

Bjerknes补偿：海气耦合系统本征模

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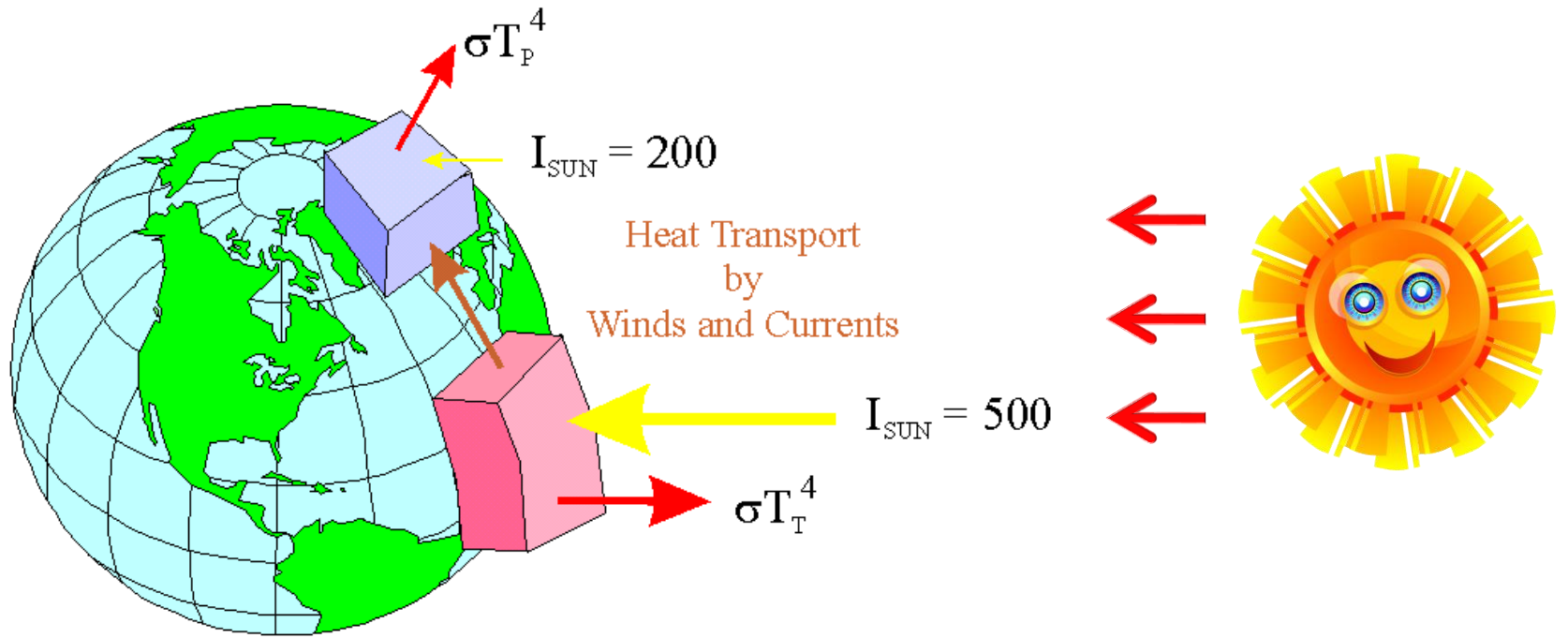
特别感谢：教授刘征宇、黄瑞新、刘秦玉等；博士李庆，王宇星、孙道勋等等



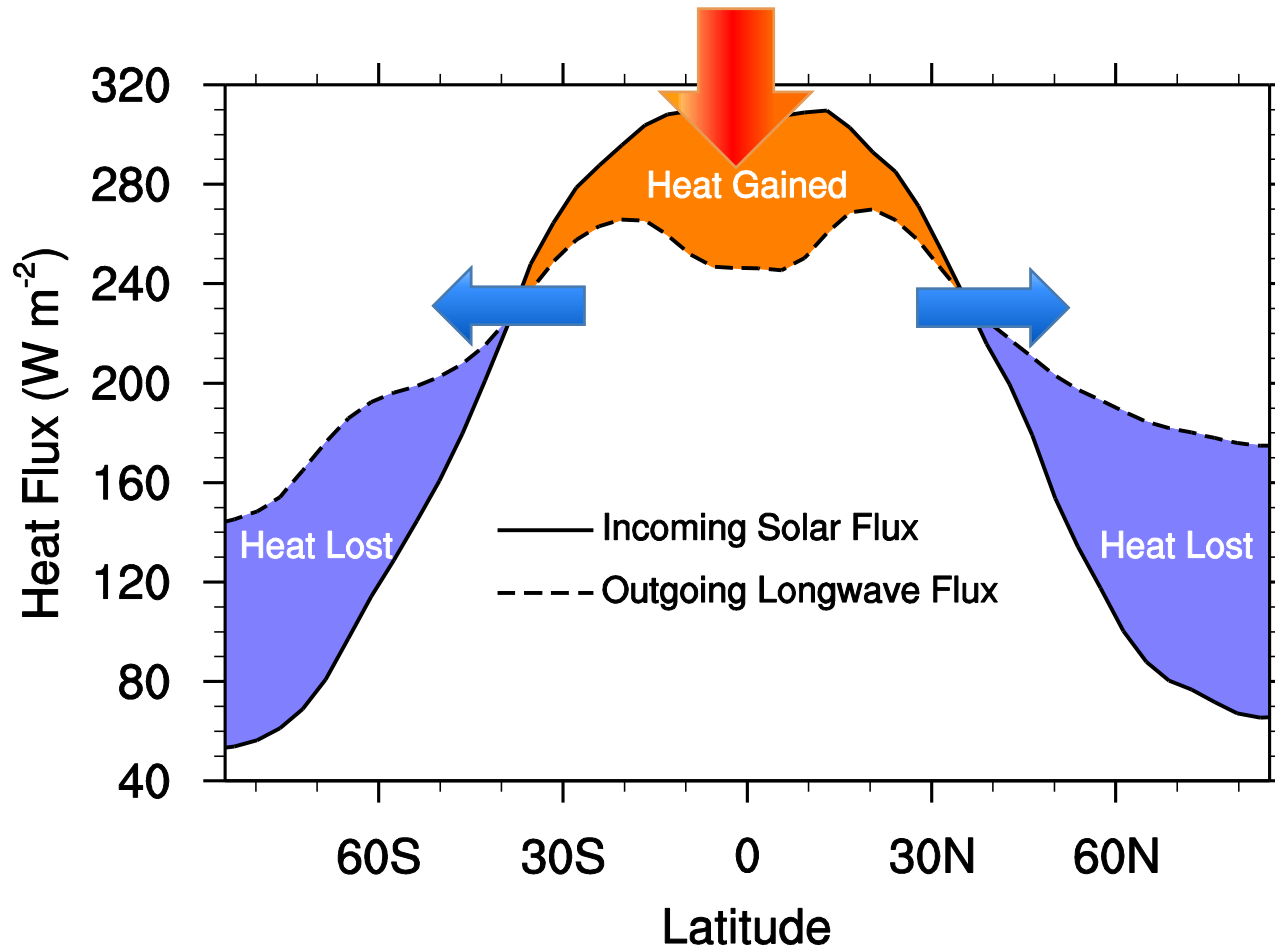
Outline

- **Fundamentals**
- **Questions**
- **Hypothesis and Theory**
- **CGCM results**
- **Aquaplanet**
- **Summary**

