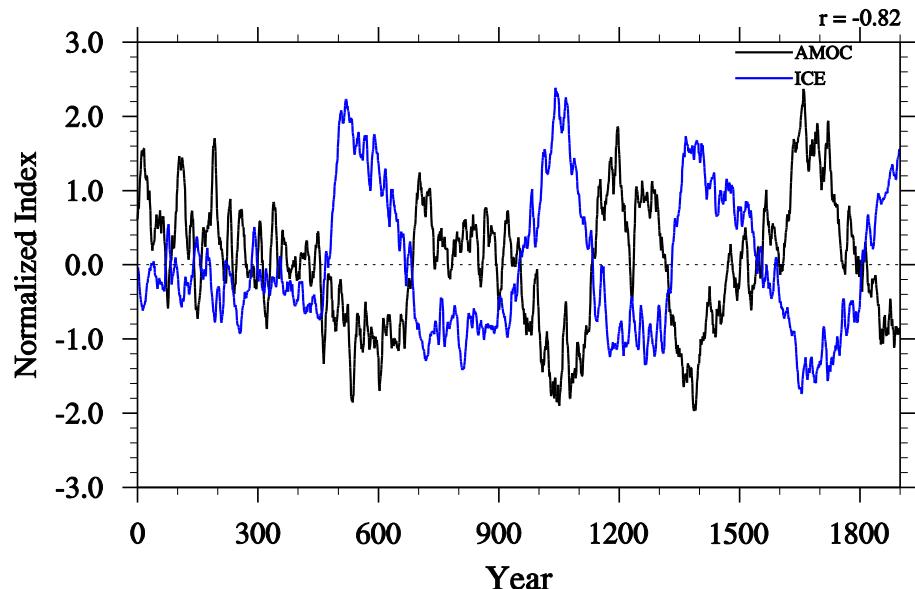
Earlier in **2013**, we confused ...



2500 years control run using NCAR-CESM1.0

Sea Ice → AMOC ?

Excellent correlation, but *causality?*

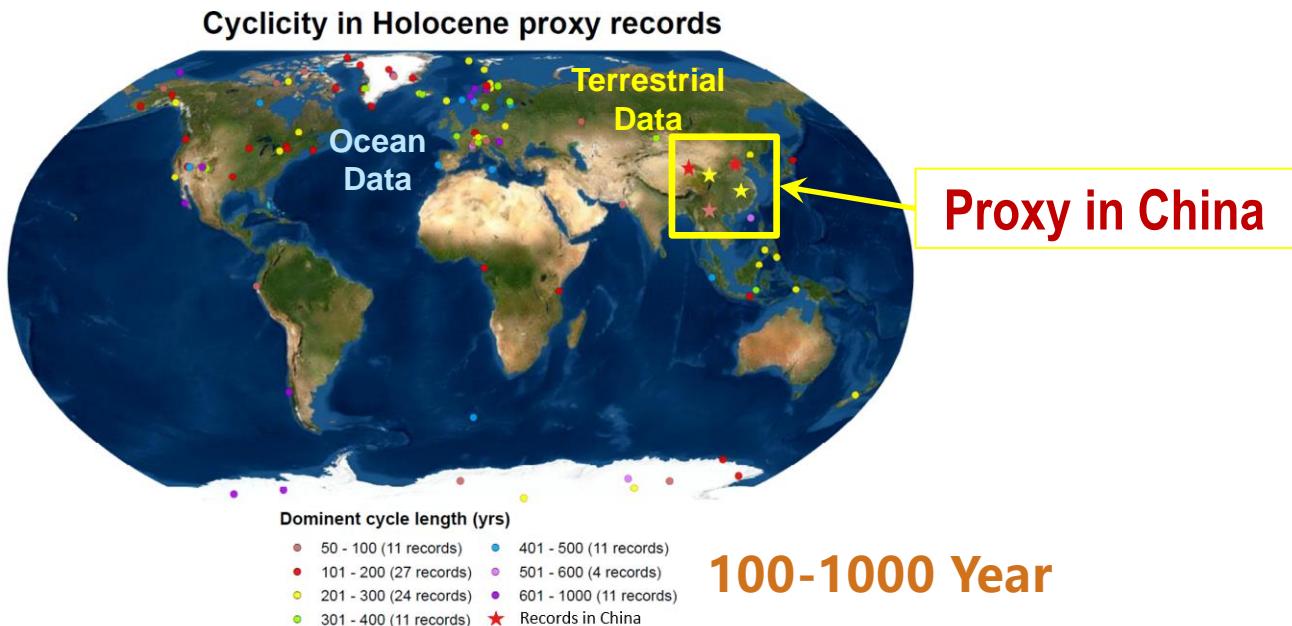


Confused ... So in 2018, We decided to decipher this mystery!

1. Motivation
2. Observations and Modeling Results
3. Theory
4. Our Modelings

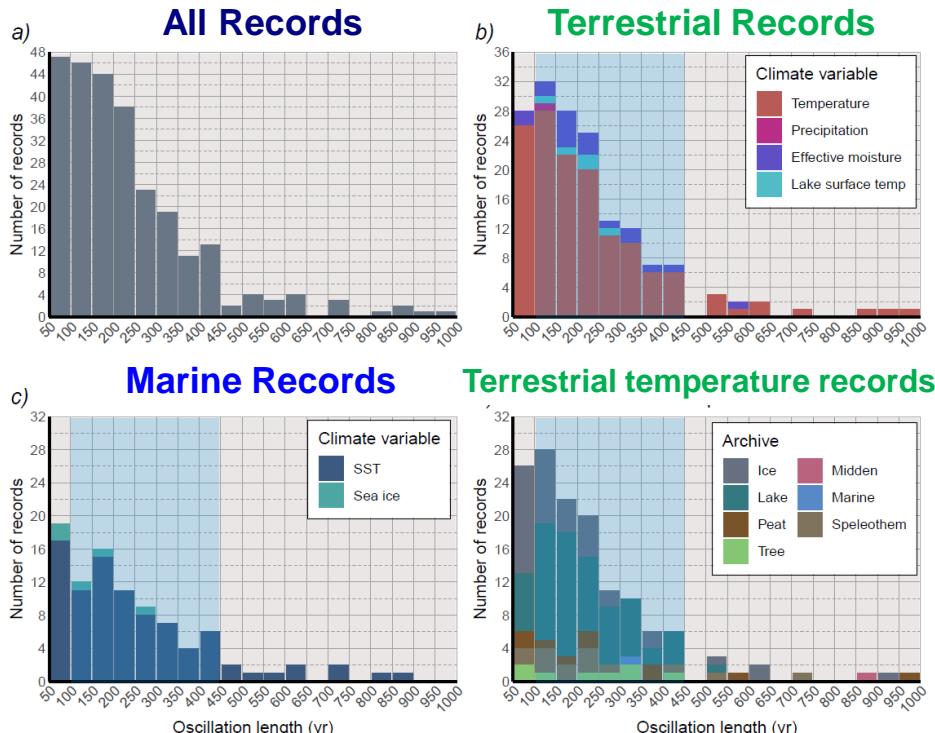
Observation: *Multicentennial* Variability in Holocene

Holocene Proxy: *Locations* and *timescale* represented



Thomas Gravgaard Askær et al., 2022: Multi-centennial Holocene Climate Variability in Proxy Records and Transient Model Simulations, QSR, 296 107801.

Observation: *Multicentennial* Variability in Holocene



500 Years
inwards

Thomas Gravgaard Askær et al., 2022: Multi-centennial Holocene Climate Variability in Proxy Records and Transient Model Simulations, QSR, submitted.

Centennial Variability: 200-300 (?) Years

文献出处	位置	代用指标	周期(年)
Siren et al., 1961. Lamb et al., 1977.	拉普兰德。	树轮。	70,90,200。
Soutar and Isaacs., 1969.	加利福尼亚。	海底沉积物。	106,170,360。
Johnsen and Dansgaard, 1970.	格陵兰。	冰芯。	53-56,69-73,104- 144,160-185。
LaMarche et al., 1974.	美国内华达州。	树轮宽度。	70,110。
Schweingruber et al., 1976.	瑞士。	树轮宽度。	30,120。
Lamb et al., 1977.	英国, 俄罗斯。	冬天严寒程度。	300,100。
Neftel et al., 1981. Sonett et al., 1984.	加利福尼亚。	树轮中的 C 放射。	150-300, 160,200。
Fisher et al., 1982.	格陵兰。 加拿大。	冰芯。	170-185,300-330,147- 435,625-714。
Hameed et al., 1983.	中国北京。	降水记录。	56,84,126。
Thompson et al., 1989.	秘鲁安第斯山脉。	冰芯。	110,250。
Gajewski, 1988.	Hells Kitchen 湖 (美 国威斯康辛州)。	湖底沉积物中的花粉。	90-120, 230-250。
Stuiver and Braziunas., 1989.	/。	树轮中的 14C。	45,52,67, 143,218,420。
Rothlisberger et al., 1989.	/。	树轮和冰川振荡。	88,102-104,123-143。

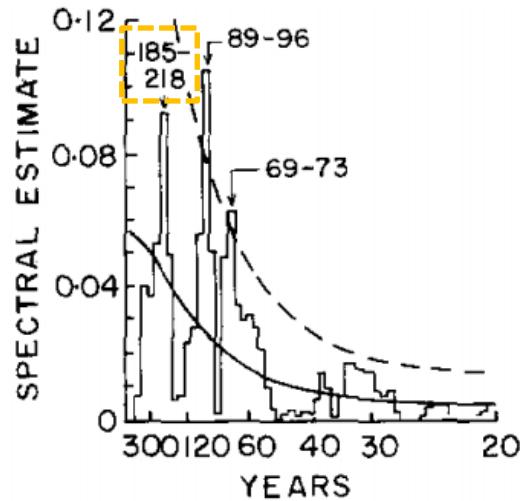
文献出处	位置	代用指标	周期(年)
Briffa et al., 1990.	Fennoscandia。	树轮。	50-150。
Anklin et al., 1998.	格陵兰岛。	冰川雪和冰芯。	100,200。
Chapman and Shackleton., 2000.	北大西洋。	深海沉积物。	550。
McDermott et al., 2001.	爱尔兰西南部。	/。	78,169,625。
Proctor et al., 2002.	苏格兰西北部。	石笋。	72-96,116-150。
Nyberg et al., 2002.	加勒比东北部。	有孔虫。	200-400。
Risebrobakken et al., 2003.	挪威海。	岩芯。	80-115,260, 417,550-570。
Oppo et al., 2003.	大西洋东北部。	有孔虫。	百年。
Sicre et al., 2008.	冰岛北部。	冰芯。	50-150。
J. Zheng et al., 2010.	中国东部、西部、青 藏高原。	历史文献、树轮、 降水。	200-300, 百年。
Perner et al., 2013.	格陵兰西部。	有孔虫。	百年。
Newby et al., 2014.	北美洲。	湖底沉积物。	几百年。
Thirumalai et al., 2018.	Garrison 海盆。	有孔虫。	百年。

杨海军, 石佳琪等, 2023: 多百年际气候变率: 观测、理论与模拟研究。科学通报, 68, 1-9

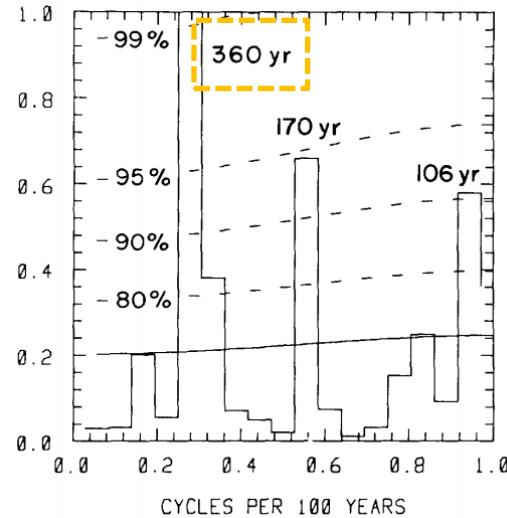


Centennial Variability in *Proxy* Data

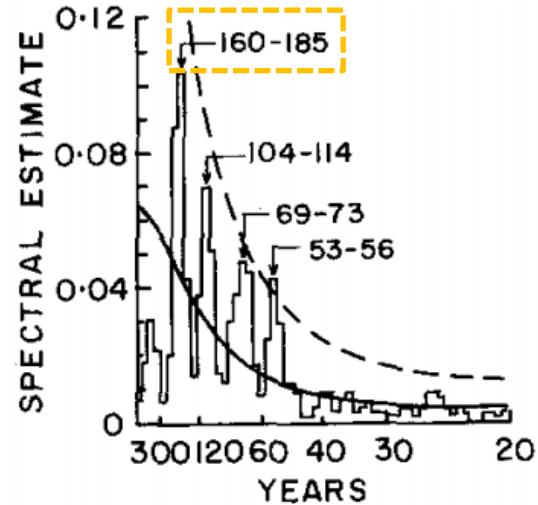
Lapland
Tree rings width



Santa Barbara Basin sediment
minimum population of hake



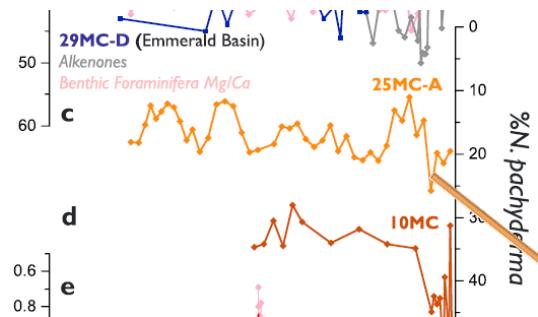
Camp Century
Cores (氧同位素)



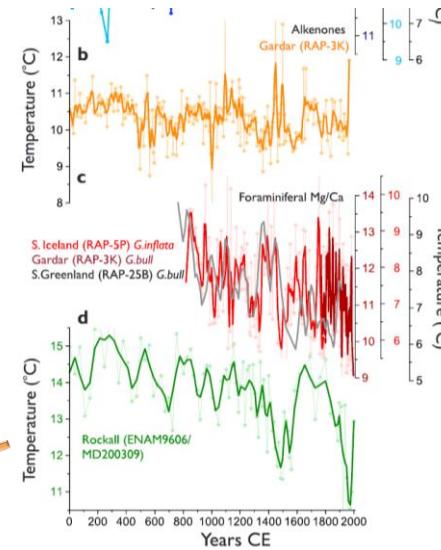
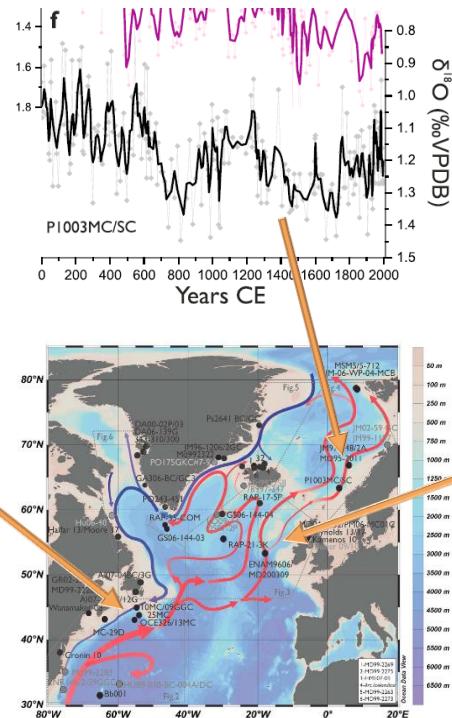
Siren et al. (1961), Lamb et al. (1977); Soutar and Issacs (1969); Johnsen and Dansgaard (1970)

Centennial Variability in *Proxy* Data

(f) $\delta^{18}\text{O}_{\text{foram}}$ from P1003MC/SC



(c) % N.pachyderma from Laurentian Fan (25MC-A)

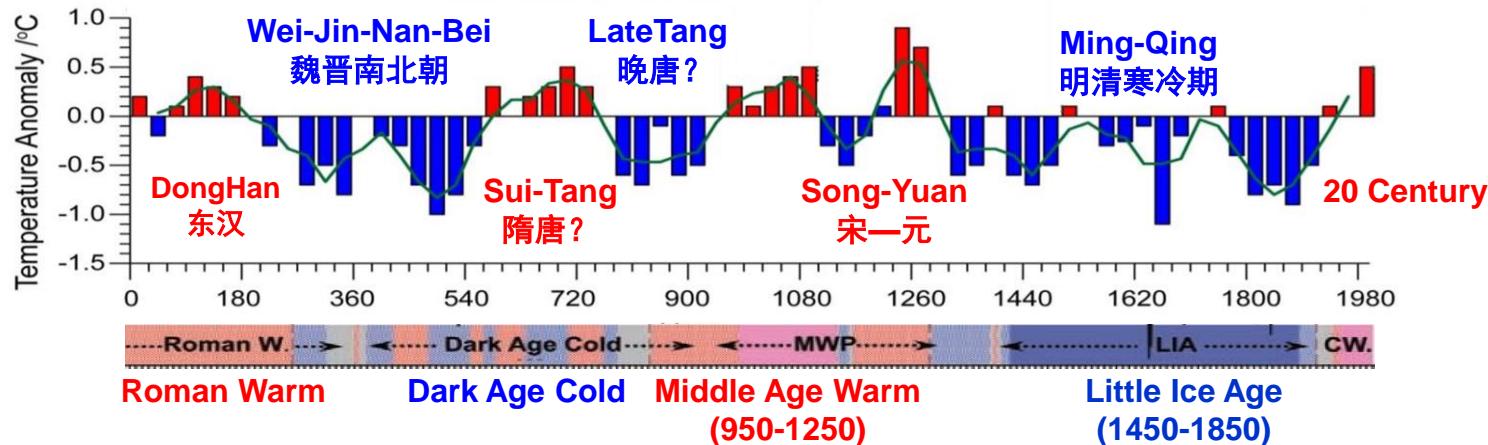


(b) alkenone records from RAPiD-21-3K;
(d) foraminiferal Mg/Ca-based
temperature reconstructions from Rockall
Trough ENAM9606/M2003209

Moffa-Sánchez et al. (2019), Paleoceanography and Paleoclimatology

Documentary records in China: 200-300 Years

Chinese Scientists' contribution: Temperature evolution in eastern China
in wintertime of the past 2000 years



葛全胜, 郑景云, 满志敏, 方修琦, 张丕远, 2002: 过去2000a中国东部冬半年温度变化序列重建及初步分析。地学前沿, 9(1), 169-181.

郑景云等, 2010; 葛全胜等, 2014

Documentary records in China: 200-300 or 600 (?) Years

Warm and Cold period during the past 5000 years in the evolution of civilization over greater China



竺可桢, 1925: 南宋时代我国气候之揣测; 1961: 历史时代世界气候的波动; 1972: 中国近五千年来气候变迁的初步研究

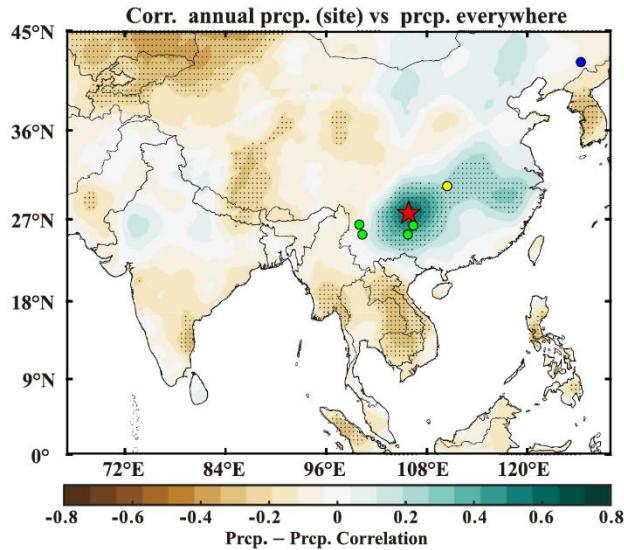
吴祥定等, 1990: 树木年轮与气候变化; 张丕远等, 1996: 中国历史气候变化; 牟重行, 1996: 中国五千年气候变迁的再考证

张德二等, 2004: 中国三千年气象记录总集; 满志敏, 2009: 中国历史时期气候变化研究

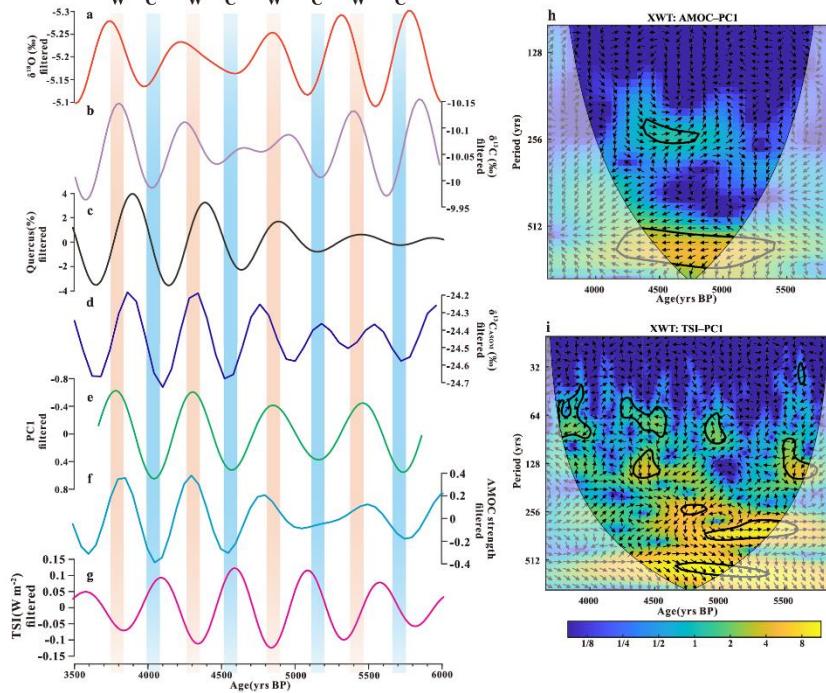
<https://corp.fudan.edu.cn/Reading/气候如何影响人类文明兴衰.pdf>
https://mp.weixin.qq.com/s/OU4YXCCc_PYKJv5xuZbvYkQ

Records in China: 200-300 or 600 (?) Years

550-Year period during 6000-3500 BP on Yunnan-Guizhou Plateau

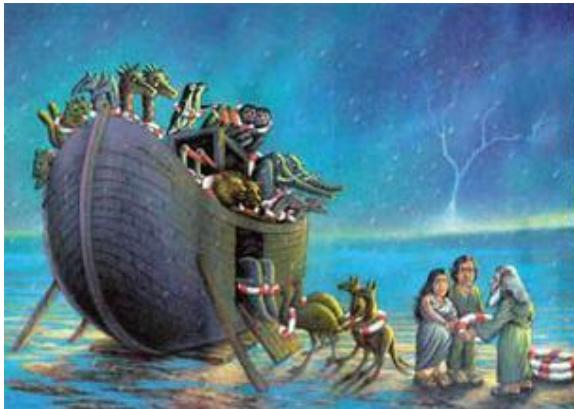


Li et al. 550-Year Climate Periodicity in the Yunnan-Guizhou Plateau During the Late Mid-Holocene: Insights and Implications. **GRL, 2023**, 10.1029/2023GL103523.