Fundamentals



Heat Budget at the TOA



Fundamental Questions

Energy

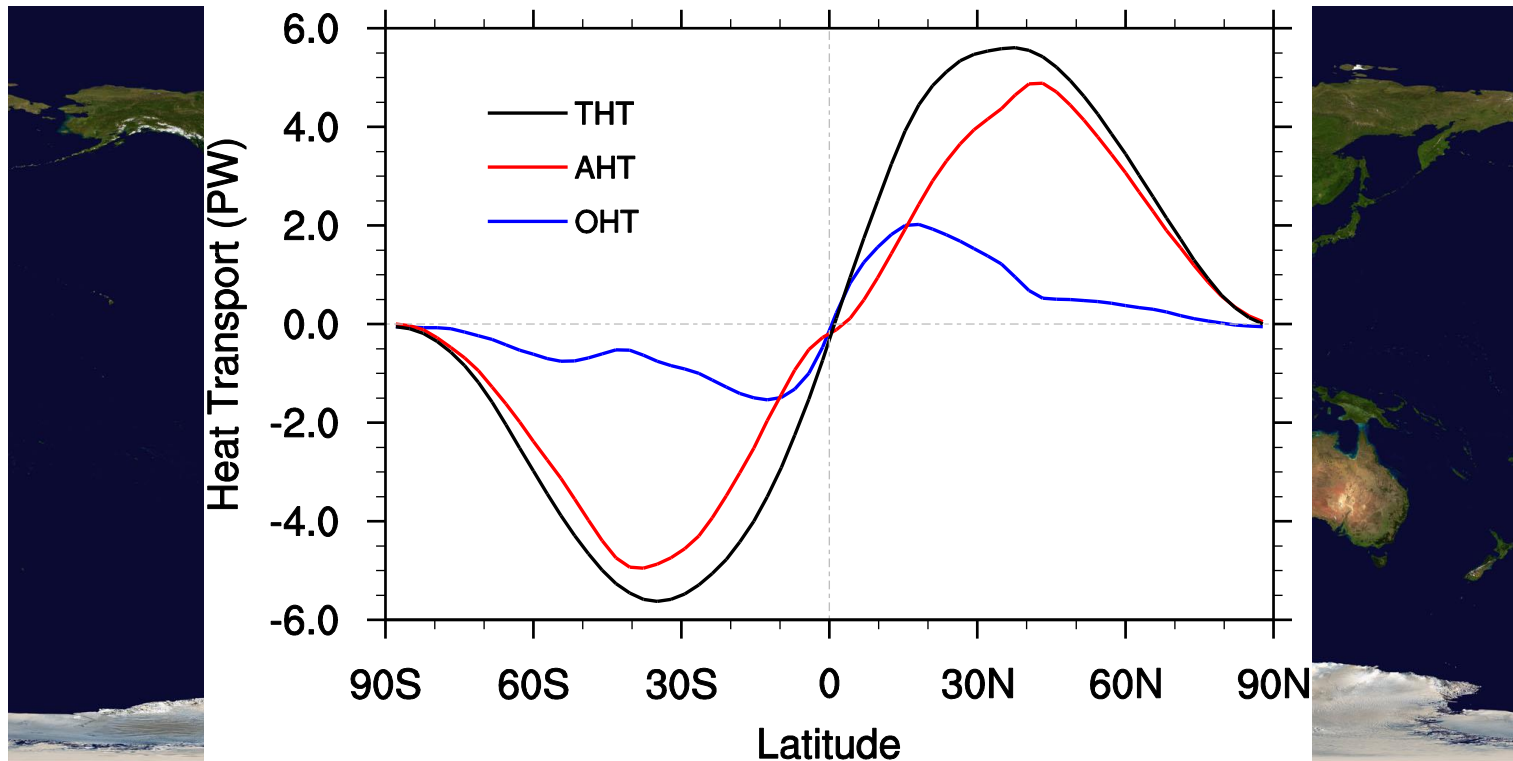
$$\text{Energy} = c_p T + L_v q + gz + \frac{(u^2 + v^2 + w^2)}{2}$$

- **Sensible Heat / Latent heat**
 - **Potential energy / Kinetic energy**
1. **Kinetic energy transport is small**
 2. **In the ocean only sensible heat transport**

Fundamental Questions

Fundamental Questions

1. Antisymmetric MHT?

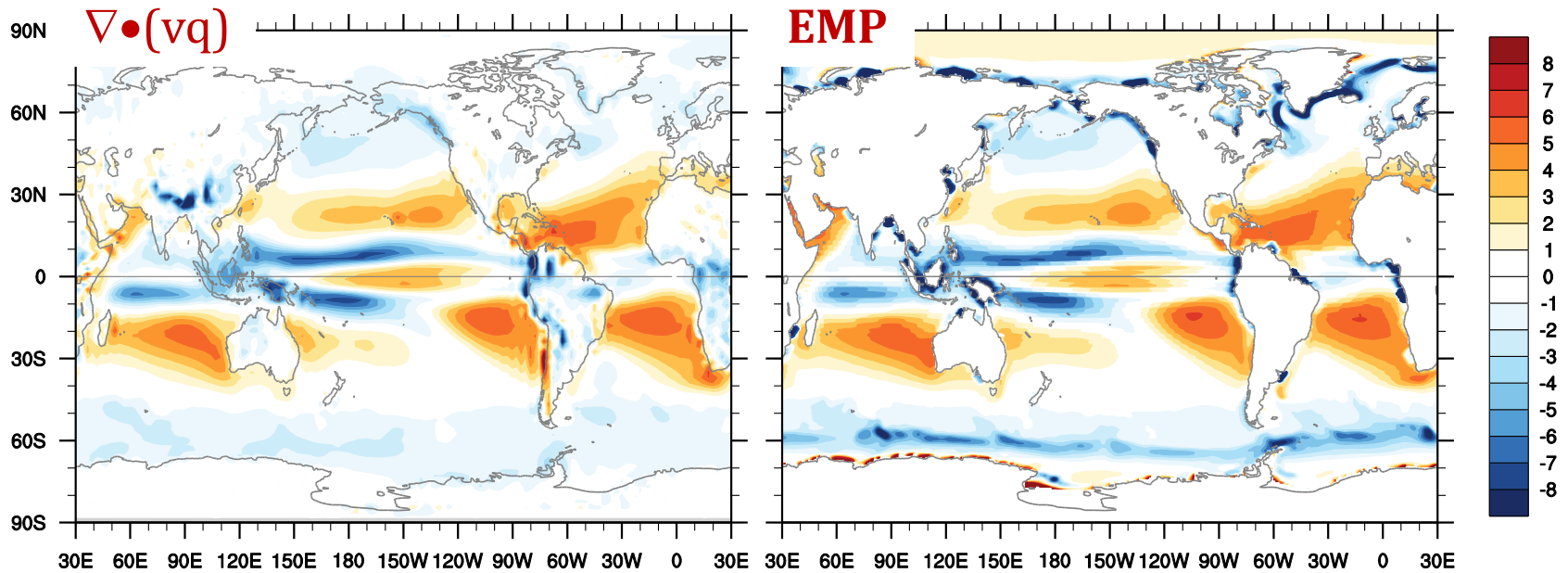


Aquaplanet → Real Earth

Trenberth and Caron (2001)

Fundamental Questions

2. “Real” Oceanic Contribution?