人类文明的兴衰史也与百年-千年的气候振荡有密切关系

诺亚方舟



大禹治水



- 王绍武 (2005a) : 公元前2.2-2千年尼罗河文明、两河流域文明及印度河文明等等突然衰落发生在中纬度普遍变冷的气候背景中，是全新世进入大暖期以来的一次强冷事件
- 王绍武 (2005b) : 洪水→干旱→中华文明的诞生→公元前2070年夏朝建立
- 王绍武和黄建斌 (2006) : 夏朝建立的基础“大禹治水”，气候干旱可能对“治水”成功产生了影响
- 王绍武等 (2011) : 距今6-4千年的五帝时代：湿润→干旱；可能与热盐环流的突然减弱有关

Our Questions

500±300 Years

1. *Natural Centennial-Millennial oscillation* in climate system?

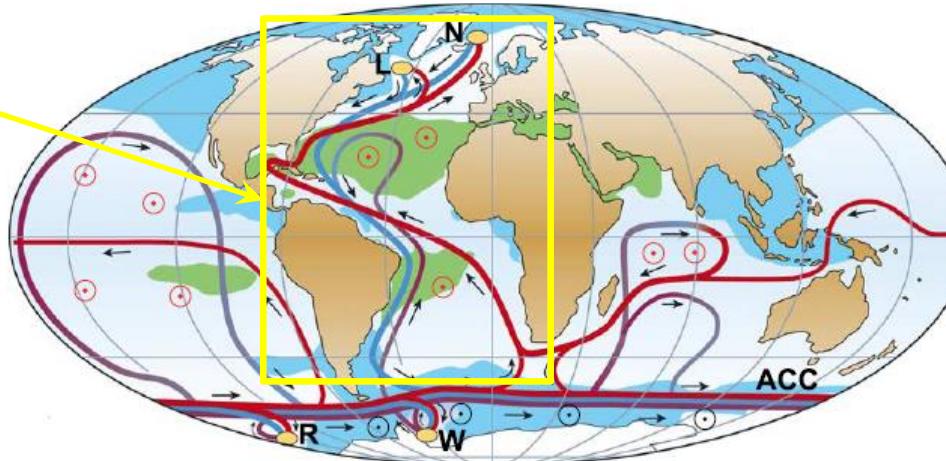
地球气候系统是否存在百年-千年尺度自然振荡? (Yes!)



*What component of the Earth's climate system can provide
multicentennial timescale?*

Great Conveyor Belt: *Thousands' Years*

AMOC



- Surface flow
- Deep flow
- Bottom flow
- Deep Water Formation

- Wind-driven upwelling
- Mixing-driven upwelling
- Salinity > 36 ‰
- Salinity < 34 ‰

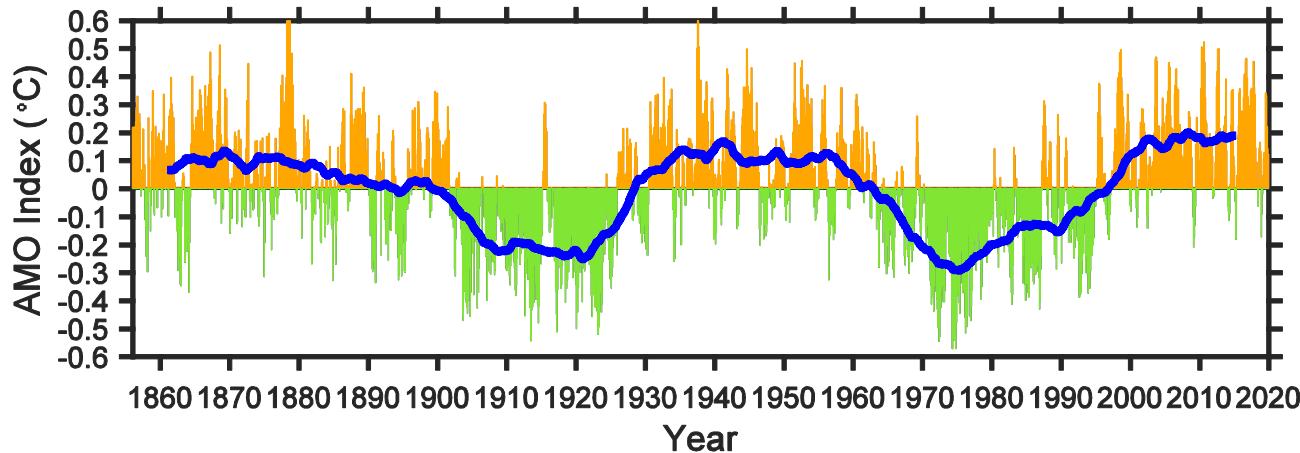
- L Labrador Sea
- N Nordic Seas
- W Weddell Sea
- R Ross Sea

Advection timescale: *Thousands' years*
→→ Timescale for multicentennial variability

AMO: 60-80 Years

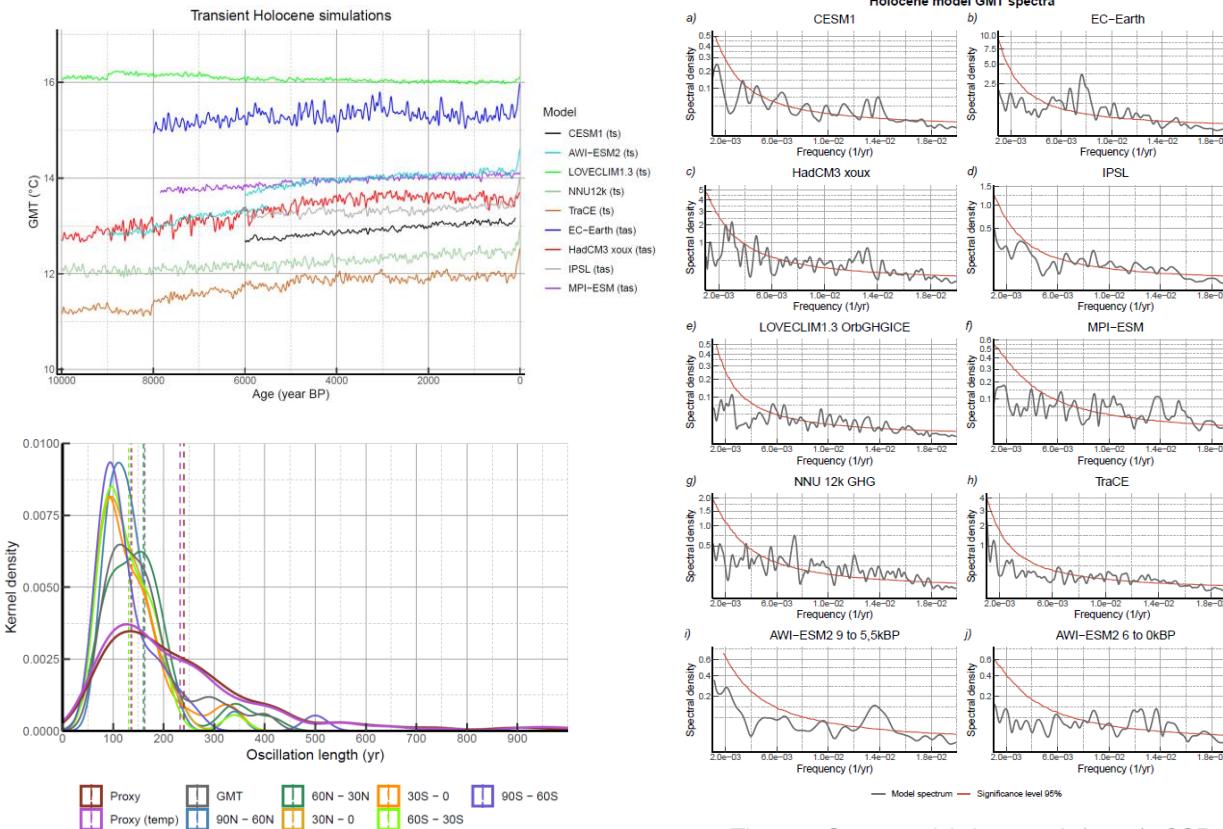
Tons of studies on *decadal* (20-30 yr) & *multi-decadal* (60-80 yr) variabilities

No direct evidences of **multicentennial** variability



Kaplan SST (Kaplan et al., 1998; Drinkwater et al., 2014)

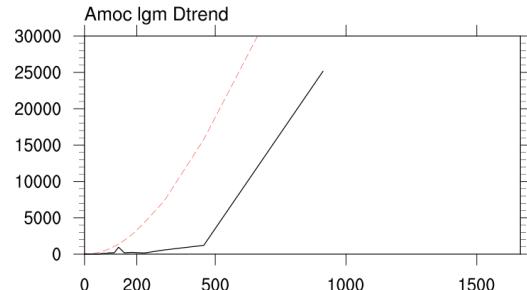
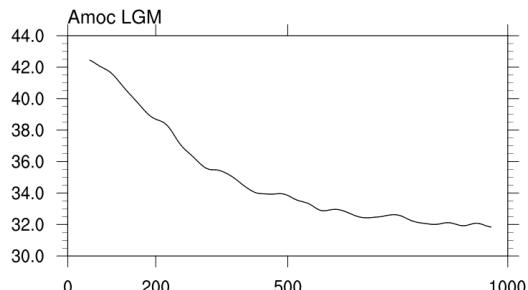
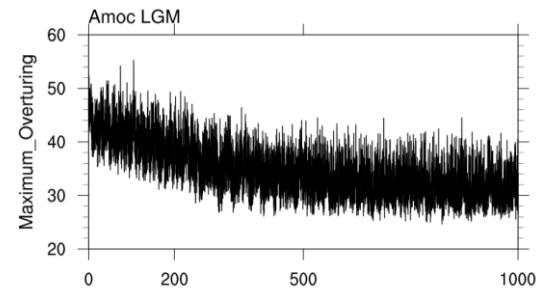
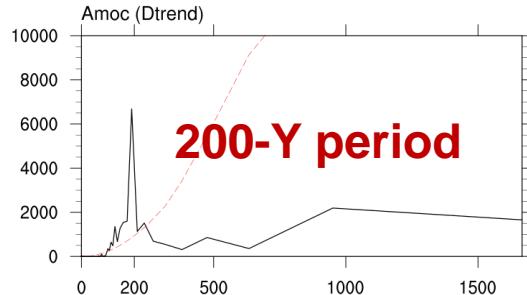
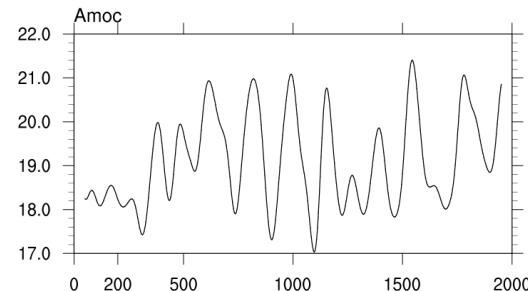
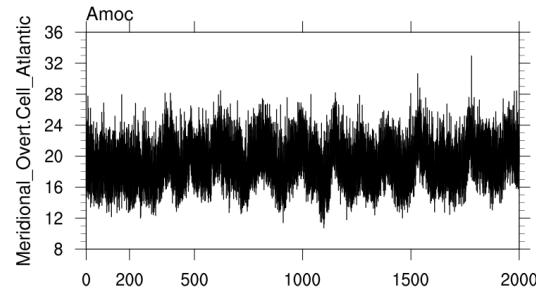
Multicentennial Variability in Coupled Models



Thomas Gravgaard Askær et al. (2022), QSR

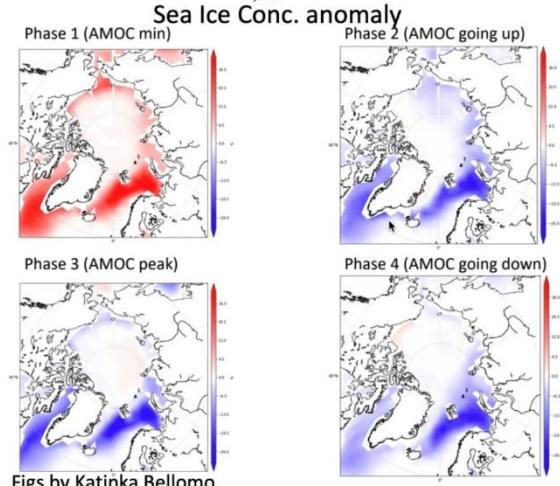
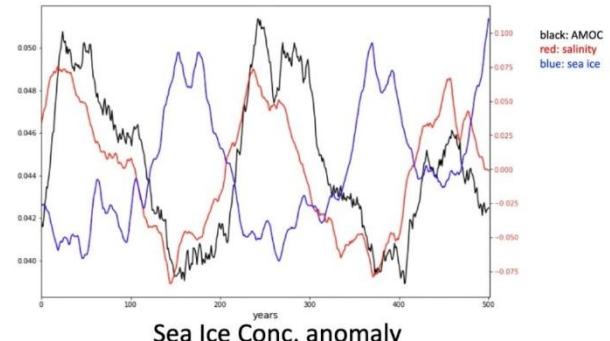
Centennial Oscillation in EC-Earth3 Model

2000 Years period PI control experiment



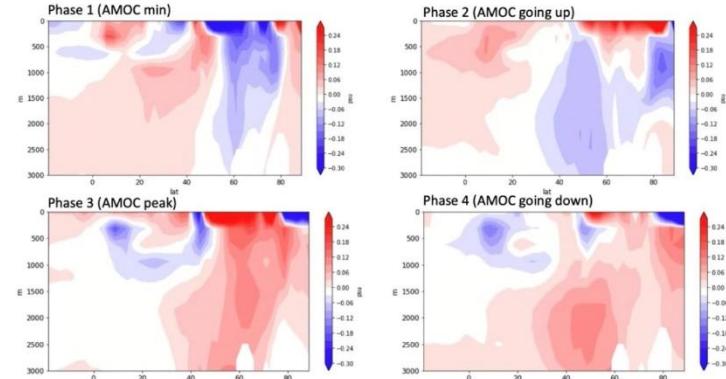
Zhang et al. (2021)

Exists also in Other Models ...



An example of topic of possibly broader interest: Oscillations in PI EC-Earth simulations

Salinity anomaly



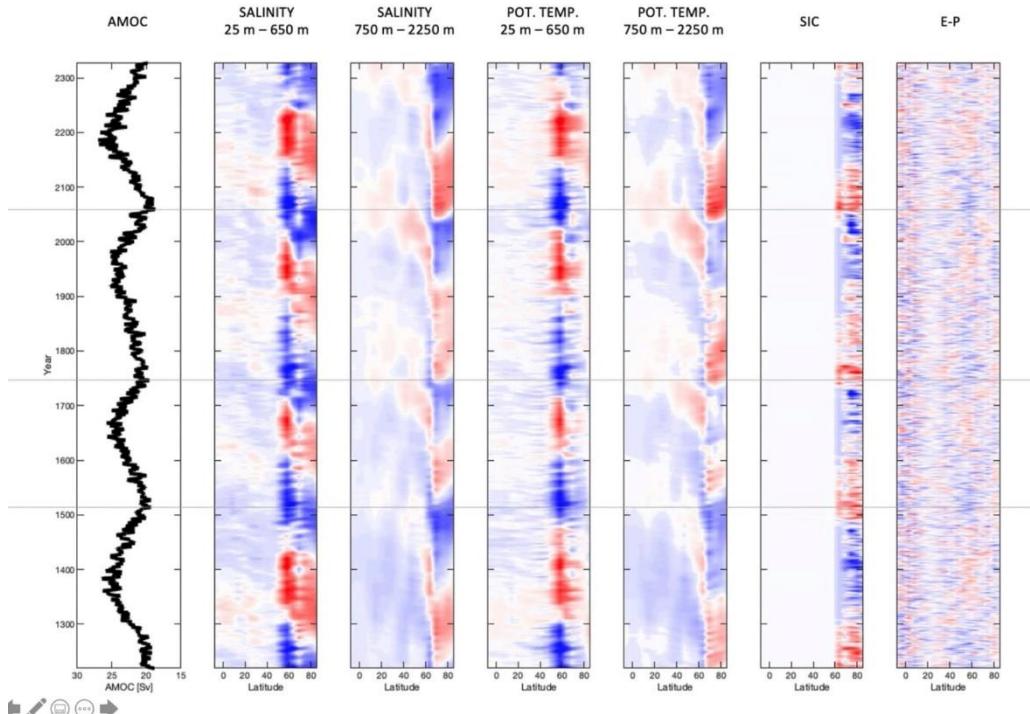
An understanding of these oscillations has implications for:

- better tuning and creation of equilibrated ICs of the model
- Interdecadal variability in EC-Earth
- Paleoclimate and tipping points
- A better understanding of mechanisms associated with AMOC decrease in projections

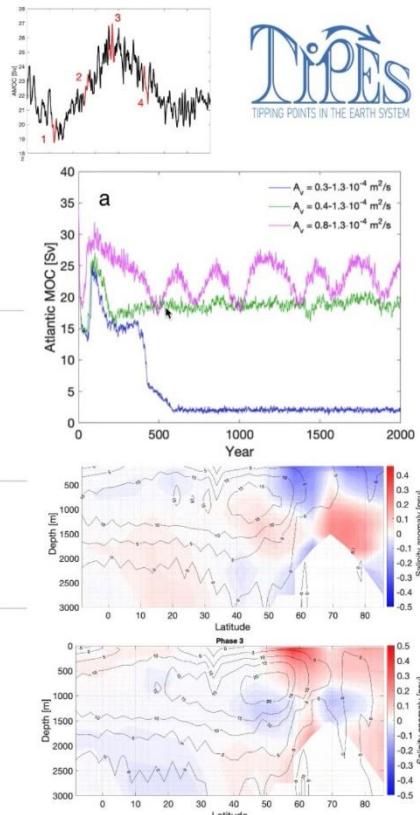
Jost von Hardenberg (2021) Personal communication

Exists also in Other Models ...

AMOC oscillations in the coupled PlaSim-LSG EMIC



Angeloni et al. (2021)



Our Questions

500±300 Years

1. *Natural Centennial-Millennial oscillation* in climate system?

地球气候系统是否存在百年-千年尺度自然振荡? (Yes!)



2. Coupled Model: AMOC has multicentennial variability

→ Climate system



Why and How? Theory needed!

1. Motivation
2. Observation and Modeling
3. Theory, Simple Model: Previously
4. Our Modelings

2-Box Model and Multi-Equilibrium

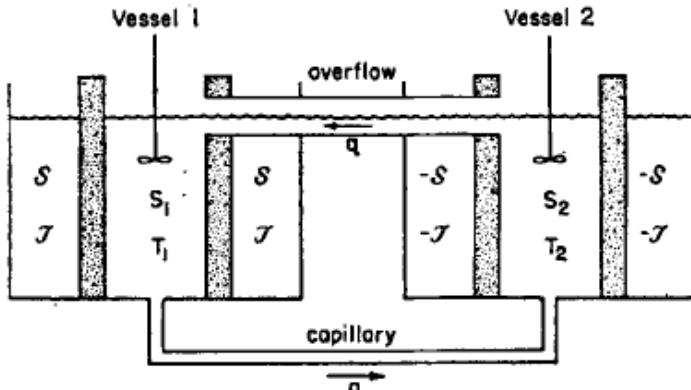
Thermohaline Convection with Two Stable Regimes of Flow

By HENRY STOMMEL, Pierce Hall, Harvard University, Massachusetts

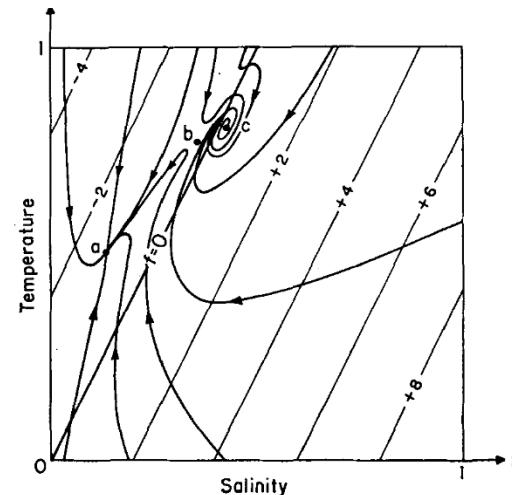
(Manuscript received January 21, 1961)

Abstract

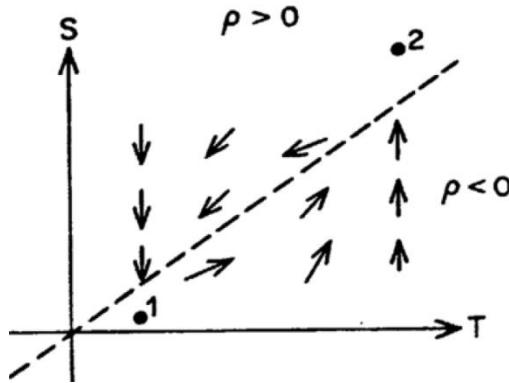
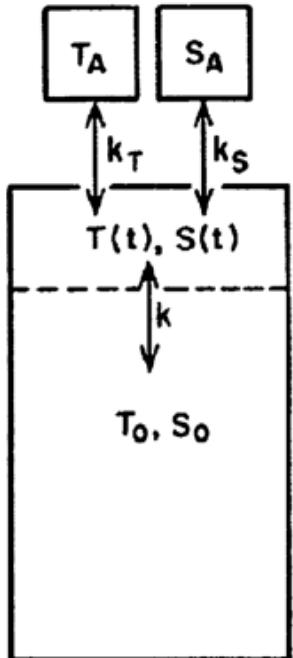
Free convection between two interconnected reservoirs, due to density differences maintained by heat and salt transfer to the reservoirs, is shown to occur sometimes in two different stable regimes, and may possibly be analogous to certain features of the oceanic circulation.



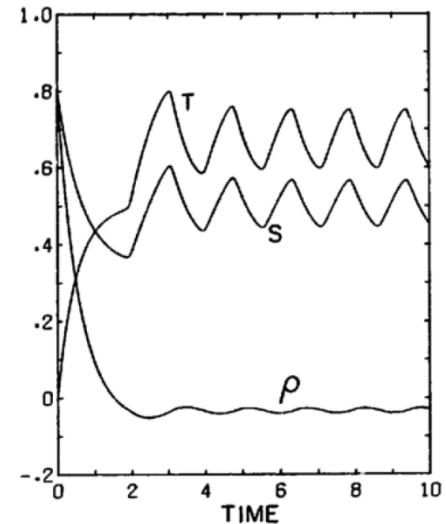
Henry Stommel (Tellus, 1961)



Energy Source: *Ocean Convection*

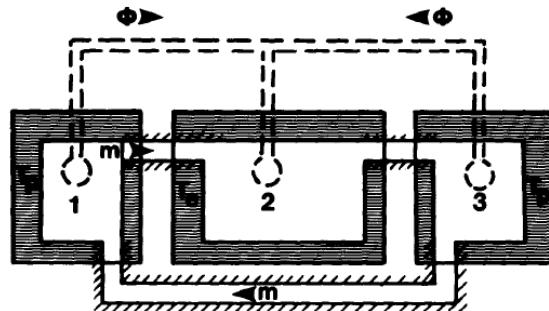


- **Flip-Flop model**
- **Self-sustained oscillation with increasing vertical turbulent mixing**

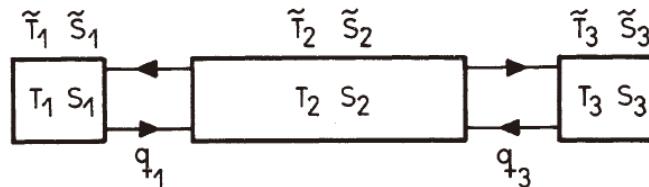
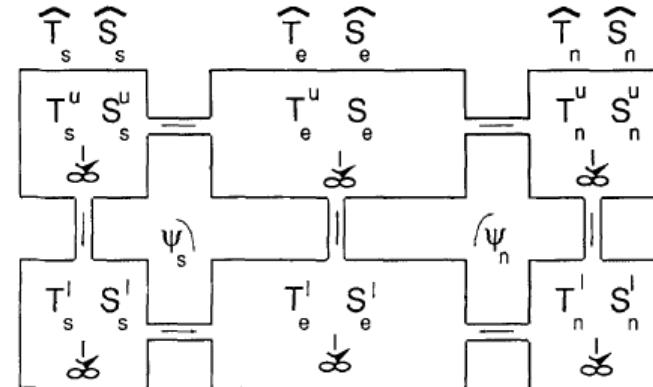


Pierre Welander (1982), A simple heat-salt oscillator. Dyn. Atmos. Oceans.

3-Box Model and Multi-Equilibrium



Claes Rooth (1982)



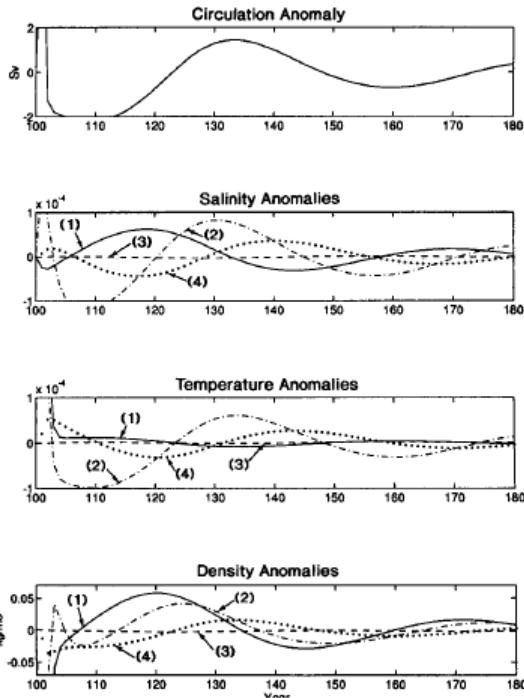
Pierre Welander (1986)

2D Model and 2-, 3-Box Model

Olivier Thual & James C.
Mcwilliams (1992)

Climate transition between different stable regimes, with global and centennial-millennium timescale

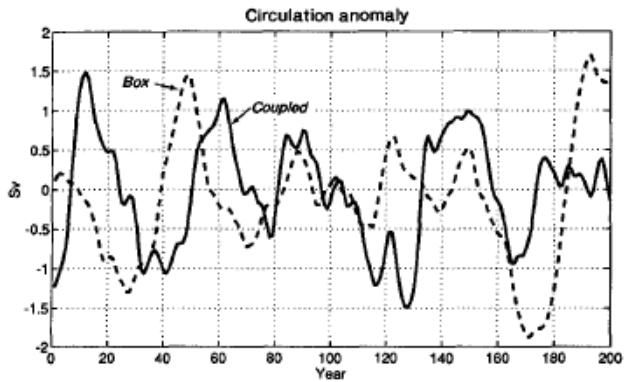
Energy Source: *Atmosphere* Perturbation



←: Damped Oscillation

Mode

Circulation under random thermal forcing →



- **2-Box: Interdecadal variability of THC**
- **Linear interpretation**
- **Excited by atmospheric random forcing**

Stephen Griffies and Eli Tziperman (1995): A linear thermohaline oscillator driven by stochastic atmospheric forcing. J. Climate

Energy Source: *Ocean Advection* Feedback

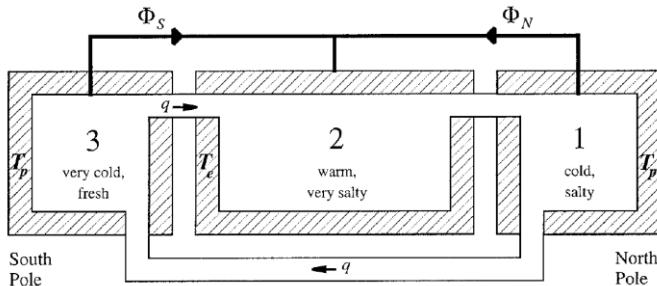
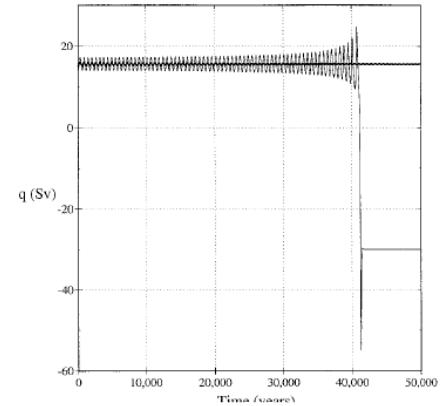
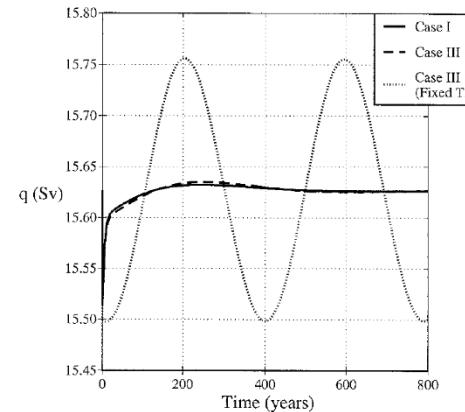


FIG. 1. Rooth's conceptual three-box model of thermohaline circulation, showing equilibrium conditions for Northern Hemisphere sinking. The separation between high- and low-latitude boxes is assumed to occur near the peak in atmospheric transports due to baroclinic eddy fluxes, i.e., about 35° latitude.



**3-Box model with asymmetrical freshwater forcing / Stability of the equilibrium
Periodic oscillation with constant Temperature / Collapse under some parameters**

Jeffery Scott, Jochem Marotzke and Peter Stone (1999): Interhemispheric thermohaline circulation in a coupled box model. JPO.

Single Equilibrium: Self-Sustained Oscillation

Self-sustained oscillation with nonlinear close condition

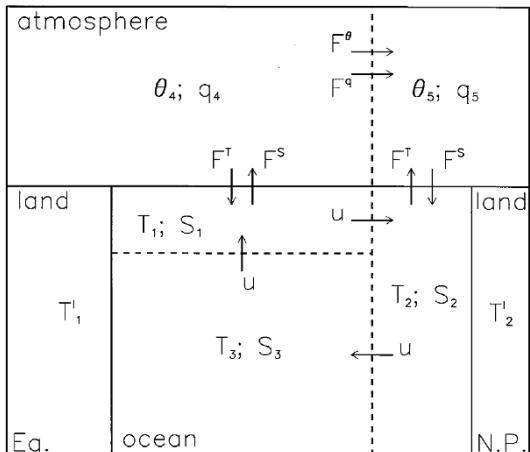
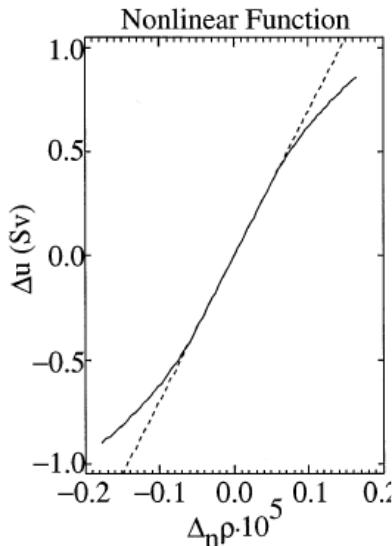


FIG. 1. The box model geometry.

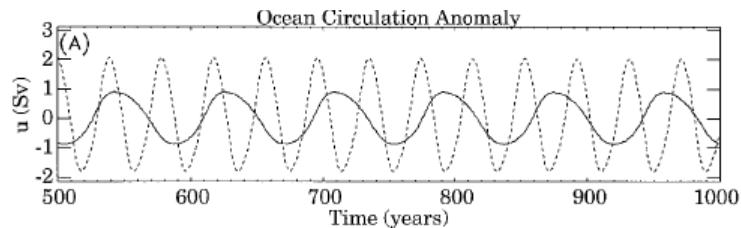
3-Box coupled model



$$u = \bar{u} + u' = \bar{u} + \xi(u_0, \Delta_n \rho') \Delta_n \rho', \quad (2)$$

where

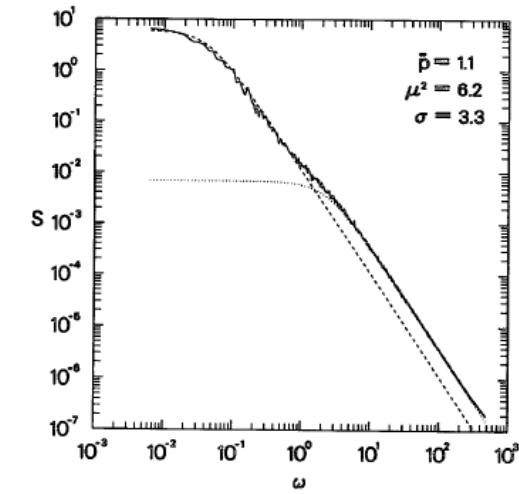
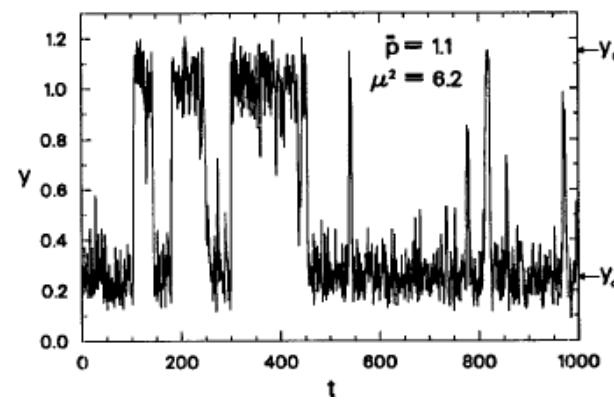
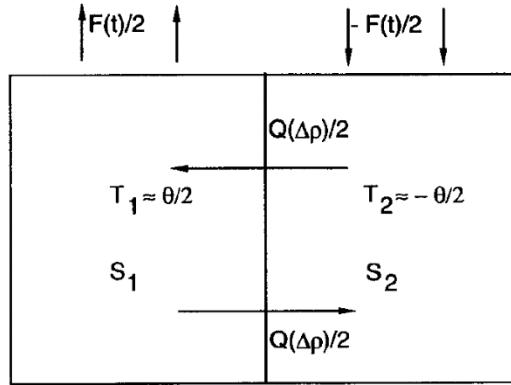
$$\xi(C, x) = \begin{cases} C \frac{x_+}{x} \left[k \left(\left(\frac{x}{x_+} \right)^{1/k} - 1 \right) + 1 \right] & \text{if } x > x_+ \\ C & \text{if } x_+ \geq x \geq x_- \\ C \frac{x_-}{x} \left[k \left(\left(\frac{x}{x_-} \right)^{1/k} - 1 \right) + 1 \right] & \text{if } x < x_- \end{cases} \quad (3)$$



Rivin & Tziperman (1997): Linear versus self-sustained interdecadal thermohaline variability in a coupled box model. JPO

Multi-Equilibrium: *Forced Regime Shift*

Stommel 2-Box model, no *intrinsic* variability, stochastic forced variability



Middle: Multi-equilibrium and forced oscillation; Right: Power spectrum

Paola Cessi (1994), A simple box model of stochastically forced thermohaline flow. JPO

Single Equilibrium: *Forced Oscillation*

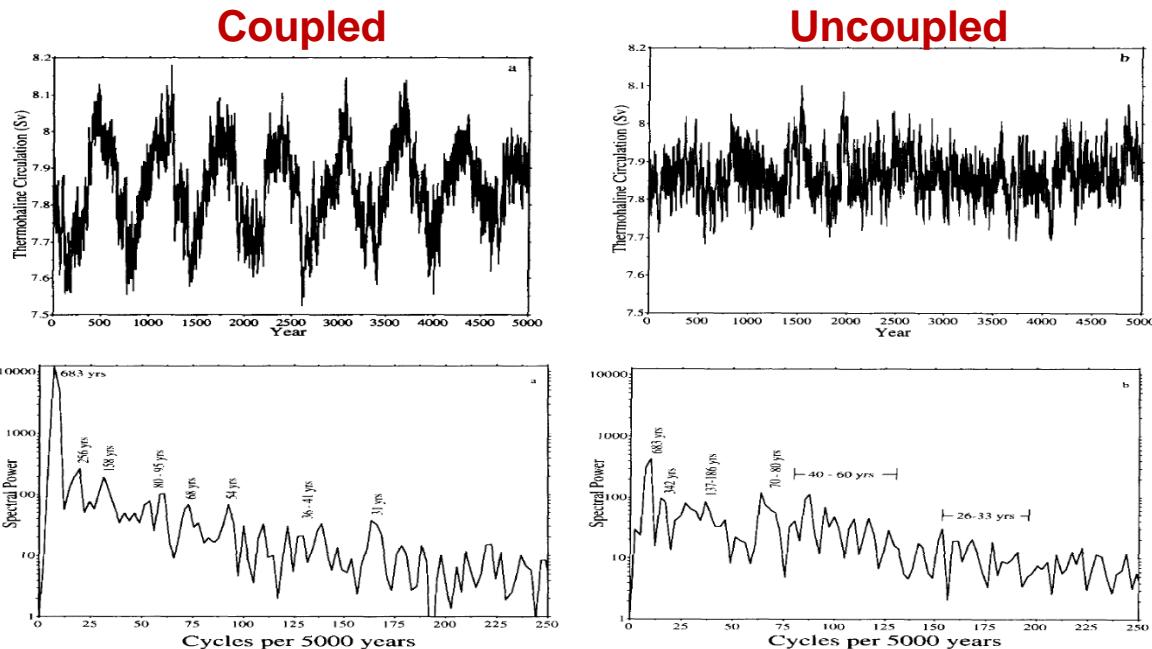
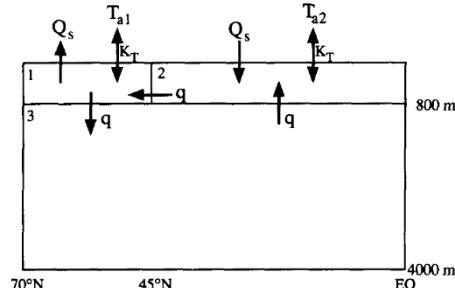
Atmosphere Lorenz model and Ocean 3-Box model

Lorenz (1984, 1990) introduced a low-order atmospheric “general circulation” model, defined by three ordinary differential equations:

$$\frac{dX}{dt} = -Y^2 - Z^2 - aX + aF, \quad (1)$$

$$\frac{dY}{dt} = XY - bXZ - Y + G, \quad (2)$$

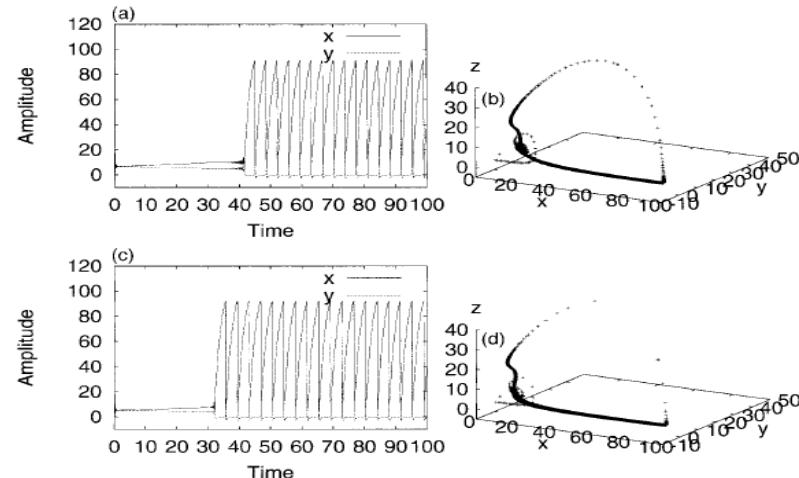
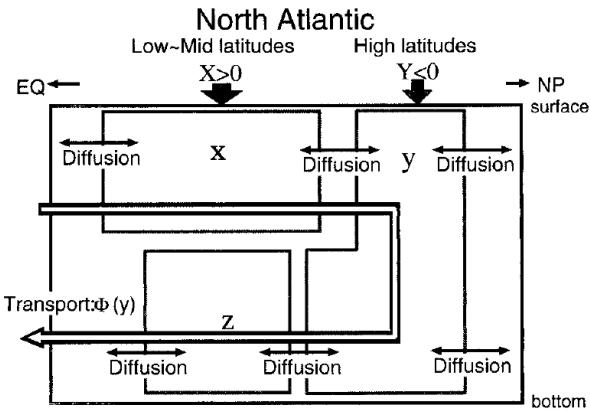
$$\frac{dZ}{dt} = bXY + XZ - Z. \quad (3)$$



Paul Roebber (1995), Climate variability in a low-order coupled atmosphere-ocean model. Tellus-A

3-Box Model for Bond Cycle

A 3-Box with only Salinity considered, internal *Millennial* oscillation



Bifurcation: from a stable solution to an unsteady bounded oscillation

Sakai & Peltier (1999), A dynamical systems model of the Dansgaard-Oeschger oscillation and the origin of the bond cycle. JC

Thermohaline Circulation Stability: *Regime Shift*

3-Box model, hysteresis behavior under freshwater forcing

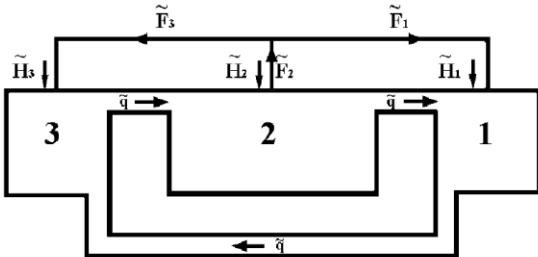
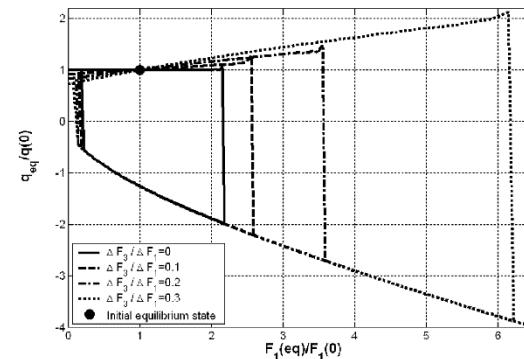
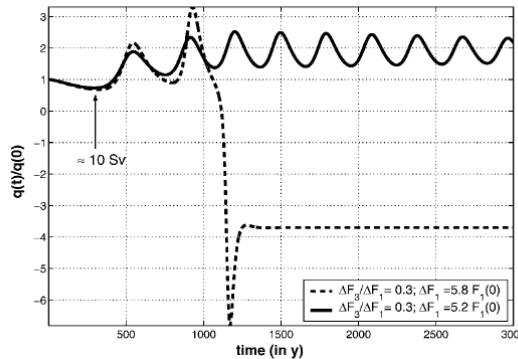


FIG. 1. Schematic picture of the interhemispheric box model.