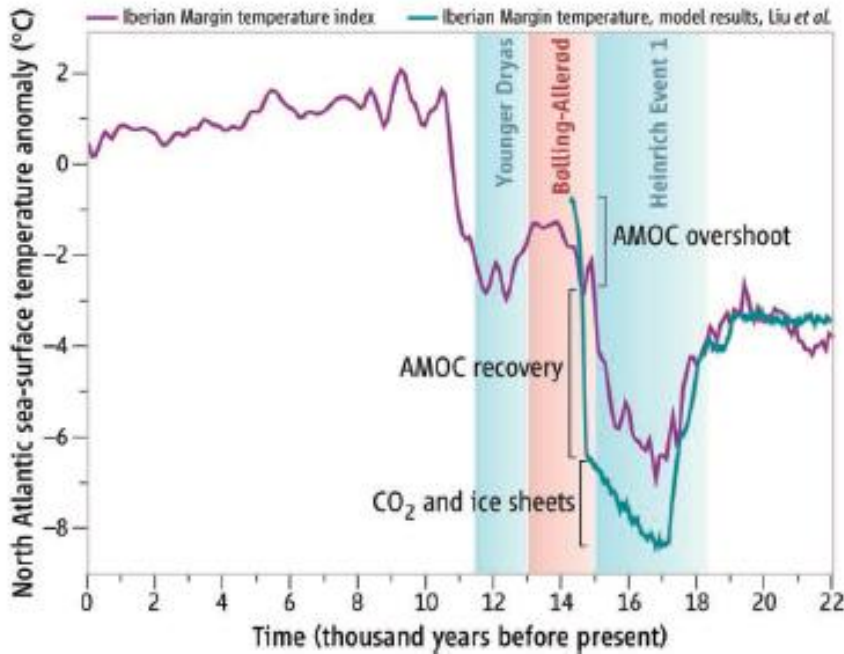


Yang and Li (2015)

Fundamental Questions

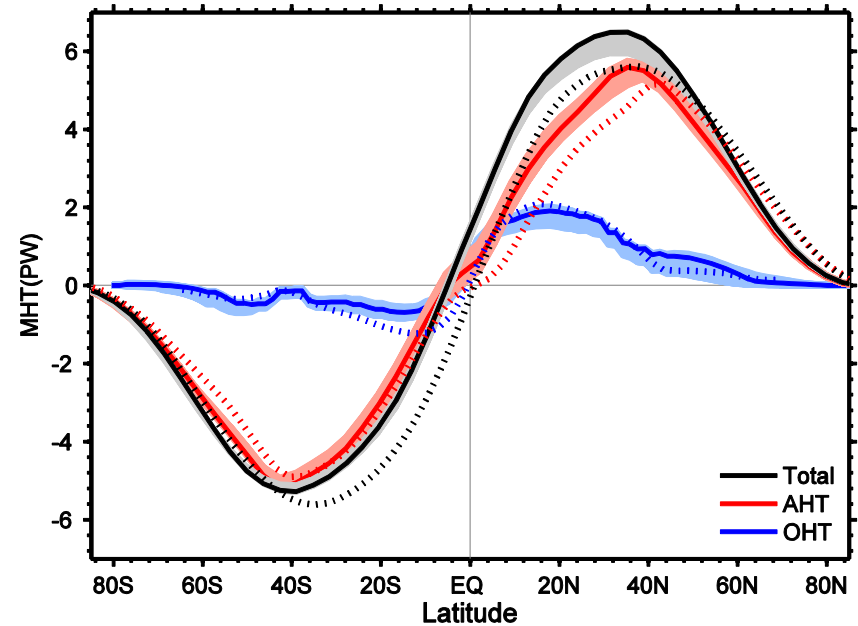
3. Relationship between OHT and AHT Changes?