Lucarini & Stone (2005), Thermohaline circulation stability: a box model study. Part I: uncoupled model. JC

Thermohaline Circulation Centennial Oscillation

2-D with random forcing, 200-300 years oscillation

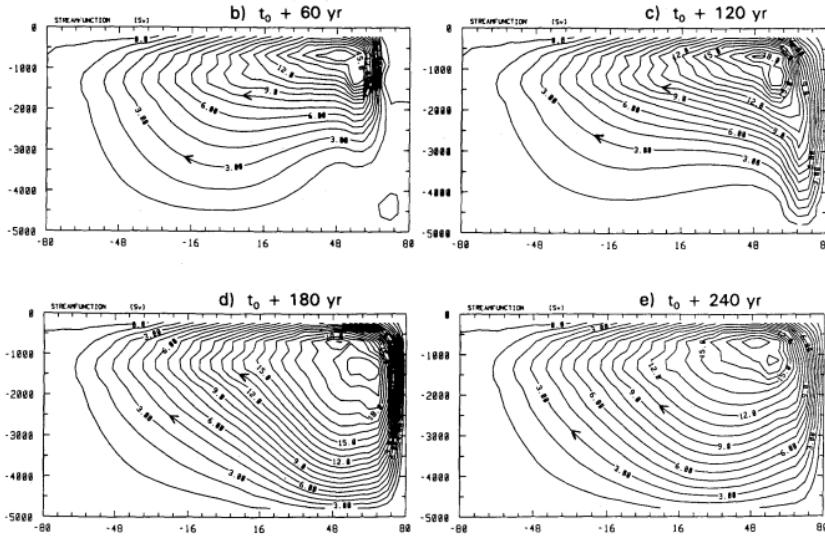
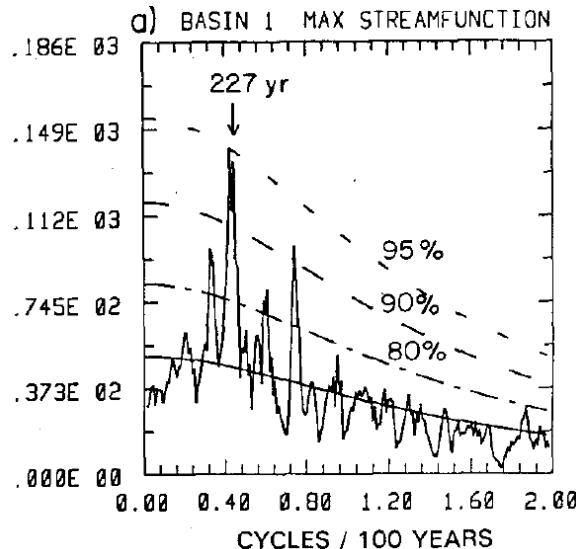


Fig. 3a-e. Streamfunction contours at 60-yr intervals which span the 240-yr oscillation EE' in Fig. 2. a $t = 6830 \text{ yr} = t_0$; b $t_0 + 60 \text{ yr}$; c $t_0 + 120 \text{ yr}$; d $t_0 + 180 \text{ yr}$, and e $t_0 + 240 \text{ yr}$ (end of oscillation)

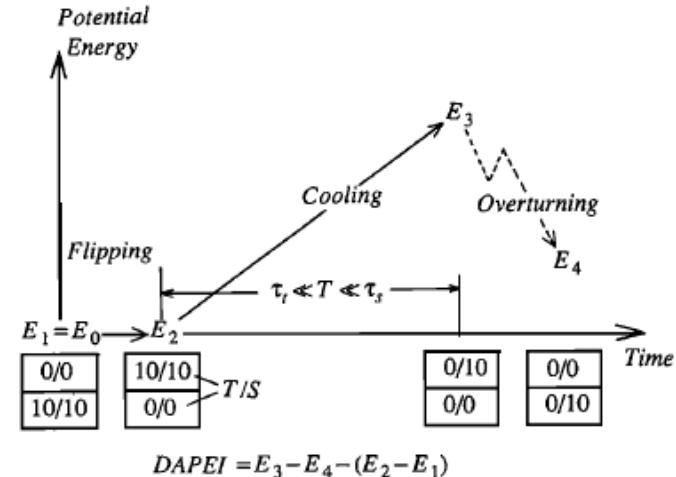
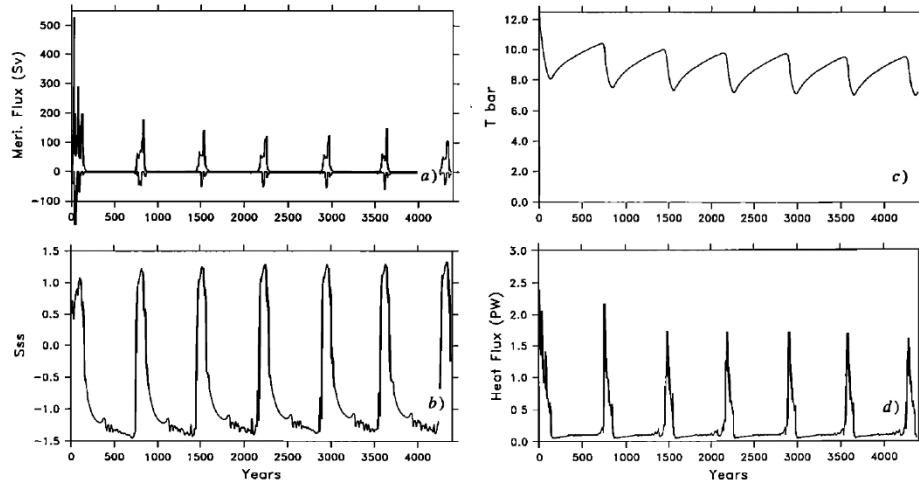


Period: 200-300 years of AMOC, Salinity advection feedback

Mysak et al., Climate Dynamics, 1993: Century-scale variability in a randomly forced, 2-D thermohaline ocean circulation model.

Energy Source: *Ocean Convection*

3-D OGCM with freshwater forcing, *centennial-millennial* oscillation

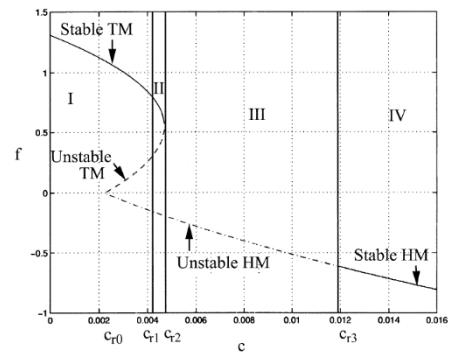
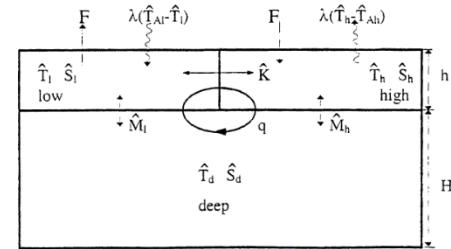
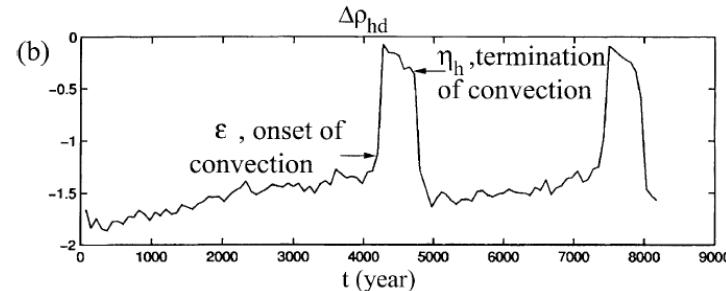
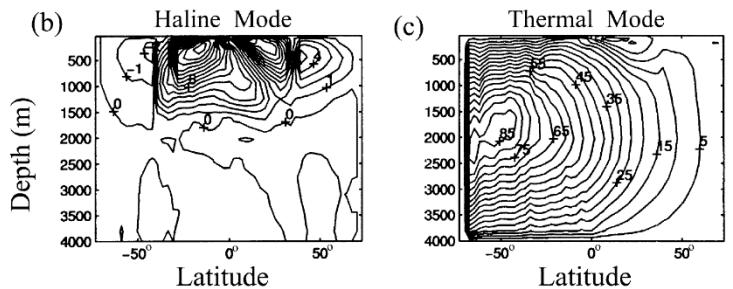
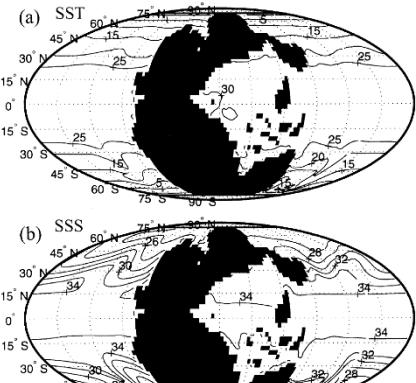


- Periodic oscillation of saline mode
- DAPE provides energy to saline mode's oscillation

Huang (1994): Thermohaline circulation: Energetics and variability in a single-hemisphere basin model. JGR-ocean

Multi-Equilibrium: *Self-Sustained Oscillation*

Late Permian, Equable climate and regime shift, *Millennial* oscillation

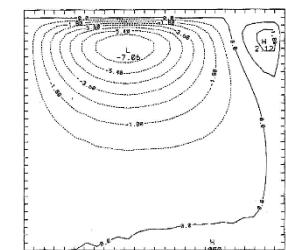
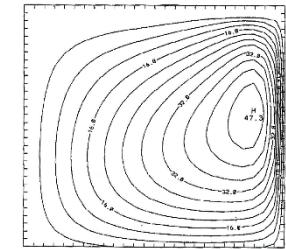
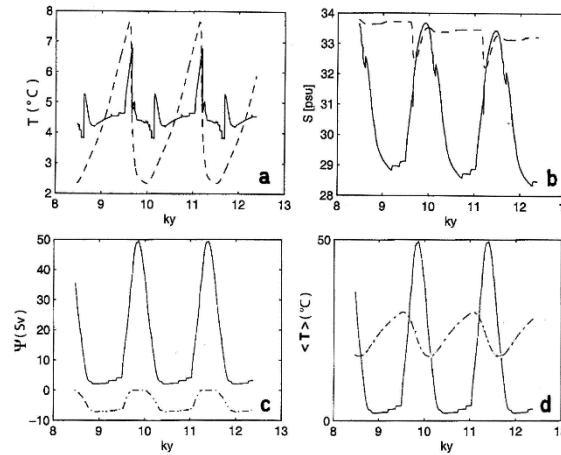
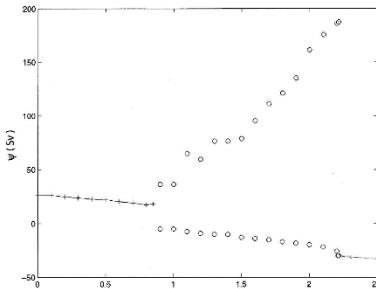
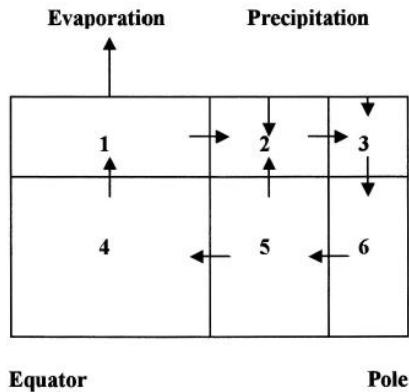


Such oscillations do not appear to occur in the modern ocean, because, apparently, the surface freshwater forcing is not strong enough. Mode switching is more likely to occur, perhaps, during glacial periods in which the freshwater forcing due to ice melting at polar regions is much stronger, or during warm equable paleoclimates such as the late Permian, or mid-Cretaceous in which the buoyancy forcing due to freshwater flux may have been stronger than the air-sea heat flux.

Zhang et al. (2002), Mechanism of thermohaline mode switching with application to warm equable climates. JC

Multi-Equilibrium: *Self-Sustained Oscillation*

Lowest-order 3x2-Box and 2D model, internal *Millennial* oscillation

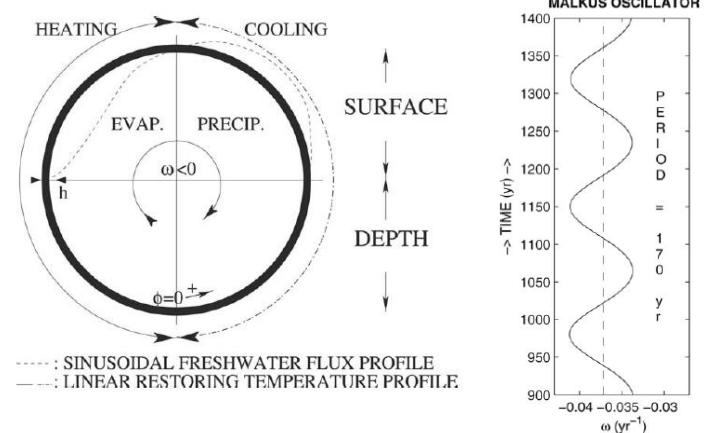
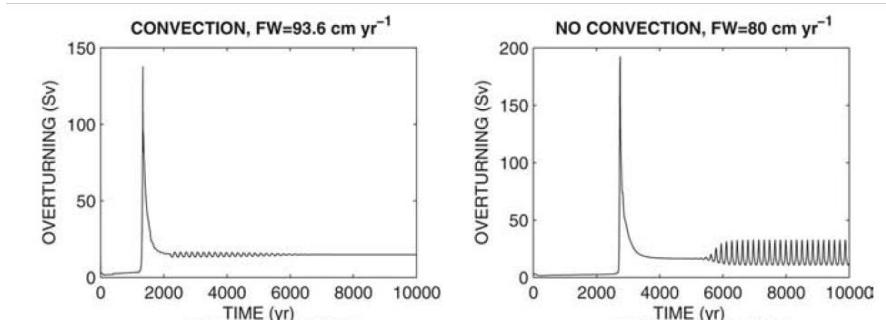


E-P increasing: stable thermal mode → oscillation mode → steady haline mode.

Colin De Verdière, Jelloul and Sevellec (2006), Bifurcation structure of thermohaline millennial oscillations. JC

Beyond Box Model

2-D model and 1-D Howard-Malkus loop model, internal *Centennial* oscillation



Left: 2-D model; Right: 1-D model of Howard-Malkus loop

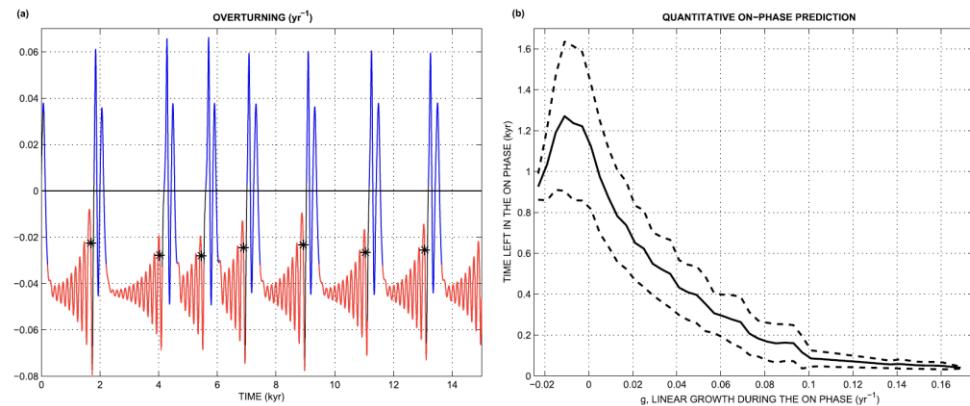
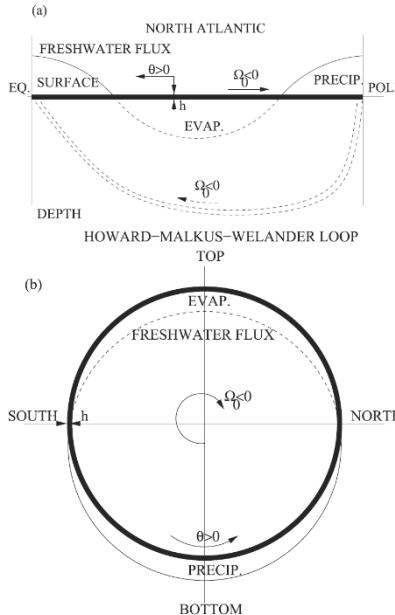
Not self-sustained: either strong damped or runaway mode

Nonlinear or linear; convection or no convection

Sévellec et al. (2006), On the mechanism of centennial thermohaline oscillations. J. Marine Research

Beyond Box Model

1-D Howard-Malkus loop model, AMOC *Millennial* regime shifts



AMOC *Millennial* shift is predictable in this chaotic model

Two predictive indices are defined

Sévellec & Fedorov (2014), Millennial variability in an idealized model: predicting the AMOC regime shifts

Centennial Oscillation in Coupled GCM

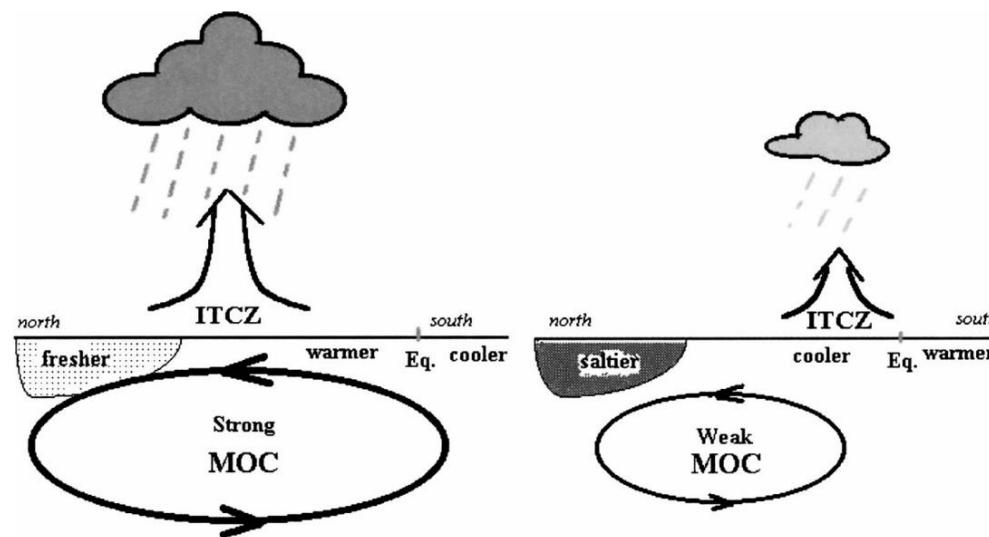


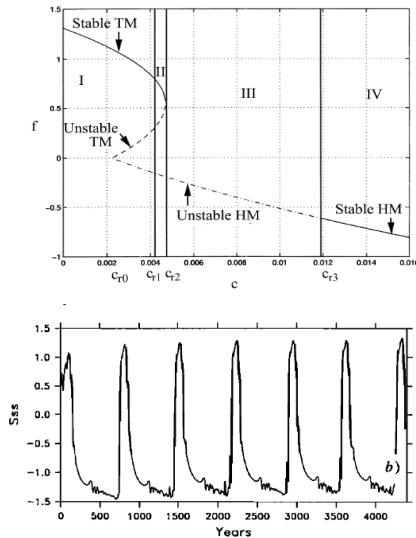
FIG. 16. Schematic of mechanism responsible for centennial THC fluctuation in HadCM3. When the THC is (left) strong ITCZ shifts northward, in response to enhanced SST gradient across equator. Fresh anomalies in the upper-ocean propagate northward and weaken the overturning. This results in the (right) weak phase.