Earth Climate Stability Mechanism



Climate Change during Past 22 kyr

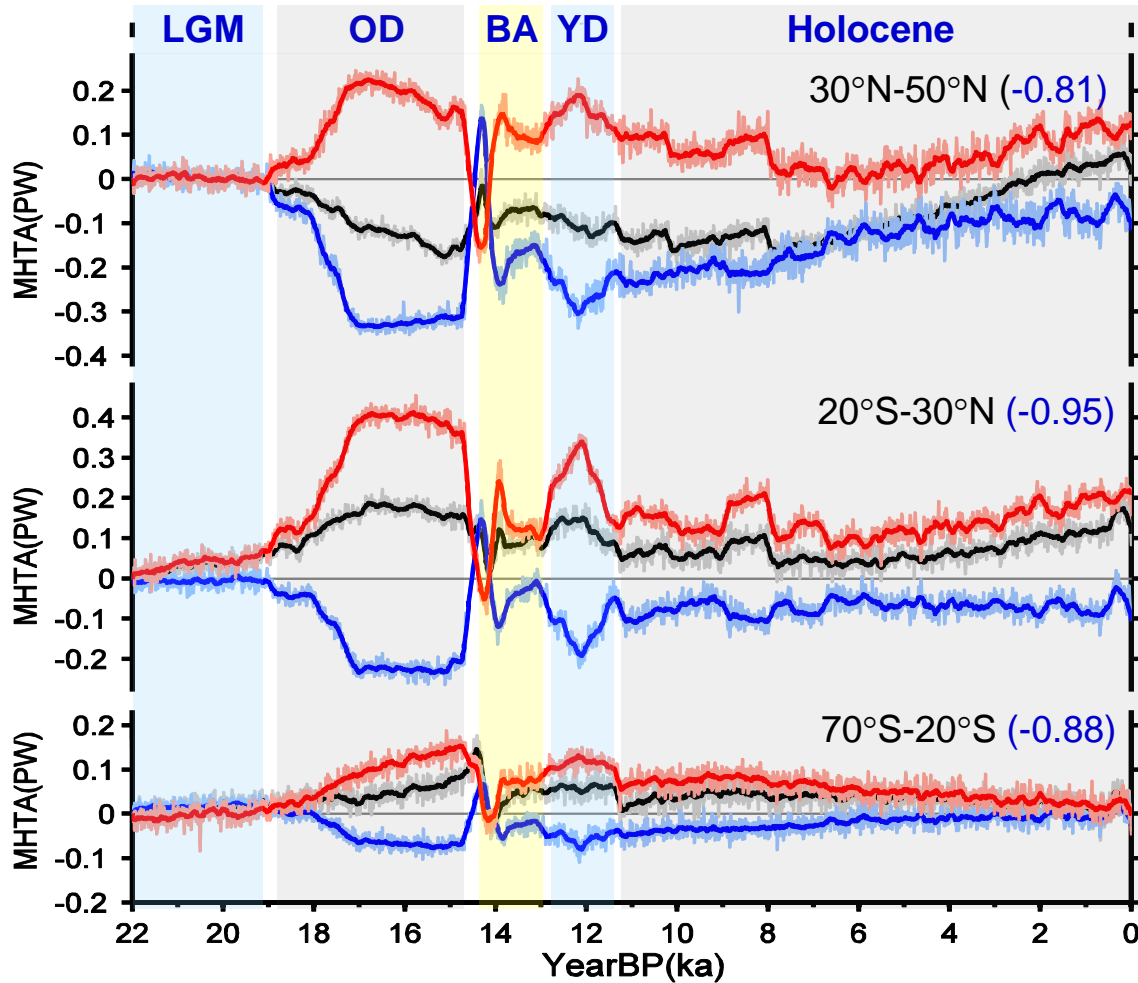
Timmermann (2009), Science



MHT from CCSM3 simulation TraCE-21K, From LGM to present

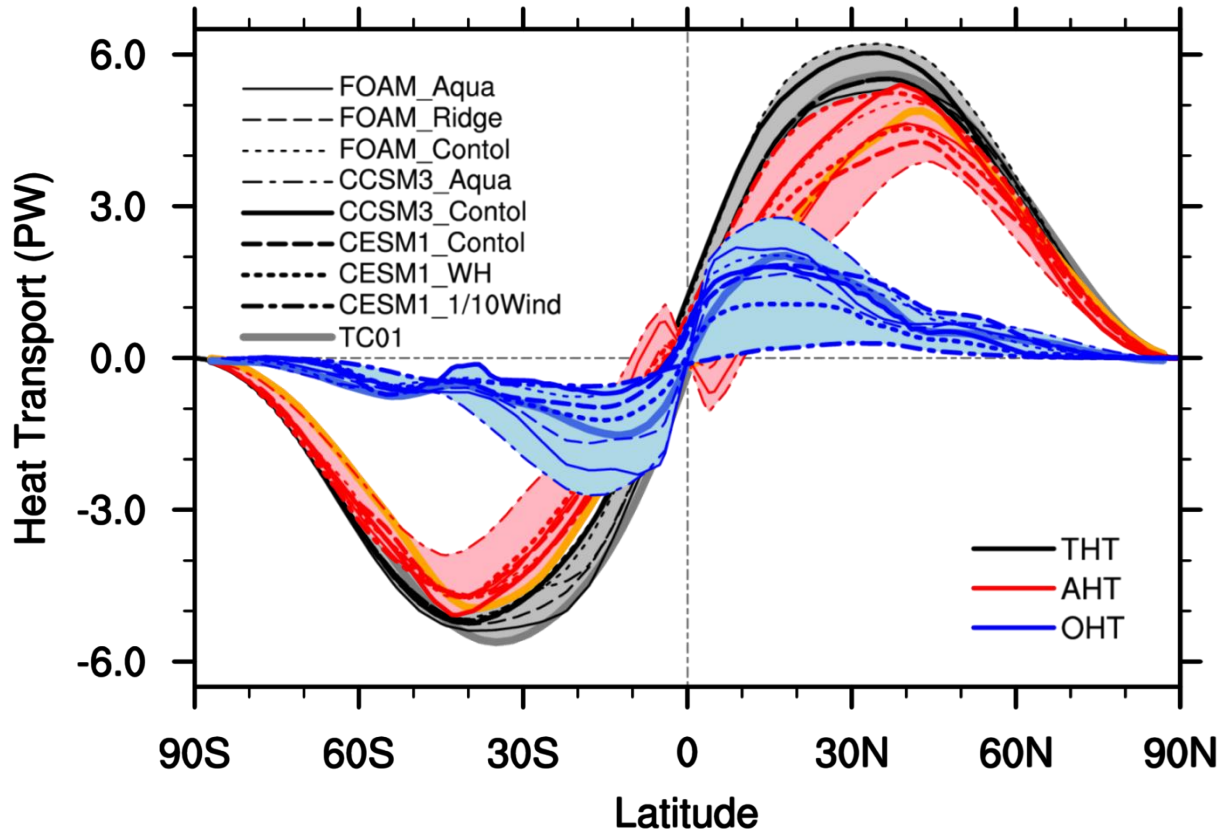
Liu et al. (2009); He (2011)

MHT Change Since LGM



Yang et al. (2015)

Compensation between AHT and OHT



Note: TC01 is from Trenberth and Caron (2001)

Hypothesis: Bjerknes Compensation

Jacob Aal Bonnevie Bjerknes
1897-1975

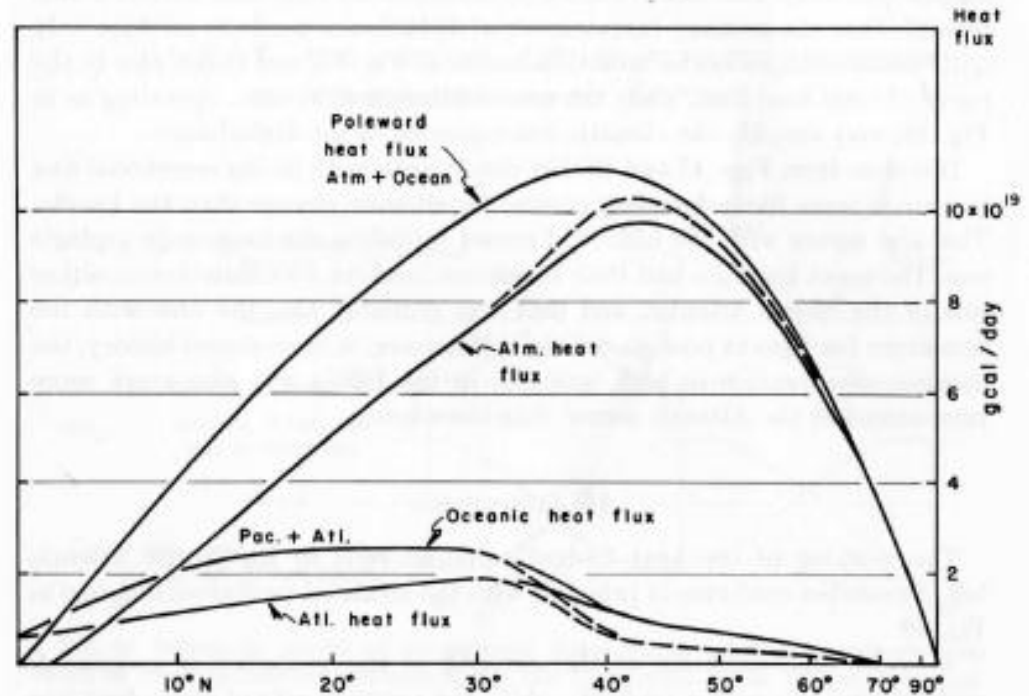
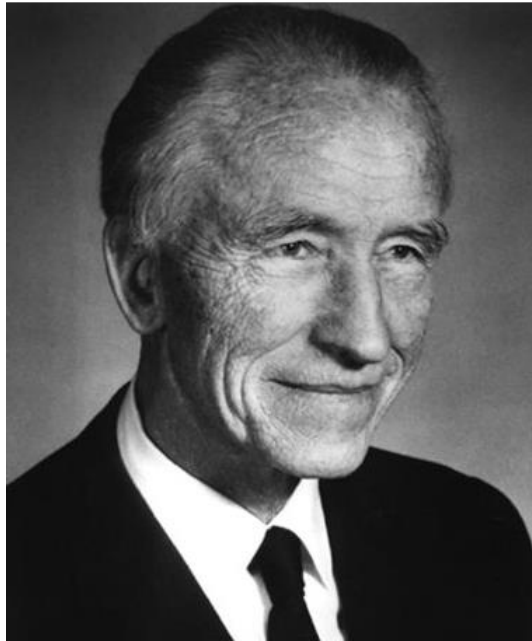
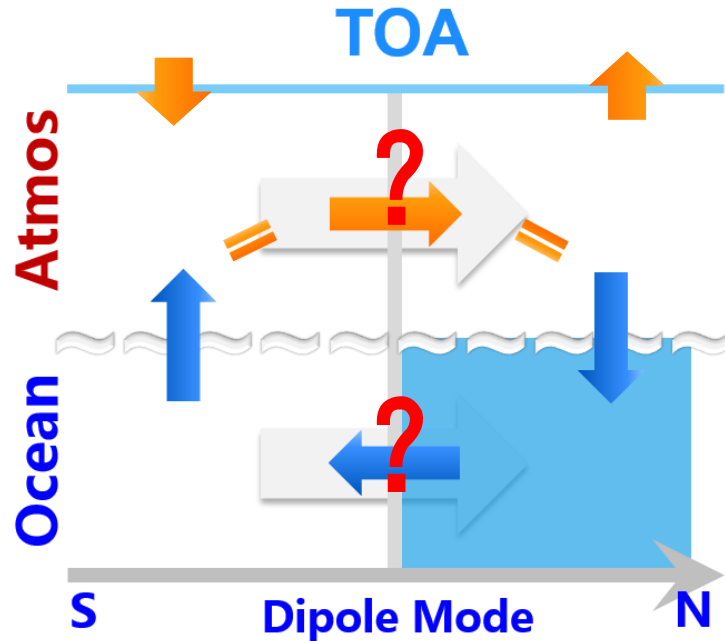


FIG. 48. Solid lines: flux data from Fig. 47 pertaining to present climatic conditions. Dashed lines refer to a sketchy model of the conditions around 1800 A.D. and show qualitative estimate of curtailed Atlantic and total oceanic heat flux as well as increased heat flux by low index atmospheric circulation. The anomalies of heat flux in oceans and atmosphere are assumed to cancel, leaving total heat flux and radiation budget unchanged. Actually, some change in the radiation budget is also likely to have taken place, but it could well have been quite small.

Bjerknes, 1964: Atlantic Air-Sea Interaction, *Advances in Geophysics*, Vol. 10, P77

Hypothesis: Bjerknes Compensation

Question: How Climate Feedback Determines BJC?



$$A + B = 0 \rightarrow A = -B$$

but $A + B + C = 0$

C: climate feedback

Then $A = -(B + C)$

Energy Conserved

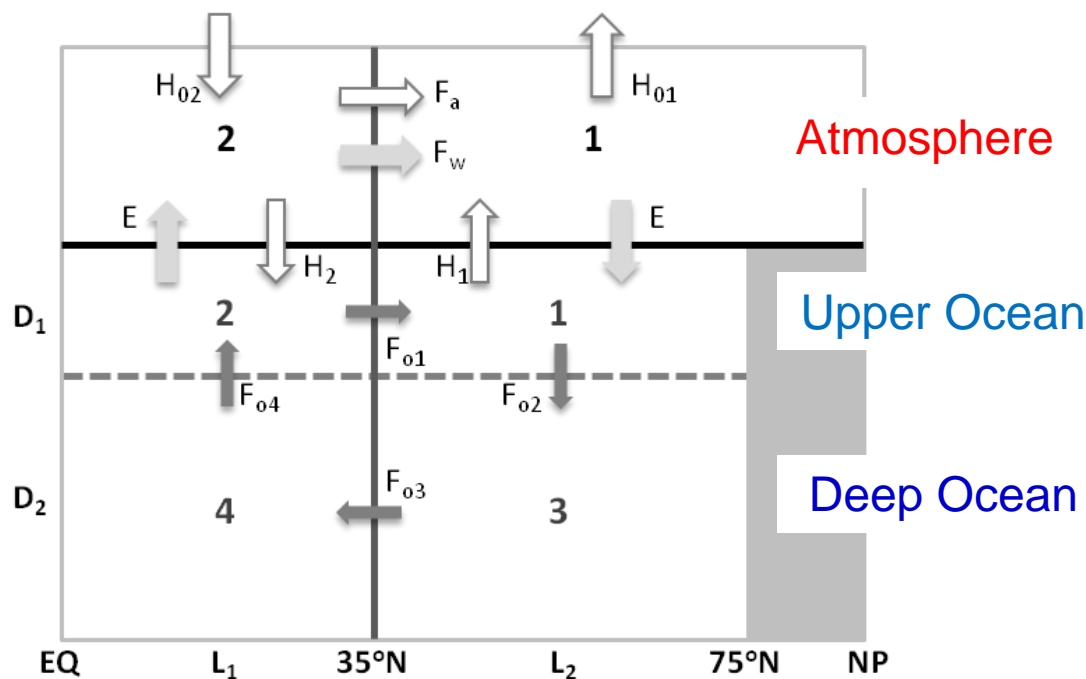
Theory for **Equilibrium** Change

1. **Coupled Multi-Box Model**
2. **1-D Energy Balance Model (EBM)**

Go to Final Equations

Coupled Multi-Box Model

Yang, Zhao and Liu, 2016: Understanding Bjerknes compensation in atmosphere and ocean heat transports using a coupled box model. *J. Climate*

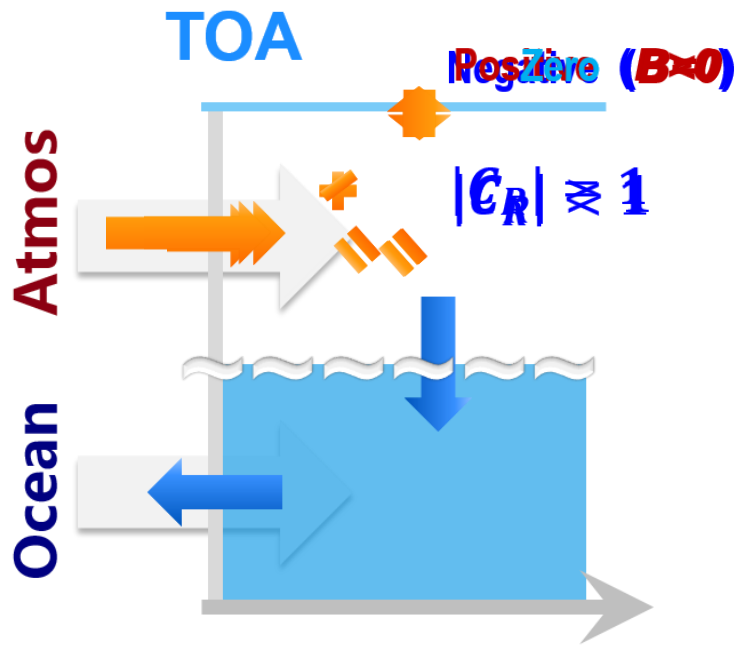


Stommel (1961); Nakamura et al. (1994); Marotzke and Stone (1995);
Tziperman et al. (1994); Tziperman and Ioannou (2002)

Go to Final Equations

Coupled Intrinsic Mode

Thermohaline-Climate Feedback-Energy Balance



$$C_R \equiv \frac{\Delta F_a}{\Delta F_o} = -\frac{1}{1-B} < 0$$

Local climate feedback $B(y)$

Yang, Zhao and Liu (2016)
Zhao, Yang and Liu (2016)

Climate Feedback + MHT → Earth Energy Balance

Coupled Intrinsic Mode

能量补偿 \Leftrightarrow 体重保持

饮食
(海洋)

新陈代谢
(气候反馈)

运动
(大气)



$$C_R = -\frac{1}{1-B}$$

Go to BJC for Climate Variability

Theory for **Transient** Climate Variability

$$\begin{aligned}\dot{T}_s &= \frac{1}{\epsilon c \rho_0 D_1} [(A_2 - A_1 - B T_s) - 2\chi T_s] - 2q T_s, \\ \dot{S}_s &= \frac{2S_0}{\epsilon_w D_1} \gamma T_s - 2q S_s + h_{fw}.\end{aligned}$$



Linearization: $T = \bar{T} + T'$ and $S = \bar{S} + S'$

$$\frac{\partial}{\partial t} \begin{pmatrix} T'_s \\ S'_s \end{pmatrix} = M \begin{pmatrix} T'_s \\ S'_s \end{pmatrix} + \begin{pmatrix} 0 \\ h_0 e^{i\omega t} \end{pmatrix}$$

If $h_{fw} = \text{const.} \rightarrow C_{R0} = -\frac{1}{1+B/2\chi} \quad (2)$

BJC for Climate Variability

Zhao, Yang and Liu, 2016: Assessing Bjerknes compensation for climate variability and its timescale dependence. *J. Climate*

$$C_{Rp} \equiv \frac{F'_a}{F'_o} = \text{Re}(C_{R0}e^{i\delta}) = r_\delta * C_{R\omega}$$

$$r_\delta \equiv \cos\delta = -\frac{F}{\sqrt{\omega^2 + F^2}}$$

$$C_{R\omega} = \frac{2\chi}{\epsilon c \rho_0 D_1 \sqrt{\omega^2 + F^2}}$$

=

$$C_R \equiv r \frac{\sigma_{F_a}}{\sigma_{F_o}}$$



$\omega \rightarrow 0$



$$C_{R0} = -\frac{1}{1 + B/2\chi}$$

BJC for Climate Variability

$$\omega \rightarrow \infty \Rightarrow r_{\delta} \rightarrow \mathbf{0}; C_{R0} \rightarrow \mathbf{0}; C_{Rp} \rightarrow \mathbf{0}$$