- AMOC ↑ →
- Northward OHT ↑
- Cross Eq. ΔSST ↑
- ITCZ Northward Rain ↑
- Tropical Salinity ↓
- Northward S-advection ↓
- NADW Salinity ↓
- AMOC ↓

Vellinga and Wu (2004), Low-latitude freshwater influence on centennial variability of the Atlantic THC. JC

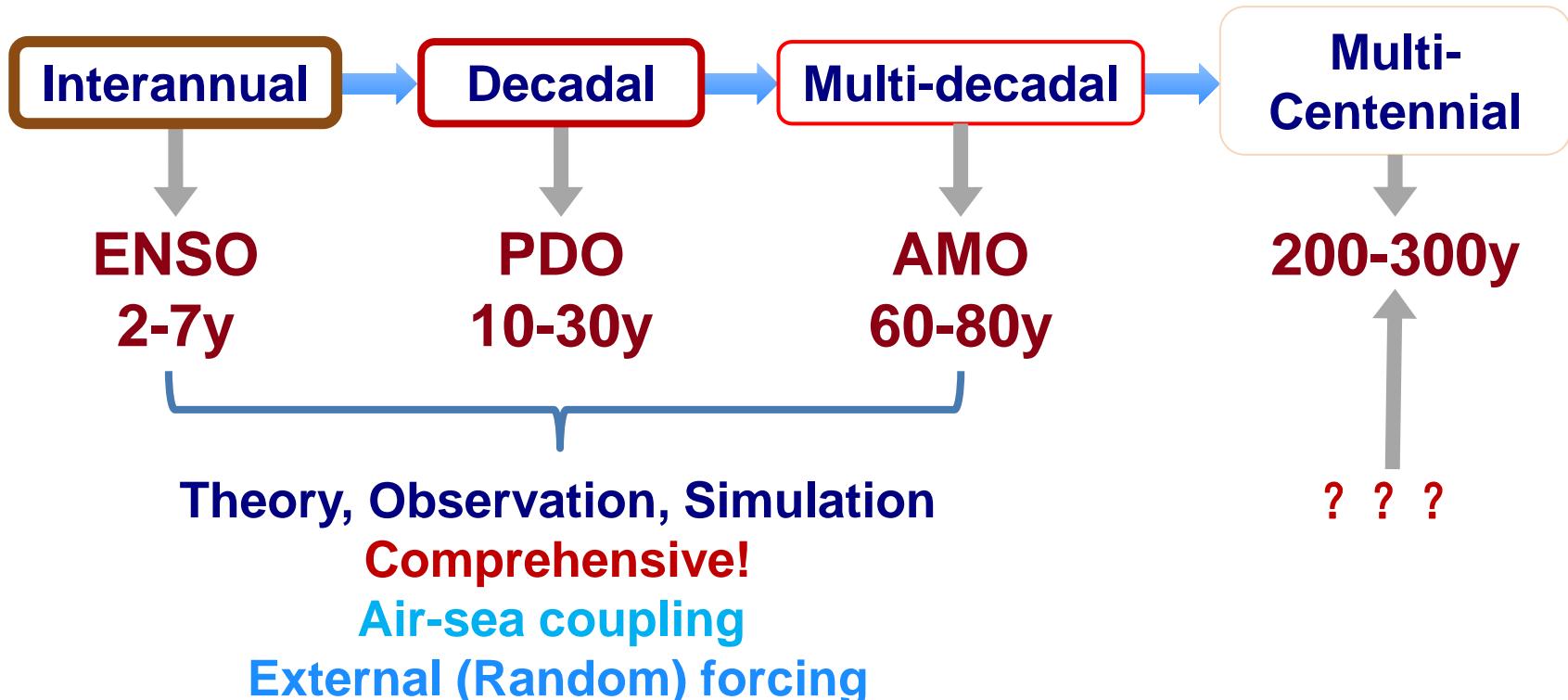
Previous Theoretical Studies: *Summary*

- THC: stability, bifurcation and regime shift
- Forcing: freshwater or/and stochastic
- Transition: thermal mode to haline mode
- Self-sustained oscillation: δ -function-like
- Not particularly on *Holocene*



No theory on the multicentennial variability in Holocene!

Climate Variability that *Ocean Matters*



We would like to

Search Eigen Mode

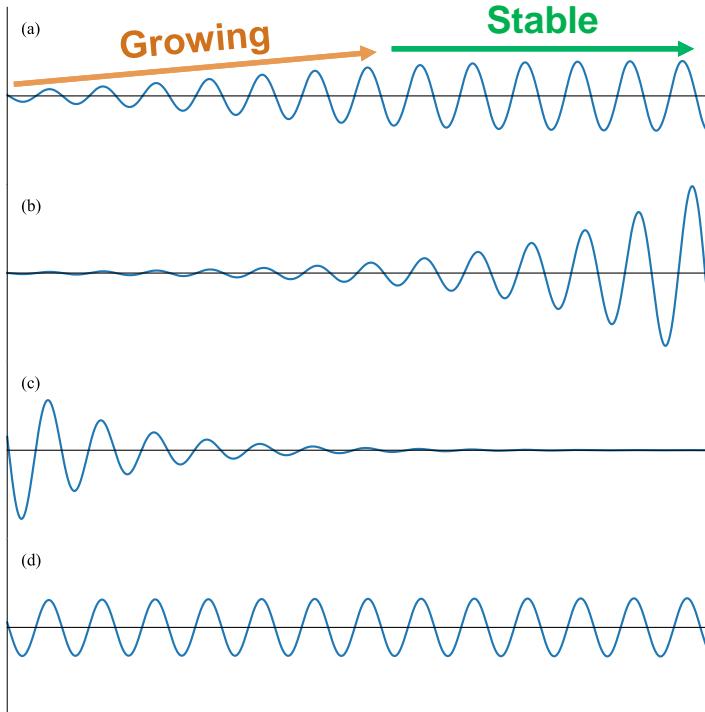


Multicentennial Climate Variability in a Stable Climate



Self-Sustained? ? ?

Self-Sustained Oscillation



Self-Sustained

Unstable

Damped

Neutral

1. Motivation

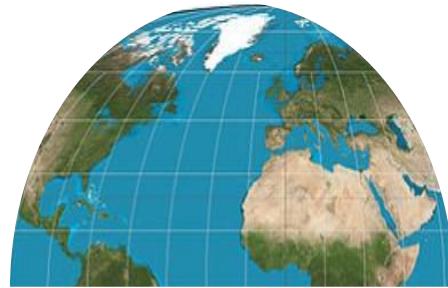
2. Observation

3. Our theory, Part I: Salinity

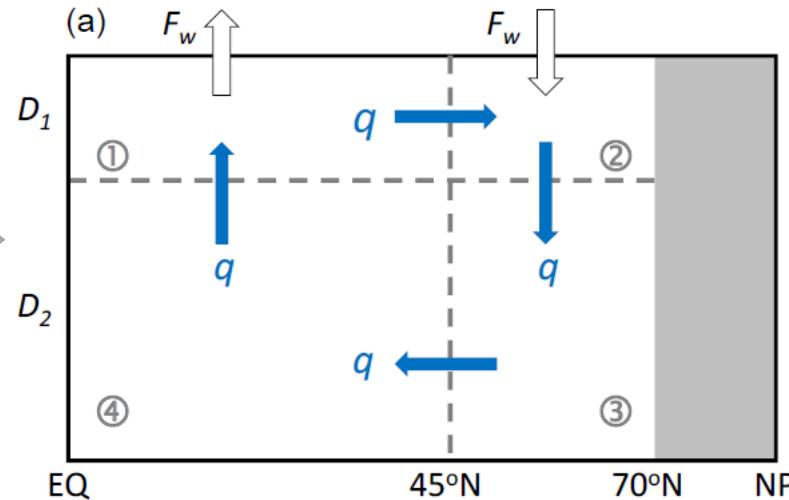
Part II: Temperature

4. Our Modelings

One Hemisphere 4-Box Model



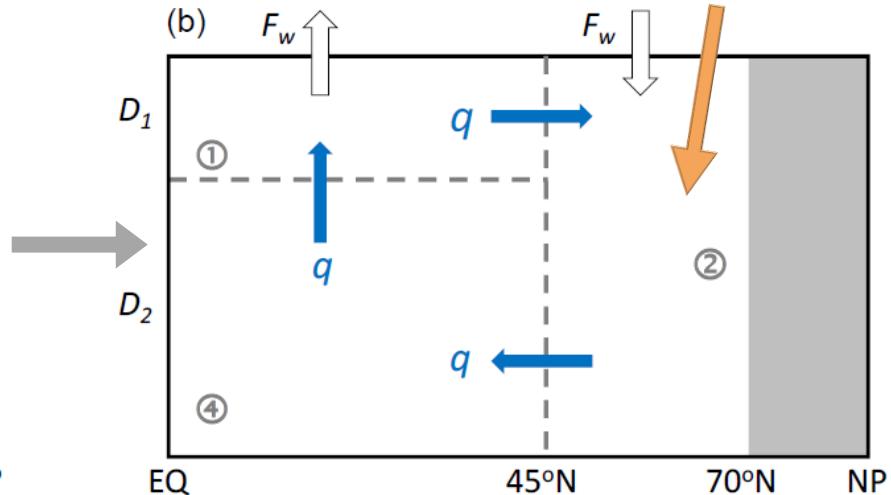
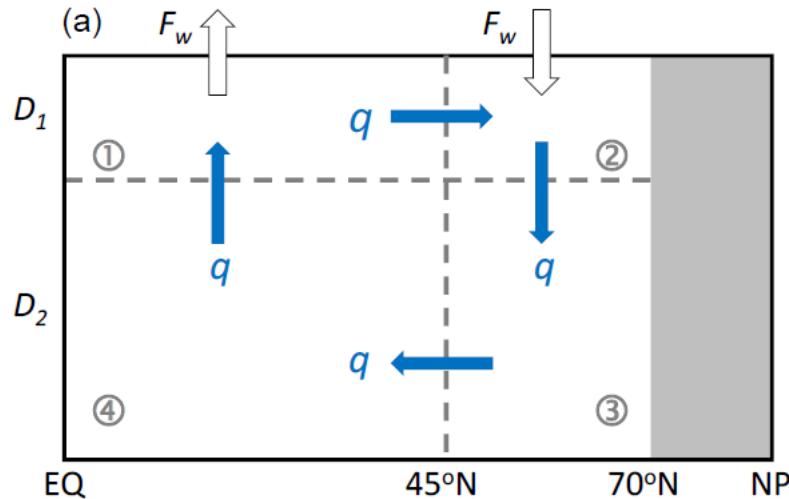
Only *Salinity* Considered



Li and Yang (2022)

One Hemisphere Box Model

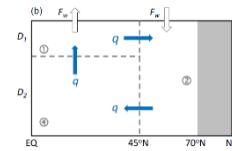
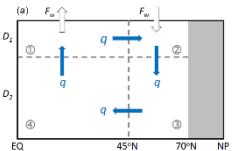
Extreme Mixing or Convection



Li and Yang (2022)



One Hemisphere Box Model



$$V_1 \dot{S}'_1 = q'(\bar{S}_4 - \bar{S}_1) + \bar{q}(S'_4 - S'_1)$$

$$V_2 \dot{S}'_2 = q'(\bar{S}_1 - \bar{S}_2) + \bar{q}(S'_1 - S'_2)$$

$$V_3 \dot{S}'_3 = q'(\bar{S}_2 - \bar{S}_3) + \bar{q}(S'_2 - S'_3)$$

$$V_4 \dot{S}'_4 = q'(\bar{S}_3 - \bar{S}_4) + \bar{q}(S'_3 - S'_4)$$



$$V_1 \dot{S}'_1 = q'(\bar{S}_4 - \bar{S}_1) + \bar{q}(S'_4 - S'_1)$$

$$V_2 \dot{S}'_2 = q'(\bar{S}_1 - \bar{S}_2) + \bar{q}(S'_1 - S'_2)$$

$$V_4 \dot{S}'_4 = q'(\bar{S}_2 - \bar{S}_4) + \bar{q}(S'_2 - S'_4)$$

$$V_1 S'_1 + V_2 S'_2 + V_4 S'_4 = \text{constant}$$

$$\Delta\rho' = \rho_0\beta[\delta(S'_2 - S'_1) + (1 - \delta)(S'_3 - S'_4)], \text{ and } \delta = \frac{V_1}{V_1 + V_4} = \frac{V_2}{V_2 + V_3} = \frac{D_1}{D}$$

$$q' = \lambda\Delta\rho' = \lambda\rho_0\beta[S'_2 - \delta S'_1 - (1 - \delta)S'_4], \text{ and } \delta = \frac{V_1}{V_1 + V_4} = \frac{D_1}{D}$$

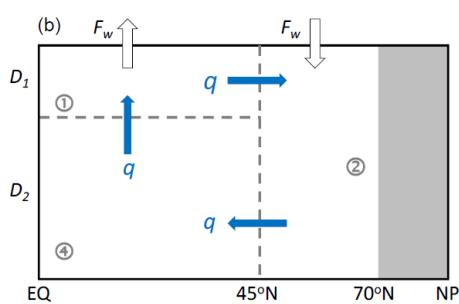
AMOC sensitivity to Density

A linear closure method:

$$\text{AMOC} \rightarrow q' = \lambda \Delta \rho' \leftarrow \text{Meridional Density Gradient}$$

λ : linear closure parameter, **critical** to the oscillatory behavior
Controlling the AMOC change in response to the meridional density gradient change

Theoretical Solution to 3-Box Model



Li and Yang (2022)

$$\omega = \frac{1}{2} \left[(C_2 M - C_3) \pm \sqrt{(C_2 M - C_3)^2 - 4C_2 C_4 (1 - M)} \right]$$

Stability Condition

$$M \leq \min\left(\frac{C_3}{C_2}, 1\right)$$

Oscillation Condition

$$M_1 < M < \min(M_2, 1)$$

$$M_1 = \frac{C_3 - 2C_4}{C_2} - \frac{2}{C_2} \sqrt{C_4^2 + C_4(C_2 - C_3)}, \quad M_2 = \frac{C_3 - 2C_4}{C_2} + \frac{2}{C_2} \sqrt{C_4^2 + C_4(C_2 - C_3)}.$$

$M = \frac{\rho_d}{\bar{q}} \lambda$: nondimensional form of λ

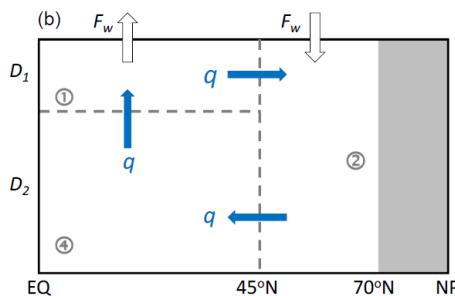
Parameter for the Box Model and Eigenvalues

4-box *Growing* Oscillatory mode ($0.31+5.83i$) 0 -37.4

3-box *Damped* Oscillatory mode ($-0.29+5.78i$)

Symbol	Physical meaning	Value
V_2	Volume of upper subpolar Atlantic box	$2.8 \times 10^{15} \text{ m}^3$
V_1, V_3, V_4	Volumes of upper tropical Atlantic, lower subpolar Atlantic, and lower tropical Atlantic boxes, respectively	$5V_2, 7V_2, 35V_2$
D_1, D_2, D $\bar{S}_1, \bar{S}_2, \bar{S}_3, \bar{S}_4$	Depths of upper box, lower box, and total, respectively Reference salinity values of the four ocean boxes	500, 3500, 4000 m 36, 33.5, 33.5, 33.5 psu
\bar{q}	Equilibrium AMOC strength	$10 \text{ Sv } (10^6 \text{ m}^3 \text{ s}^{-1})$
F_w	Total virtual salt flux	$2.50 \times 10^7 \text{ psu m}^3 \text{ s}^{-1}$
β	Haline contraction coefficient	$7.61 \times 10^{-4} \text{ psu}^{-1}$
ρ_0	Reference density	$1.00 \times 10^3 \text{ kg m}^{-3}$
λ	Linear closure coefficient	$12 \text{ Sv kg}^{-1} \text{ m}^{-3}$

Stability Condition for 3-Box Model



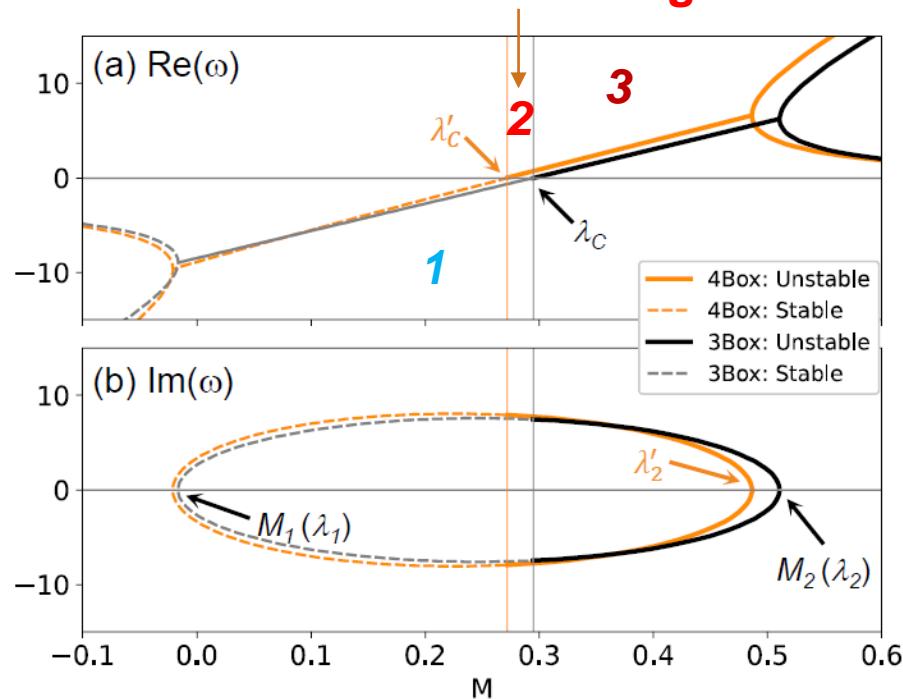
Li and Yang (2022)

$$\lambda < \lambda_C \equiv \frac{\bar{q}^2}{\rho_0 \beta \bar{F}_w} \left[1 + \frac{\delta_2}{\delta(1-\delta)} \right]$$

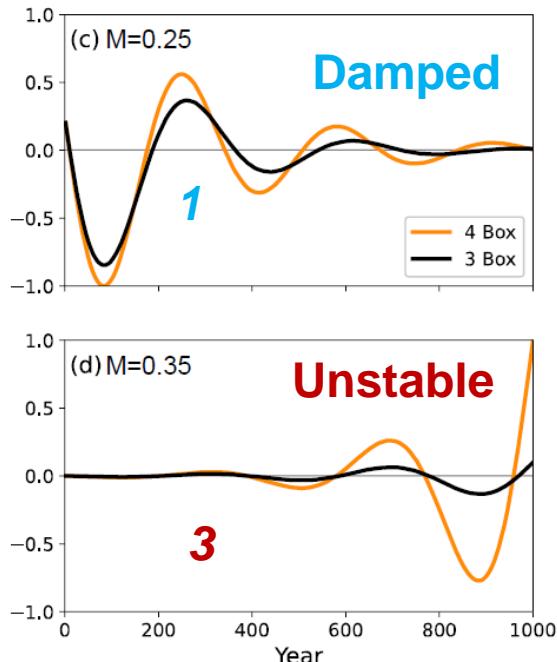
λ_C : the critical linear closure parameter when $Re[\omega] = 0$, determined by \bar{q} , \bar{F}_w and basin geometry. A stronger \bar{F}_w and a weaker \bar{q} give a smaller λ_C , implying higher possibility for an unstable oscillation, since the background meridional salinity gradient in this situation will be stronger. In addition, salinity anomalies also spend more time at the surface with a weaker \bar{q} . This will also make the system more unstable, and this is why we have a quadratic term of \bar{q} . A bigger volume of the subpolar ocean (δ_2) gives a larger λ_C , implying a higher probability for a stable oscillation. In this situation, the salinity difference anomaly between subpolar and tropical upper oceans is larger under the same q' , and thus the mean advection of salinity anomaly is stronger, which would result in a stronger stabilizing effect.

Oscillatory Modes with λ

Self-Sustained Regime

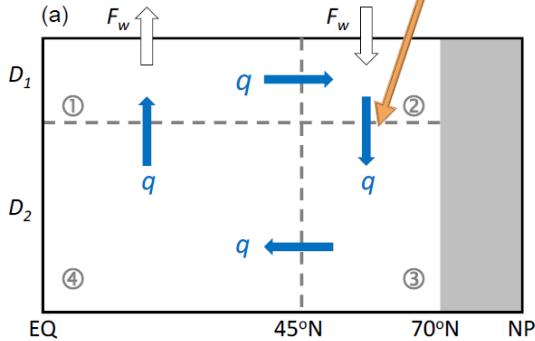


Li and Yang (2022)



How to *Realize a Self-Sustained Oscillation*?

An Enhanced Mixing or Convection



$$V_2 \dot{S}'_2 = q'(\bar{S}_1 - \bar{S}_2) + \bar{q}(S'_1 - S'_2) - k_m(S'_2 - S'_3)$$

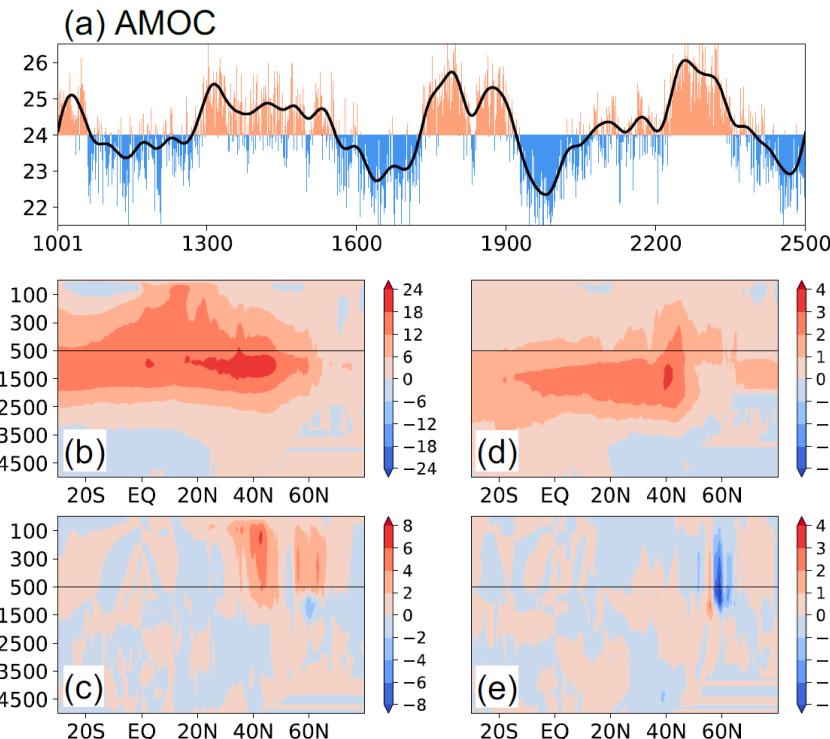
$$V_3 \dot{S}'_3 = \bar{q}(S'_2 - S'_3) + k_m(S'_2 - S'_3)$$

$k_m = \kappa q'^2$: Proportional to AMOC anomaly

What *Enhanced* Mixing or Convection?

Eulerian-mean

Eddy-induced



Euler AMOC \uparrow



Vertical diffusion \uparrow

Eddy AMOC \uparrow

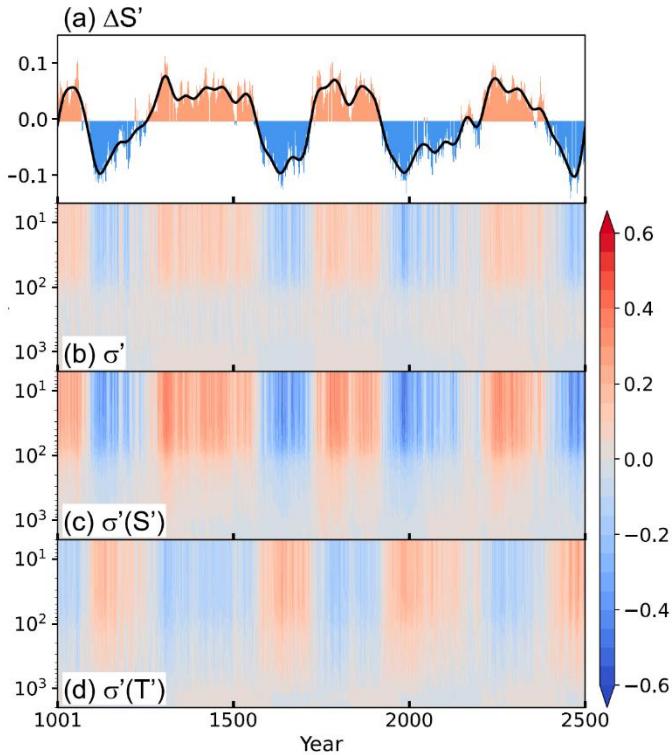


Vertical mixing \uparrow

What *Enhanced* Mixing or Convection?

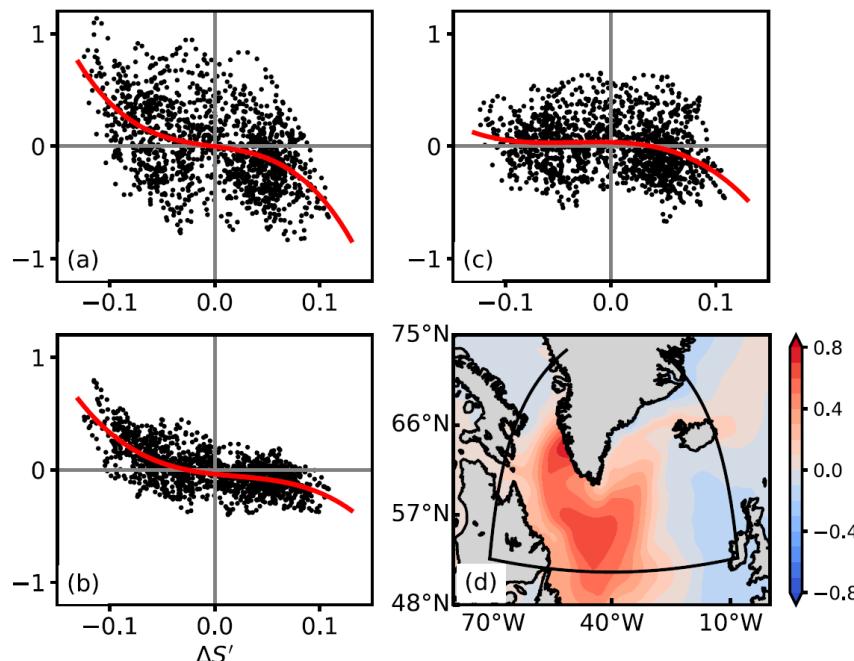
Stratification in Subpolar Atlantic

AMOC $\sim \sigma' \sim S' \sim -T'$



What *Enhanced* Mixing or Convection?

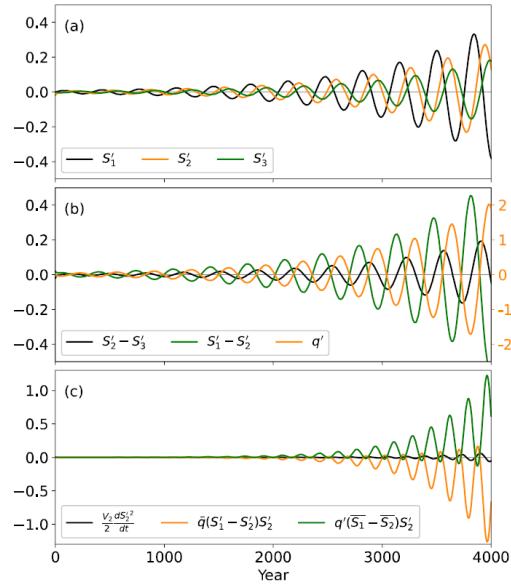
Mixing $\sim \Delta S'$



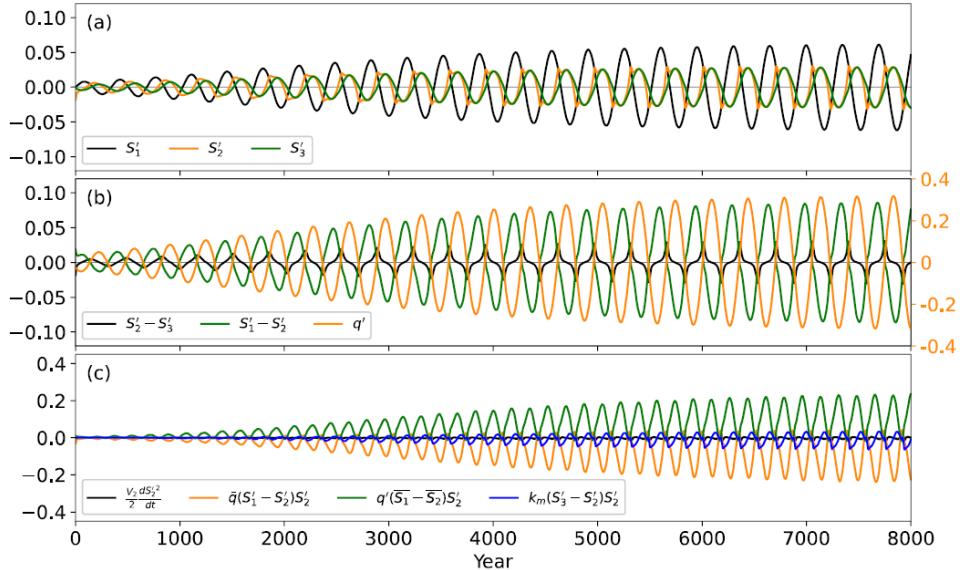
$$F_{\text{mixing}} \sim -(\Delta S')^3 \sim -(q')^2 \Delta S' \sim -k_m \Delta S'$$

Self-Sustained Oscillation

Without k_m



With k_m

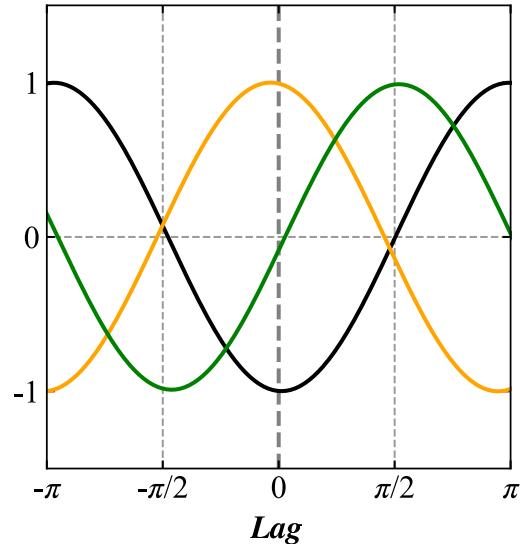


Can be only realized in 4-Box model

Li and Yang (2022)

Self-Sustained Oscillation: *Physics*

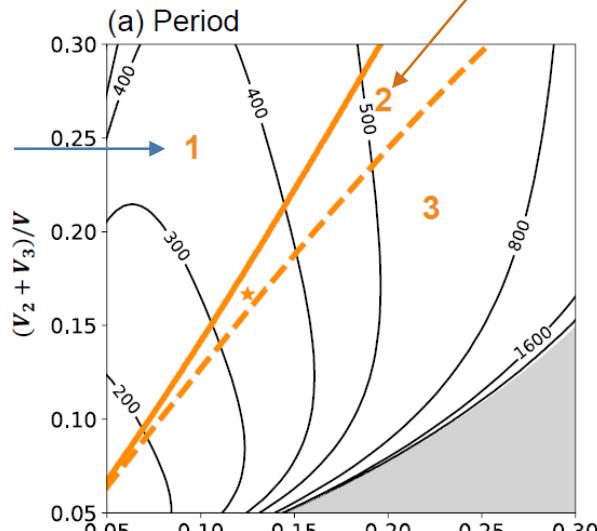
$$q'(S'_2) \sim \begin{cases} q'(\bar{S}_1 - \bar{S}_2) & \text{Local Term Positive Feedback} \\ \bar{q}(S'_1 - S'_2) & \text{Advection Term Negative Feedback} \\ -k_m(S'_2 - S'_3) & \text{Enhanced Mixing Negative Feedback} \end{cases}$$



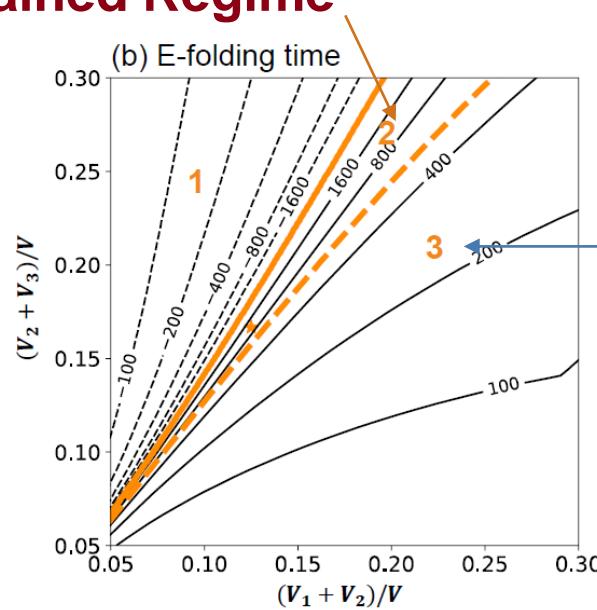
Li and Yang (2022); Yang et al. (2022)

Self-Sustained Oscillation in Ocean Space

Damped
Regime



Self-Sustained Regime

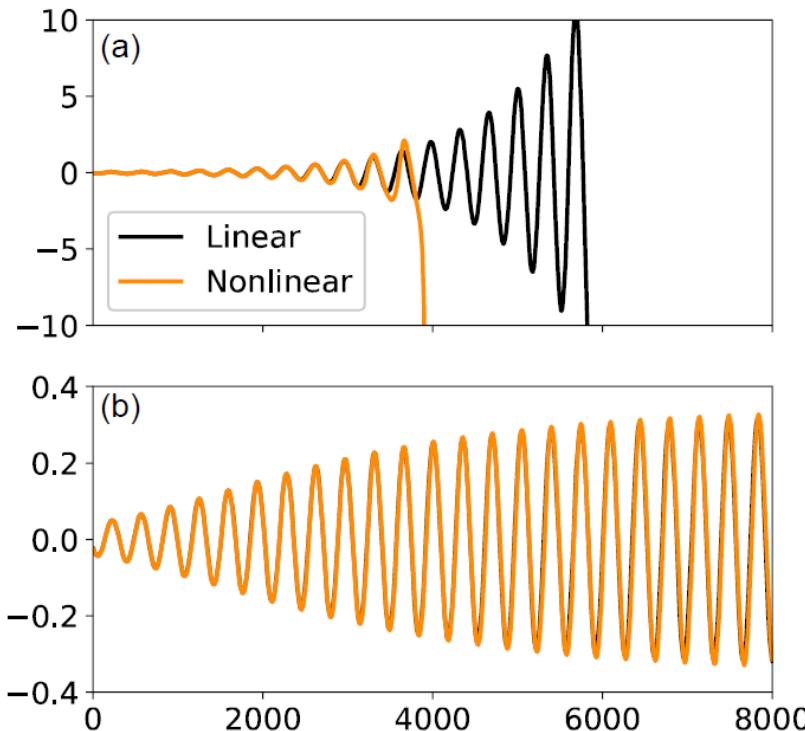


Unstable
Regime

Li and Yang (2022)

Nonlinear Advection Effect

$q'(S'_1 - S'_2)$

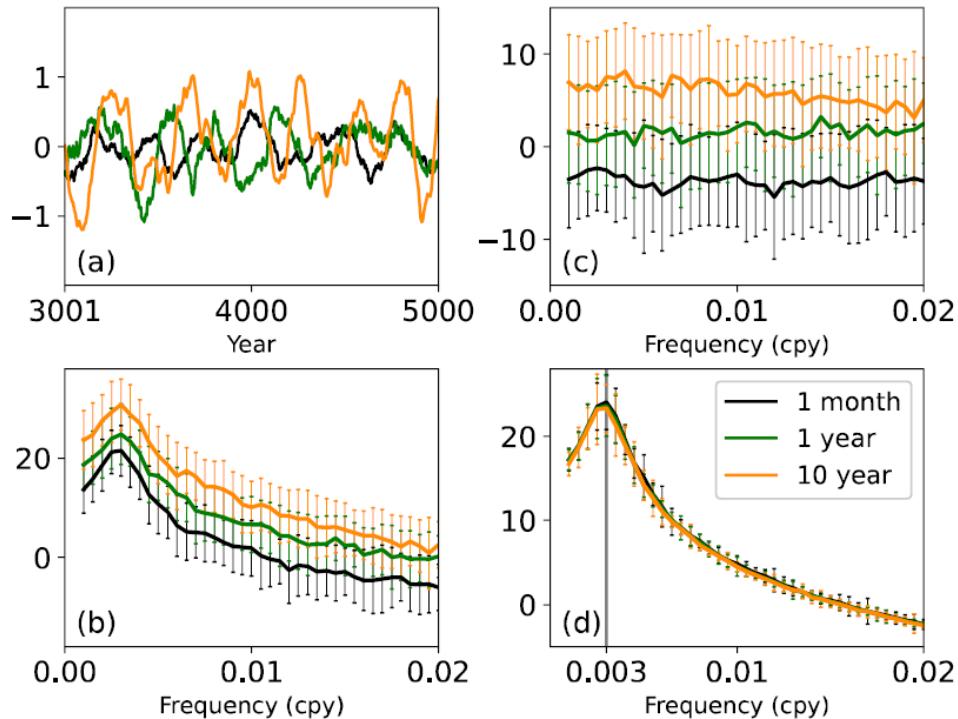


Without k_m

With k_m

Li and Yang (2022)

Self-Sustained Oscillation Excited by *Stochastic Forcing*



Li and Yang (2022)

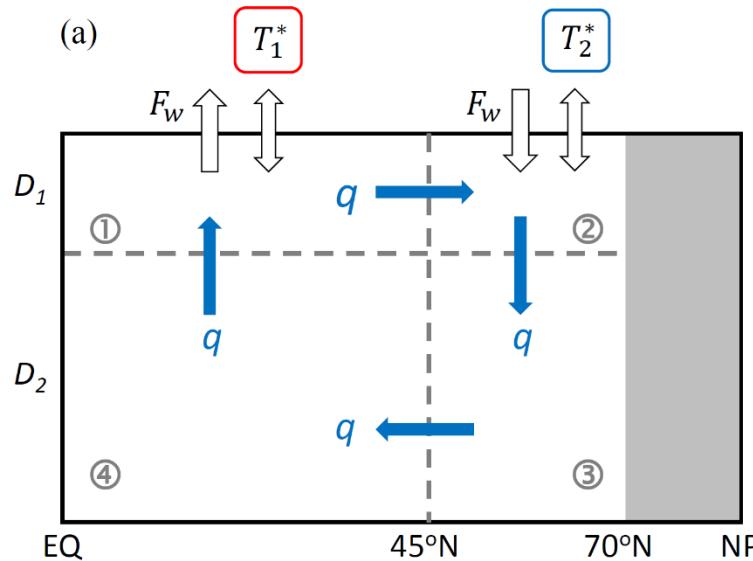
1. Motivation
2. Observation
3. Out theory, Part I: Salinity