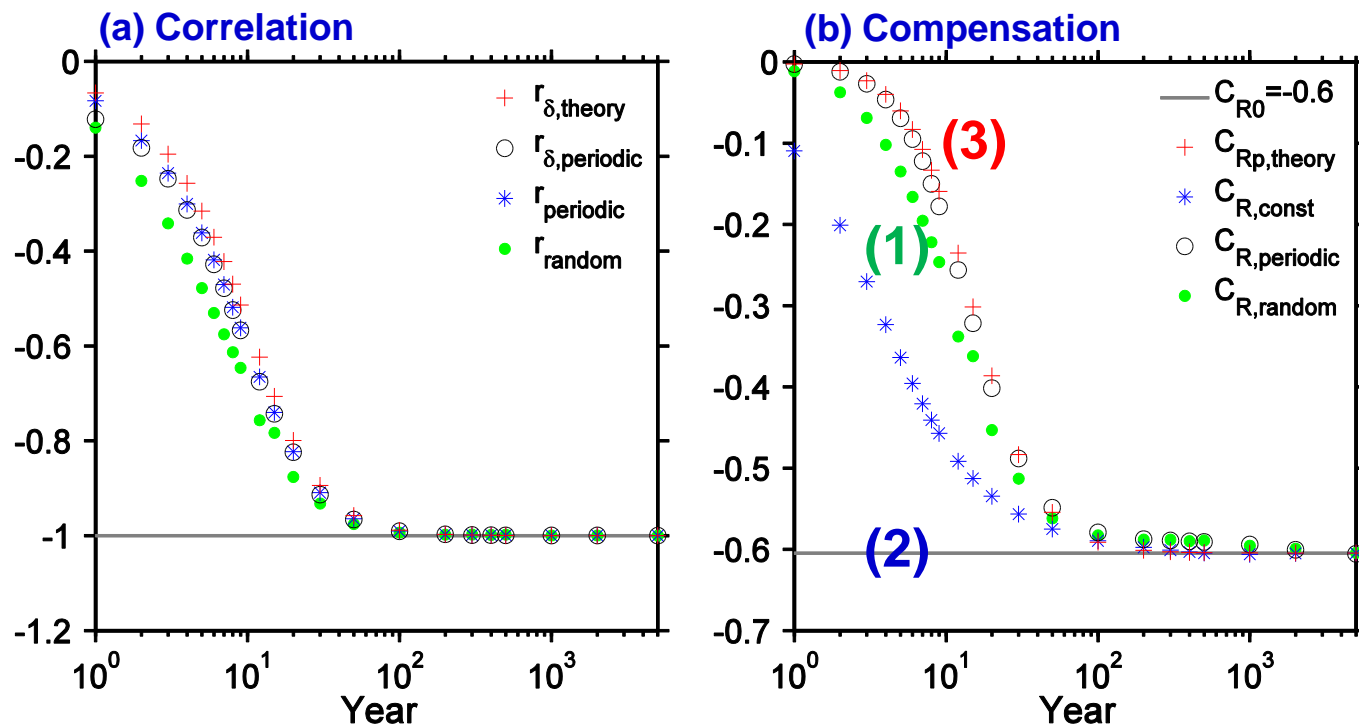
No correlation and No BJC

$$\omega \rightarrow \mathbf{0} \Rightarrow r_{\delta} \rightarrow \mathbf{-1}; C_R(\mathbf{1}) \approx C_{R0}(\mathbf{2}) \approx C_{Rp}(\mathbf{3})$$

Full correlation and equilibrium BJC

[Go to Climate Variability Validation](#)

BJC Theory **Valid** for Climate Variability



Beyond *decadal* timescale, AHT and OHT out of phase, BJC established

Outline

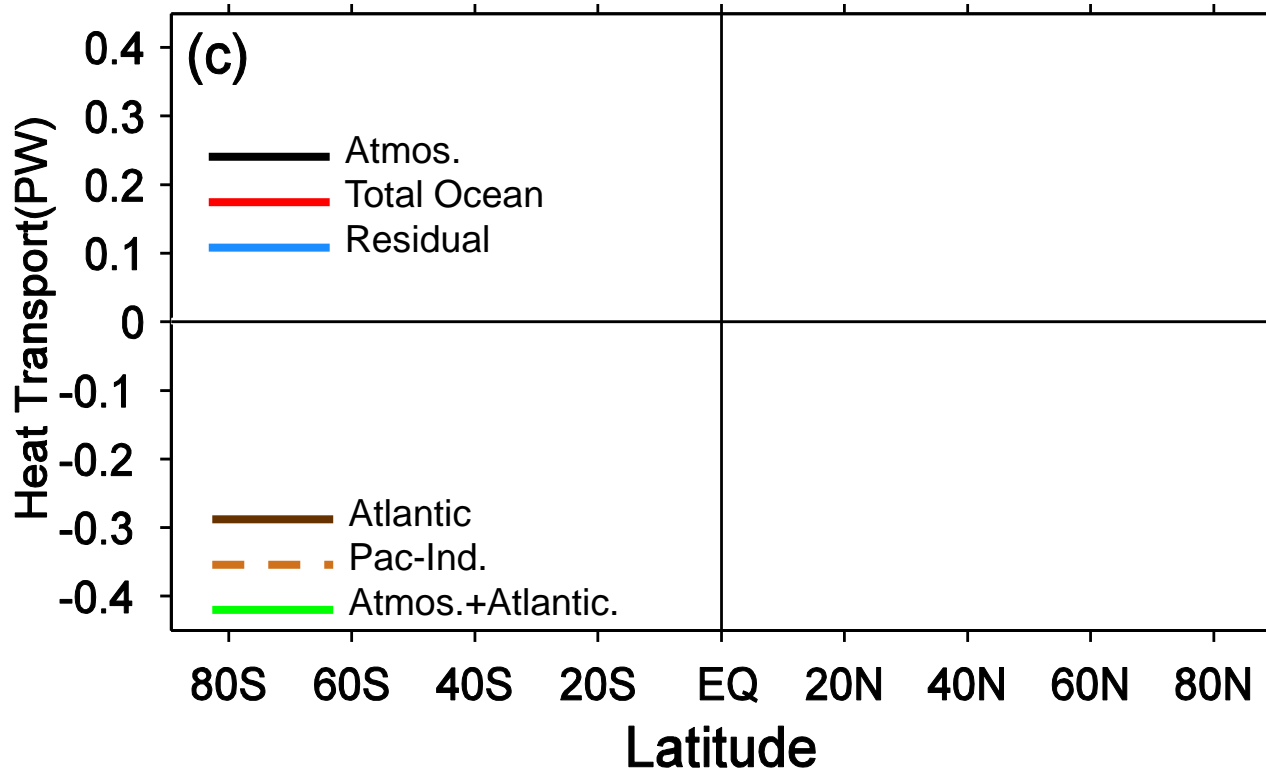
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CESM Experiment and Mechanism

- ◇ **Fresh-water experiments**
- ◇ **Wind-perturbation experiments**
- ◇ **Global warming experiments**
- ◇ **Internal variability from a long control run**

Yang and Dai (2015), Yang et al. (2013, 2016, 2017)