Part II: Temperature

4. Modeling – CGCM or OGCM

One Hemisphere 4-Box Model

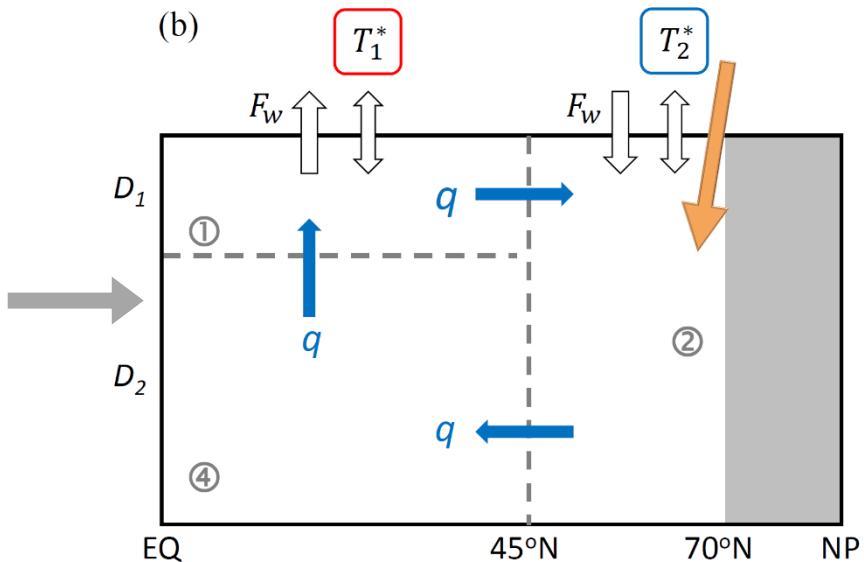
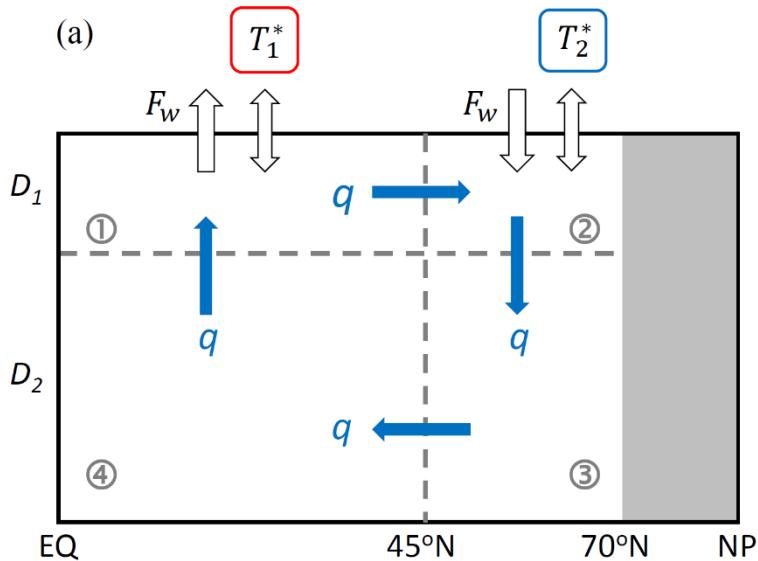
Both *Temperature* and *Salinity* Considered



Yang et al. (2022)

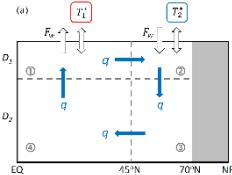
One Hemisphere 4-Box Model

Extreme Mixing or Convection



Li and Yang (2022)

One Hemisphere 4-Box Model



$$V_1 \dot{T}_1 = q(T_4 - T_1) + V_1 \tau(T_1^* - T_1)$$

$$V_2 \dot{T}_2 = q(T_1 - T_2) + V_2 \tau(T_2^* - T_2)$$

$$V_3 \dot{T}_3 = q(T_2 - T_3)$$

$$V_4 \dot{T}_4 = q(T_3 - T_4)$$

$$V_1 \dot{S}_1 = q(S_4 - S_1) + F_w$$

$$V_2 \dot{S}_2 = q(S_1 - S_2) - F_w$$

$$V_3 \dot{S}_3 = q(S_2 - S_3)$$

$$V_4 \dot{S}_4 = q(S_3 - S_4)$$



$$\overline{T}_1 = T_1^* - \frac{\bar{q}V_2(T_1^* - T_2^*)}{\bar{q}(V_1 + V_2) + V_1V_2\tau}, \quad \overline{T}_2 = \frac{V_1T_1^* + V_2T_2^* - V_1\overline{T}_1}{V_2} = \overline{T}_3 = \overline{T}_4$$

$$\overline{S}_1 = F_w/\bar{q} + \overline{S}_2, \quad \overline{S}_2 = \overline{S}_3 = \overline{S}_4$$

$$1/\tau = \frac{\rho_w c \Delta z A}{\kappa_0 A} = \frac{\rho_w c \Delta z}{\kappa_0}$$

$$q = \bar{q} + q'$$

$$q' = q'_T + q'_S = \lambda \Delta \rho'_T + \lambda \Delta \rho'_S = \lambda \Delta \rho'$$

$$\Delta \rho'_T = -\rho_0 \alpha [\delta(T'_2 - T'_1) + (1 - \delta)(T'_3 - T'_4)]$$

$$\Delta \rho'_S = \rho_0 \beta [\delta(S'_2 - S'_1) + (1 - \delta)(S'_3 - S'_4)]$$

$$\delta = \frac{V_1}{V_1 + V_4} = \frac{V_2}{V_2 + V_3} = \frac{D_1}{D}$$

Yang et al. (2022)

AMOC sensitivity to Density

A linear closure method:

$$\text{AMOC} \rightarrow q' = \lambda \Delta \rho' \leftarrow \text{Meridional Density Gradient}$$

λ : linear closure parameter, **critical** to the oscillatory behavior
Controlling the AMOC change in response to the meridional density gradient change

Eigenvalues: 4TS vs 4S

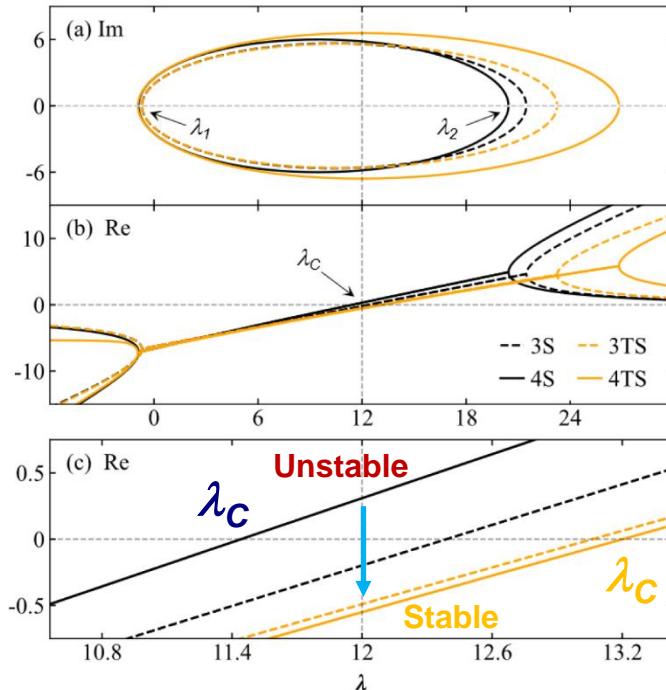
4S-box	<i>Growing</i> Oscillatory mode ($0.31 \pm 5.83i$)	0	-37.4
4TS-box	<i>Damped</i> Oscillatory mode ($-0.55 \pm 6.59i$)	0	-37.4, -366
		0	-366, -324
		0	-5.28, -0.78



Oscillatory Modes with λ

Temperature
makes
system
more
damped!

Bigger
 λ_C
requires
bigger
sensitivity!



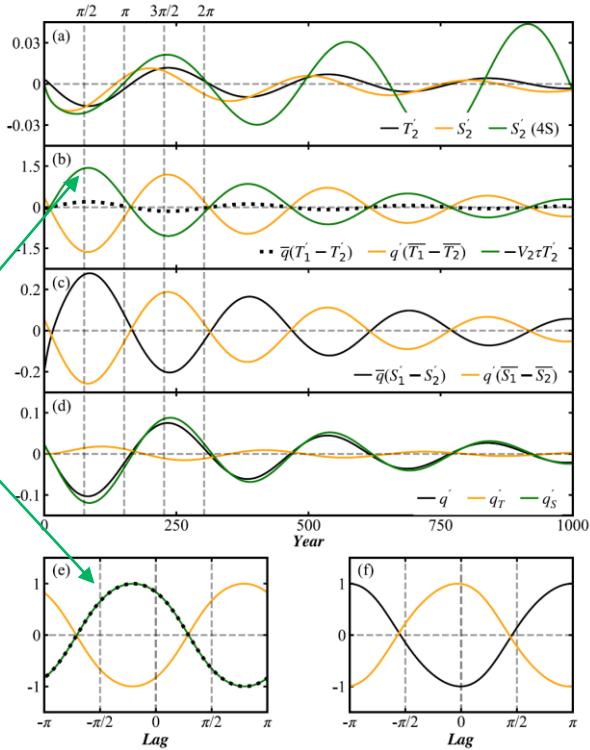
Yang et al. (2022)

Oscillation with T and S

Temperature turn
unstable into *damped!*

Positive
restoring feedback

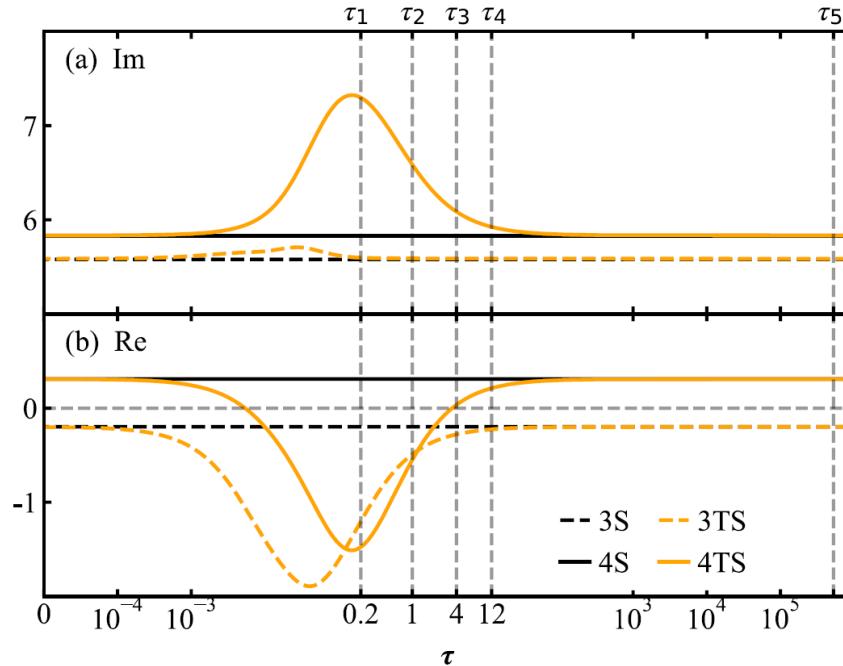
Salinity
dominates AMOC



Yang et al. (2022)

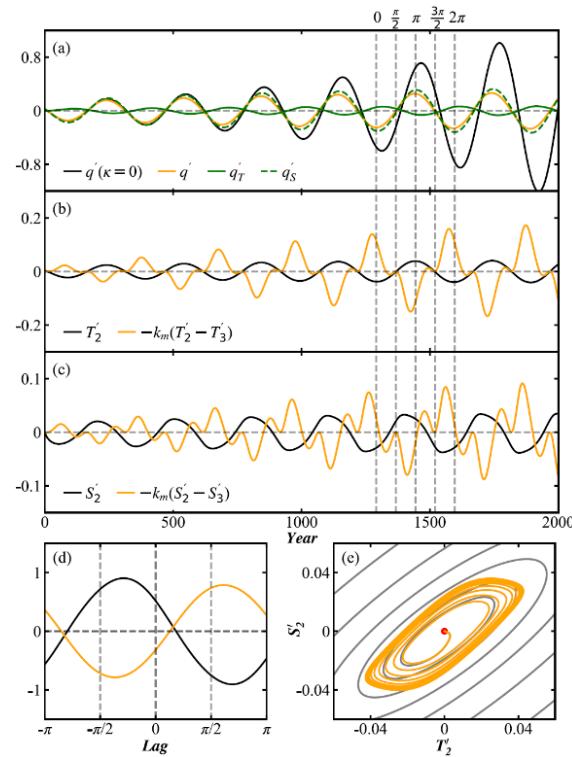
Role of *Restoring* Temperature

Restoring
feedback
Contained!



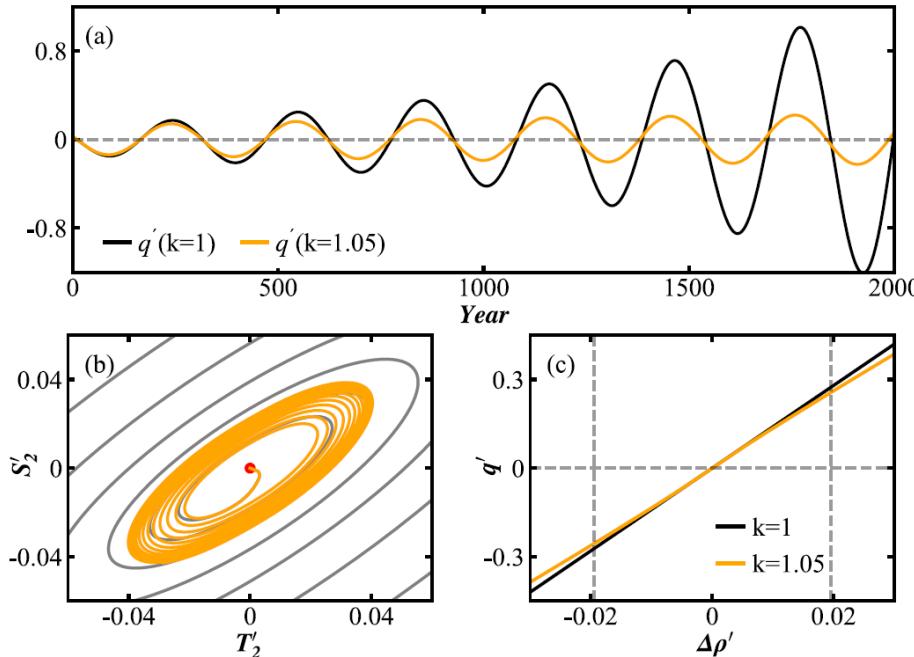
Yang et al. (2022)

Self-sustained Oscillation With Enhanced Mixing



Yang et al. (2022)

Self-sustained Oscillation With Nonlinear Closure



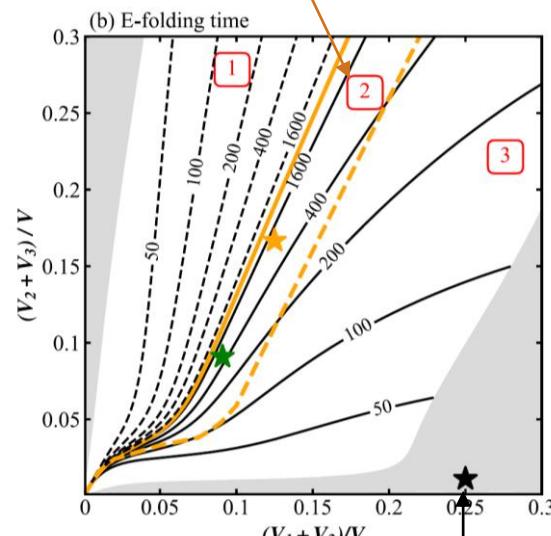
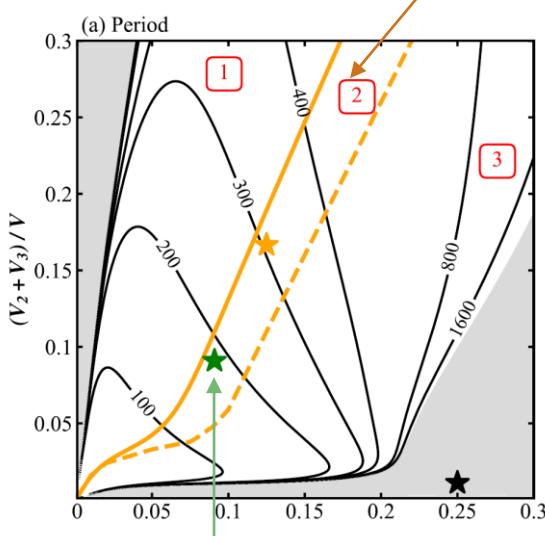
A tiny nonlinearity makes the system **Self-sustained!**

$$q' = \begin{cases} \lambda\rho_{cri} \left[k \left(\left[\frac{\Delta\rho'}{\rho_{cri}} \right]^{\frac{1}{k}} - 1 \right) + 1 \right], & \text{if } \Delta\rho' > \rho_{cri} \\ \lambda\Delta\rho' & \text{if } -\rho_{cri} < \Delta\rho' < \rho_{cri} \\ -\lambda\rho_{cri} \left[k \left(\left[-\frac{\Delta\rho'}{\rho_{cri}} \right]^{\frac{1}{k}} - 1 \right) + 1 \right], & \text{if } \Delta\rho' < -\rho_{cri} \end{cases}$$

Yang et al. (2022)

Self-Sustained Oscillation in Ocean Space

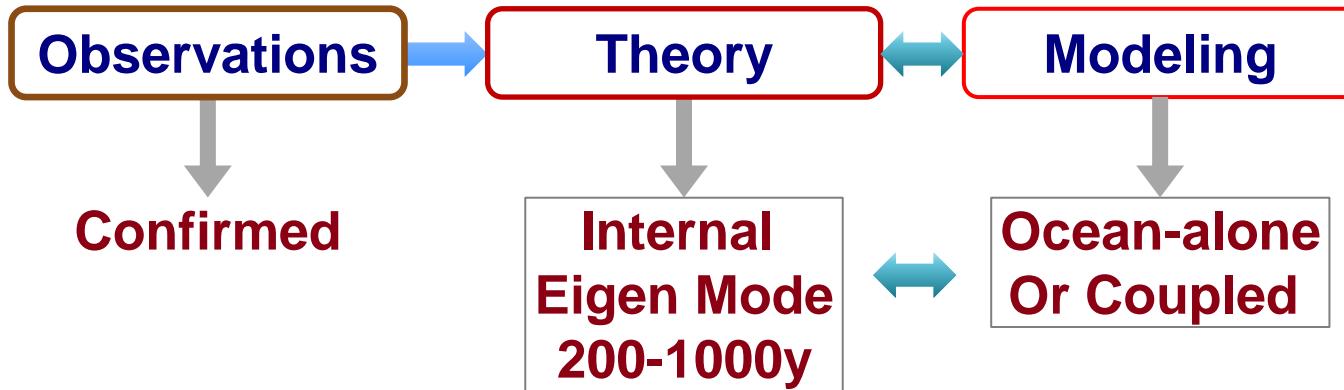
Self-Sustained Regime



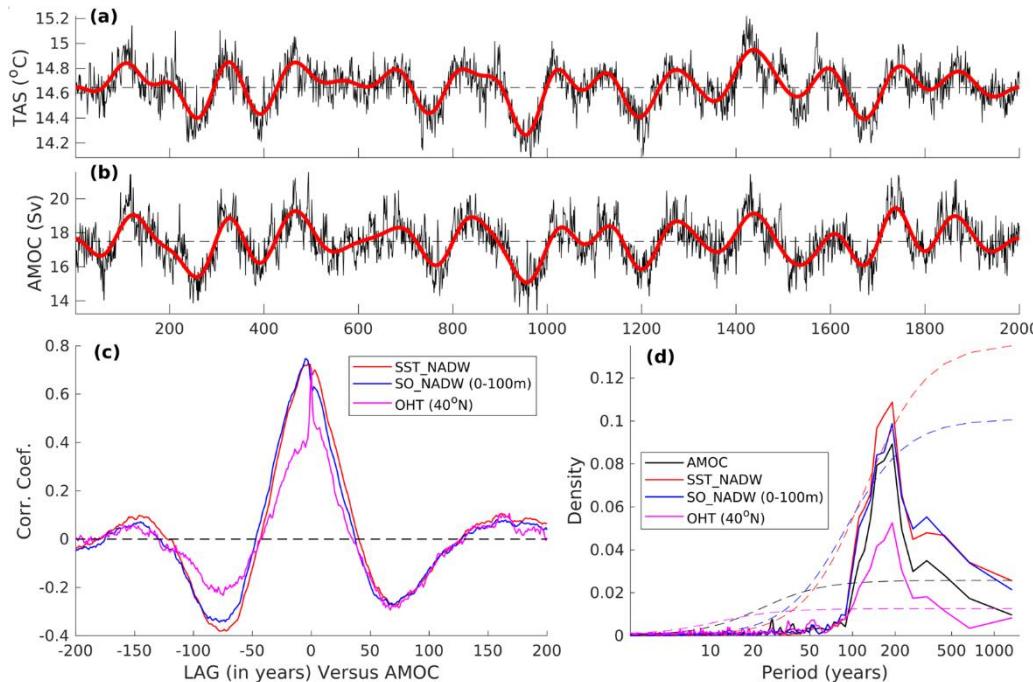
Yang et al. (2022)

1. Motivation
2. Observation
3. Theory
4. Modeling – CGCM or OGCM

Centennial-Millennial Variabilities



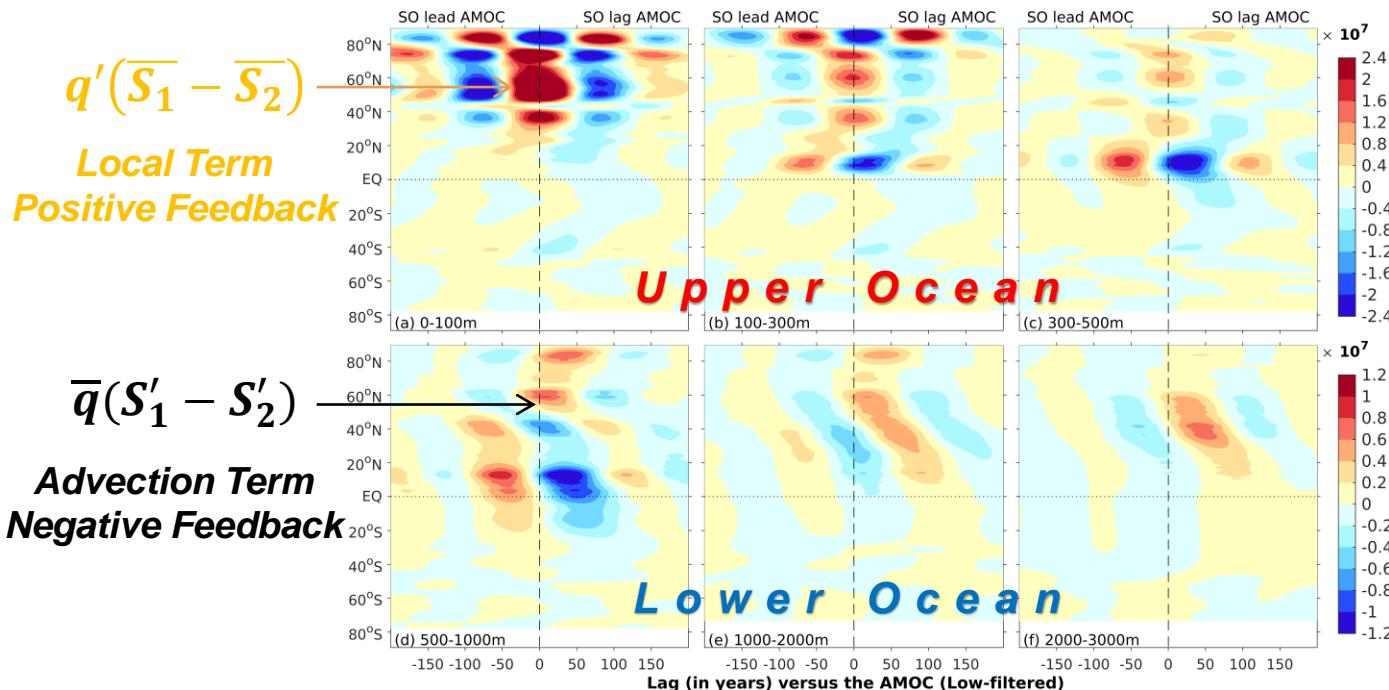
MCO in EC-Earth3.0: 200 Years



Cao et al., 2023: On the mechanisms in sustaining multi-centennial variability of the Atlantic meridional overturning circulation in EC-Earth3-LR simulation. ERL, accepted.