BJC under **Freshwater** in CESM

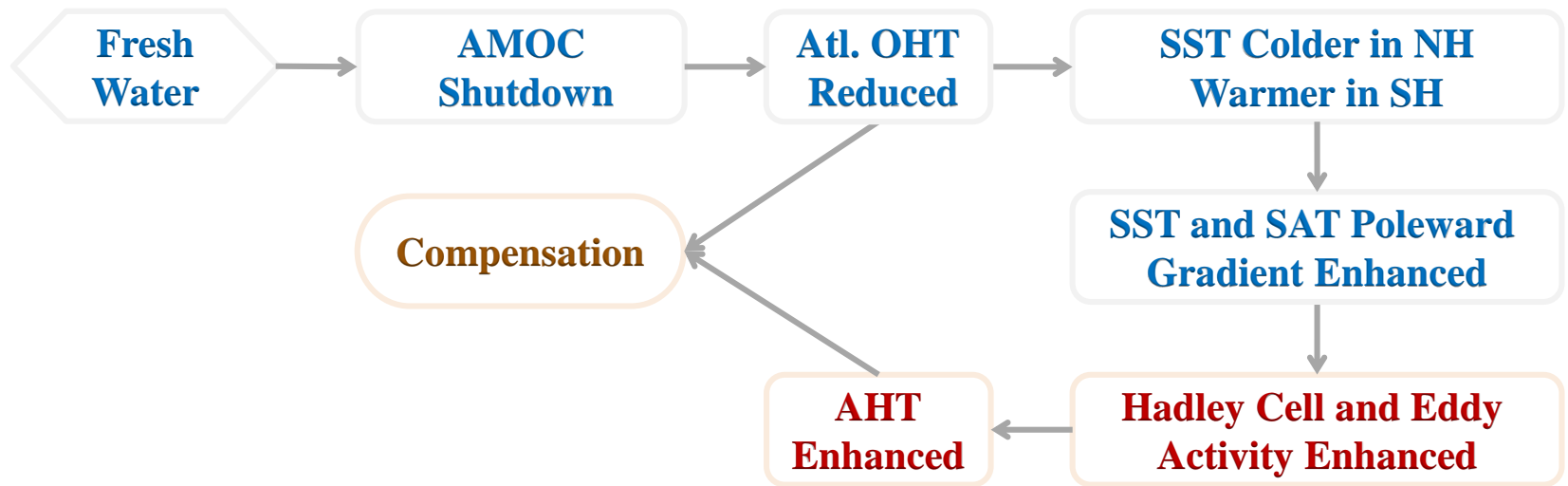


80-90%

Atlantic OHT ↓ ⇒ AHT ↑ ⇒ Pac-Ind. OHT ↑

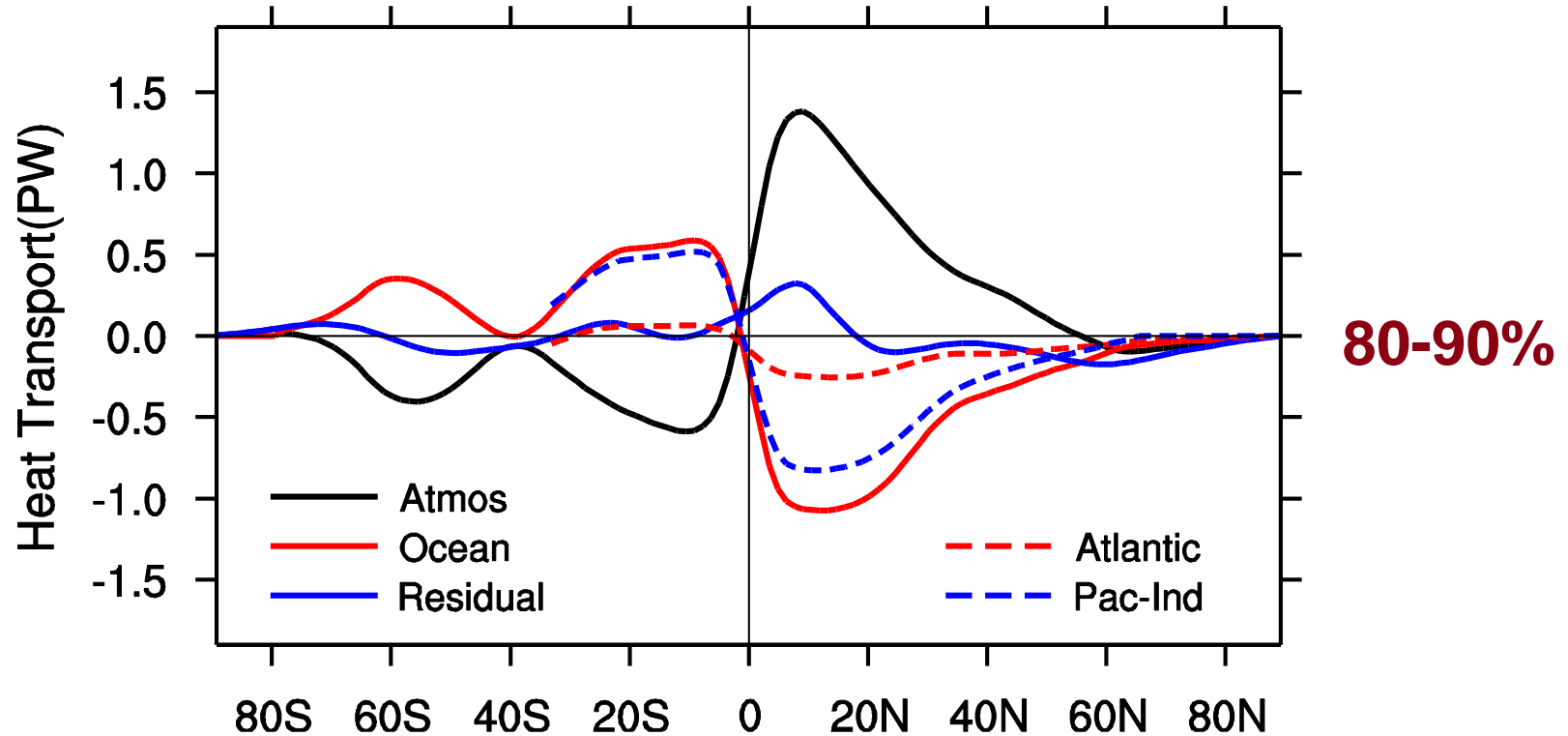
Atlantic OHT ≈ AHT; Pac-Ind. OHT ≈ Overcompensation

“Mechanism”



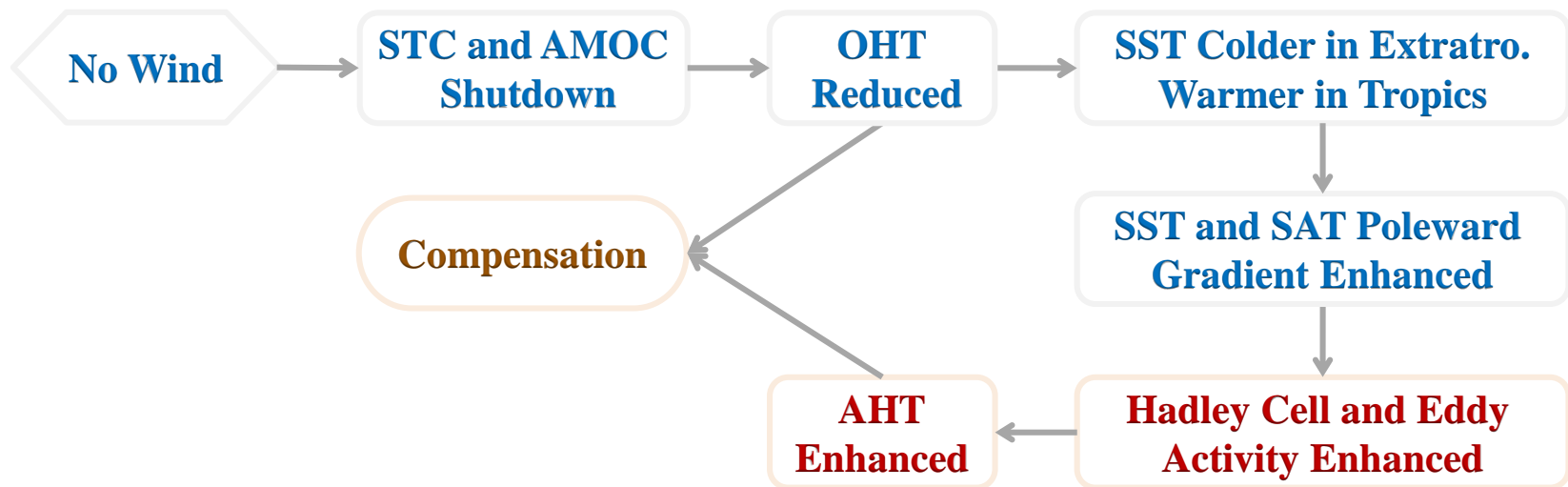
Yang et al. (2013, 2017)