MCO in EC-Earth3.0: 200 Years

Salinity regression on AMOC



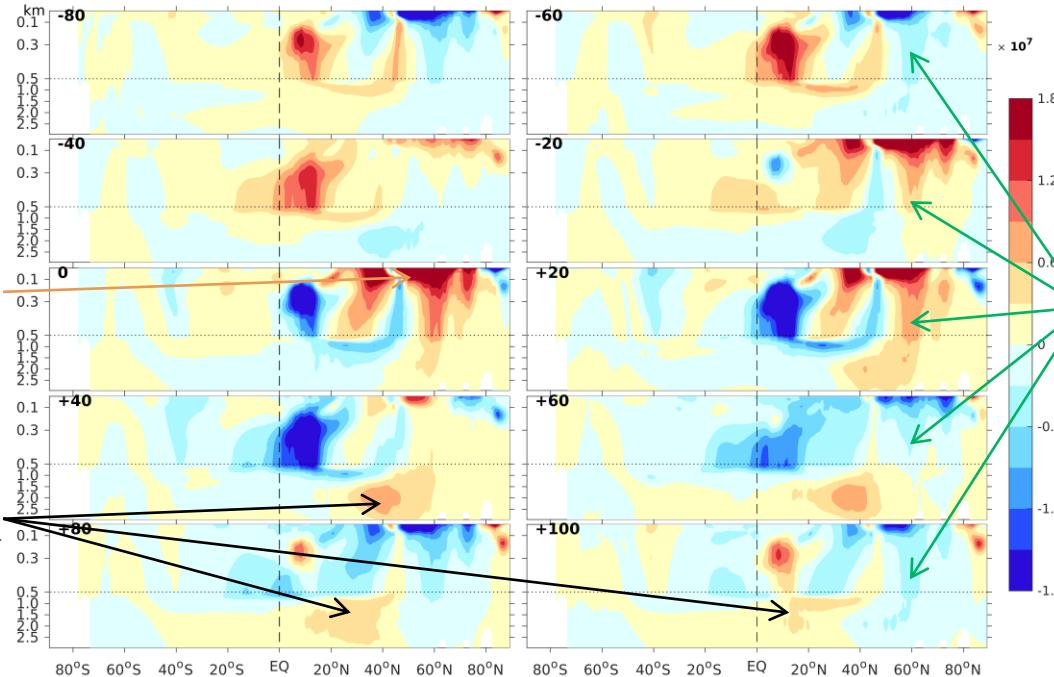
Cao et al., 2023: On the mechanisms in sustaining multi-centennial variability of the Atlantic meridional overturning circulation in EC-Earth3-LR simulation. ERL, accepted.

MCO in EC-Earth3.0: 200 Years

Salinity regression on AMOC

Local Term
Positive Feedback

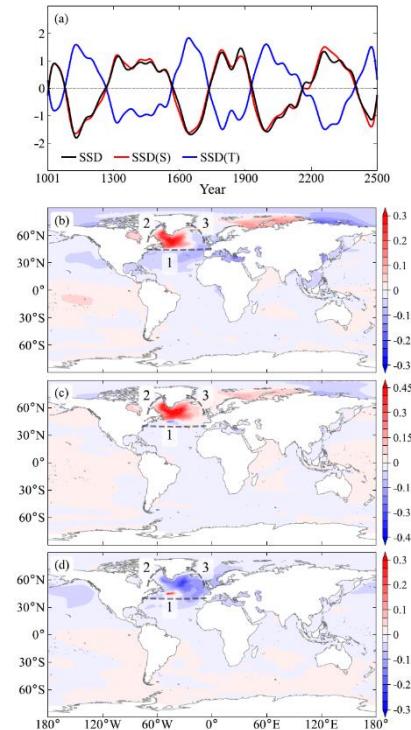
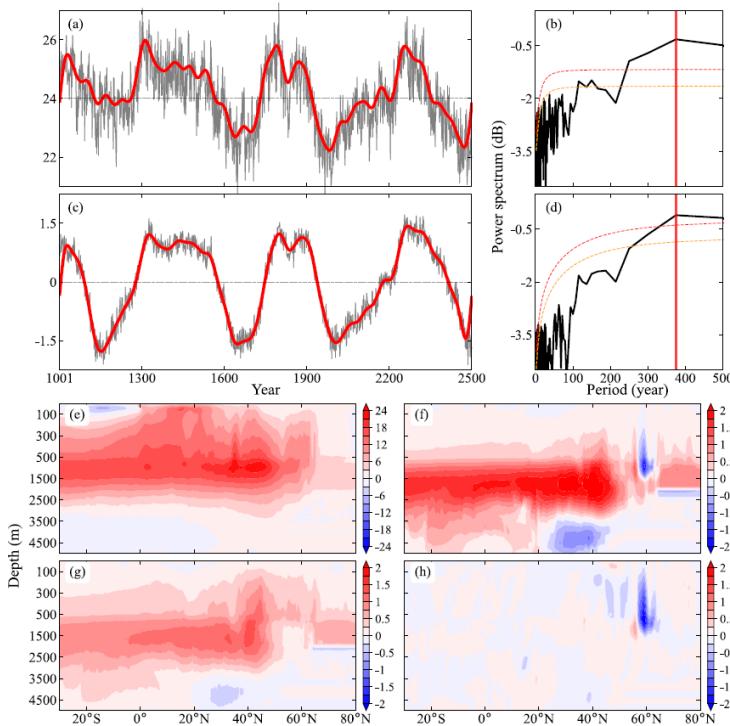
Advection Term
Negative Feedback



$-k_m(S'_2 - S'_3)$
Enhanced Mixing
Negative Feedback

Cao et al., 2023: On the mechanisms in sustaining multi-centennial variability of the Atlantic meridional overturning circulation in EC-Earth3-LR simulation. ERL, accepted.

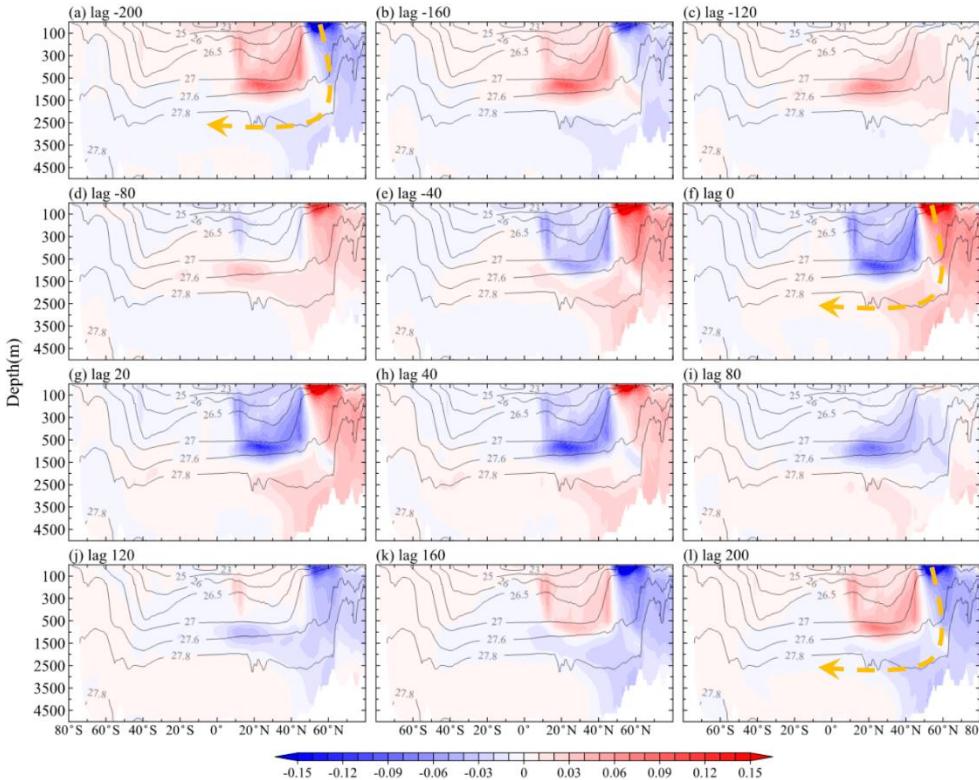
MCO in CESM1.0: 350 Years



Yang et al., 2023: North Atlantic Ocean-originated multicentennial oscillation of the AMOC: a coupled model study. *J. Climate*. Submitted.

MCO in CESM1.0: 350 Years

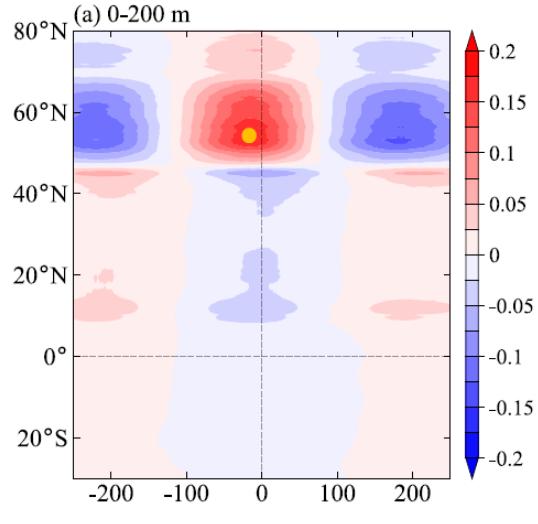
Salinity regression on AMOC



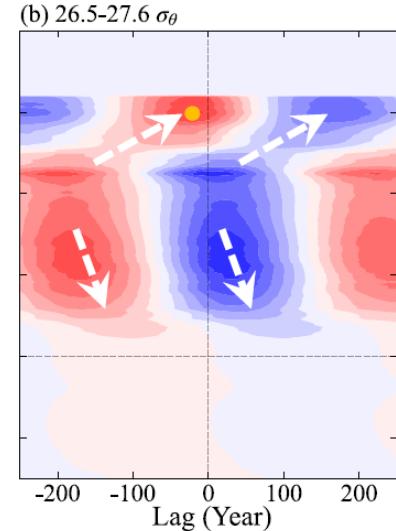
MCO in CESM1.0: 350 Years

Salinity regression on AMOC

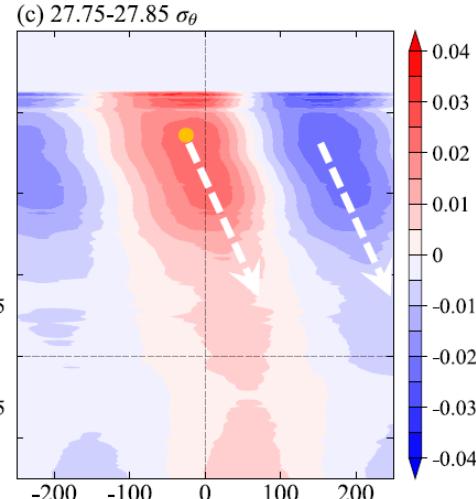
Upper Ocean



Intermediate Ocean

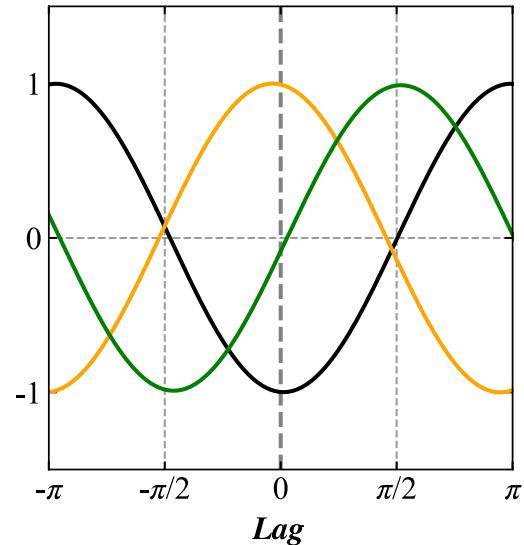


Deep Ocean



Self-Sustained Oscillation: *Physics*

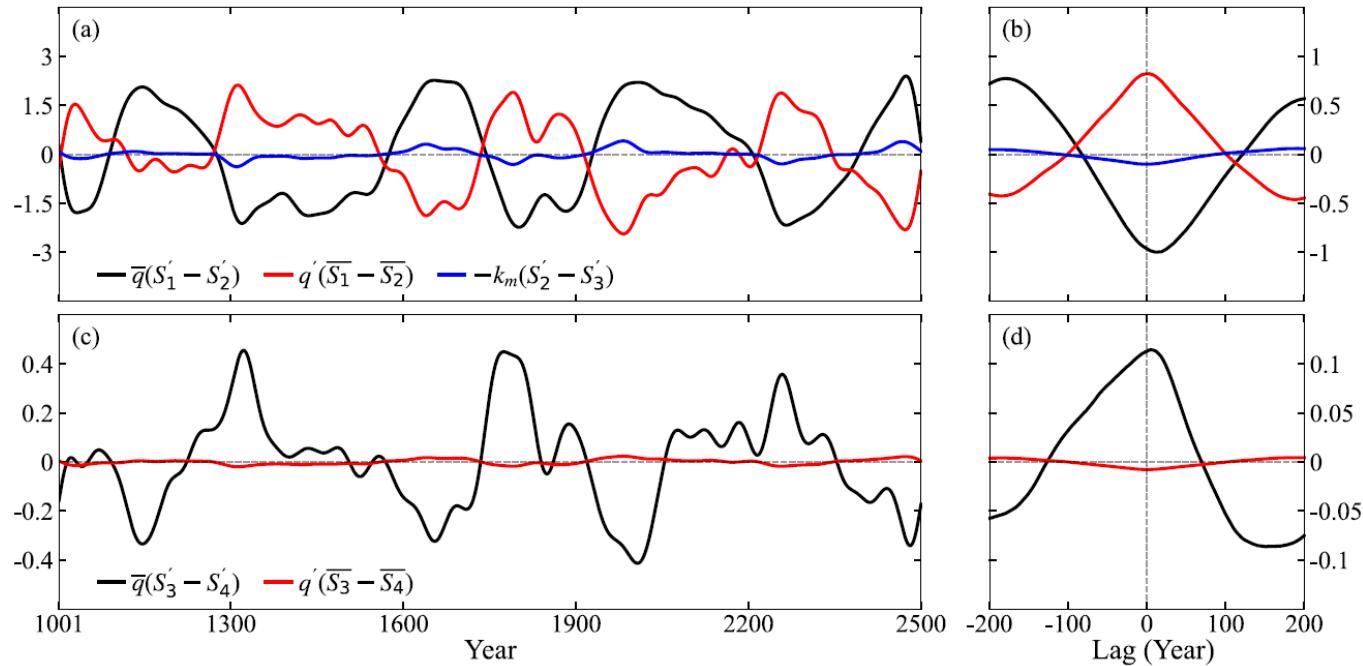
$$q'(S'_2) \sim \begin{cases} q'(\bar{S}_1 - \bar{S}_2) & \text{Local Term Positive Feedback} \\ \bar{q}(S'_1 - S'_2) & \text{Advection Term Negative Feedback} \\ -k_m(S'_2 - S'_3) & \text{Enhanced Mixing Negative Feedback} \end{cases}$$



Li and Yang (2022); Yang et al. (2022)

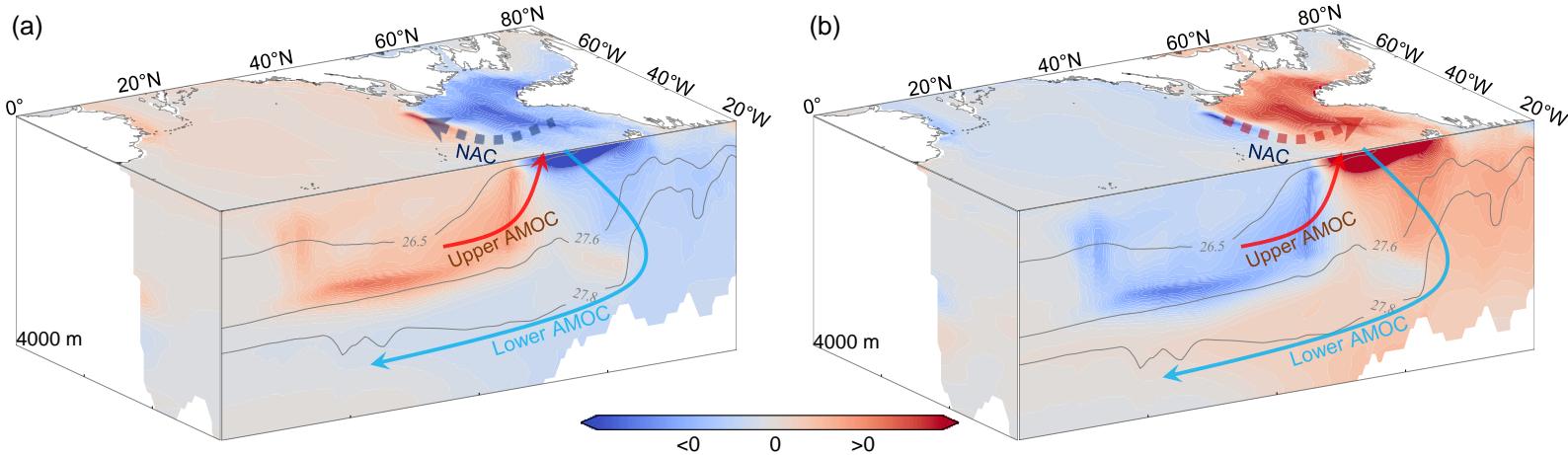
MCO in CESM1.0: 350 Years

Validated by theoretical model



A Schematic Diagram: MCO of AMOC in CESM1.0

Originated in the *North Atlantic*



Summary

<https://corp.fudan.edu.cn/>

- Eigen Mode: *Identified!*
- Physics: *Disclosed!*
- Self-sustained: *Realized!*
- Salinity change matters
- Advection-feedback process dominates

A 10-year journey to decipher the MCO

Li and Yang, 2022: A theory of self-sustained multicentennial oscillation of the AMOC. , *J. Climate*

Yang et al., 2023: A theory for self-sustained multicentennial oscillation of the AMOC. Part II: Role of Temperature. *J. Climate. In press*

Yang, K., H. Yang, Y. Li, and Q. Zhang, 2023: North Atlantic Ocean-originated multicentennial oscillation of the AMOC: a coupled model study. *J. Climate. Submitted.*



LaCOAS
北京大学气候与海-气实验室

Thanks