BJC under Wind Perturbation in CESM



Pacific-Indian OHT ↓ ⇒ Ty ↑ ⇒ HC ↑ ⇒ AHT ↑
Nearly Compensation

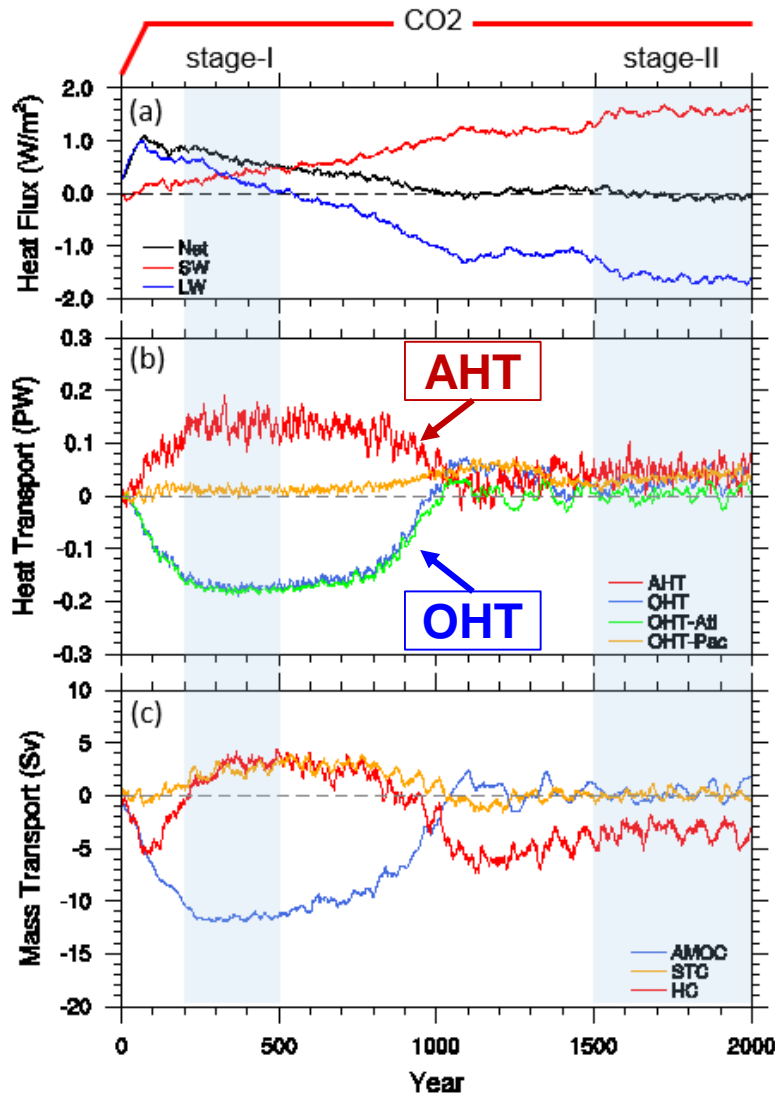
“Mechanism”



Yang and Dai (2015), Dai et al. (2017)

BJC under Global Warming in CESM

85%



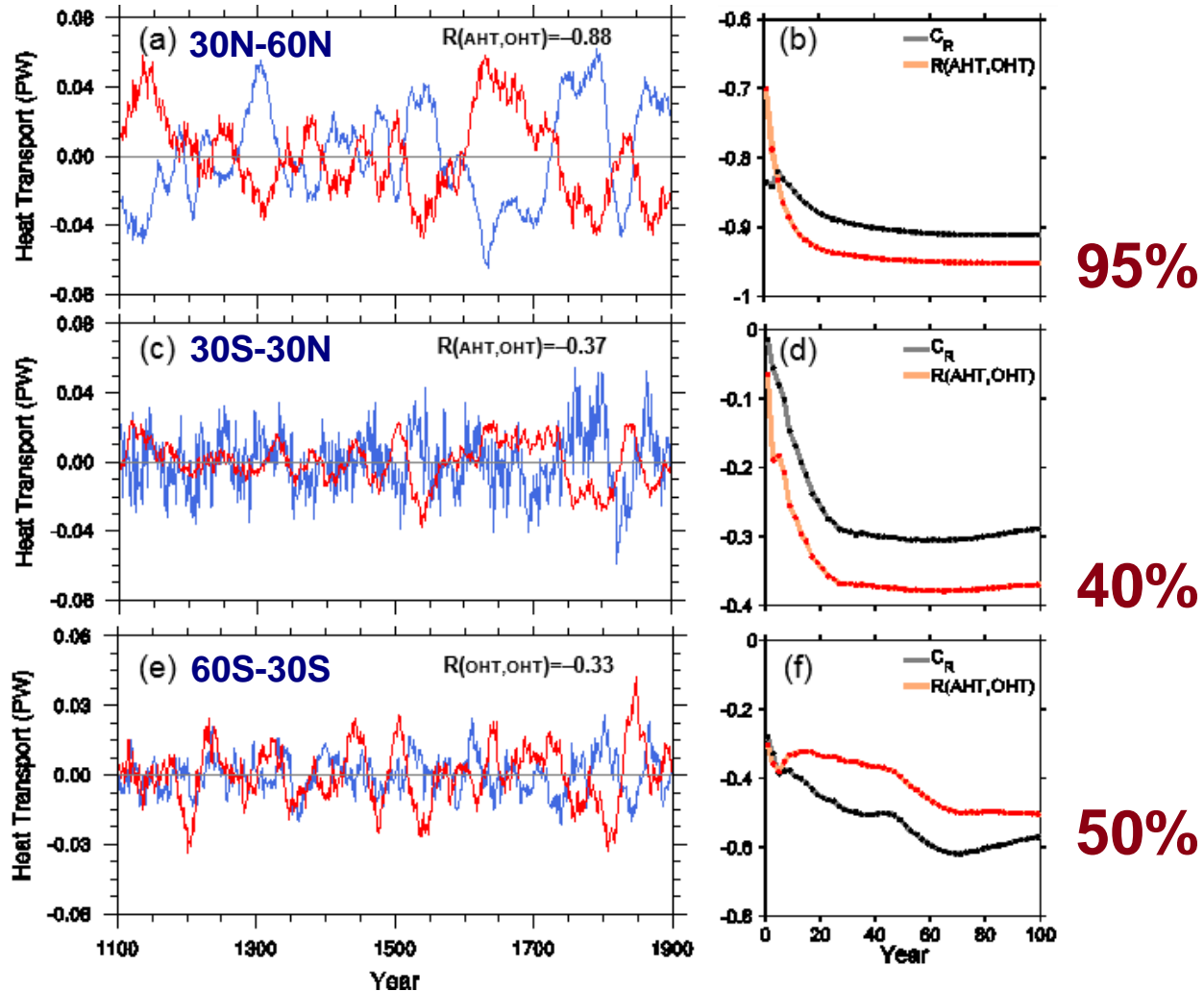
Under 2 X CO2 forcing
BJC valid due to
thermohaline dynamics!

Yang et al. (2017)



BJC in Natural Variability in CESM

2000-year CESM control run

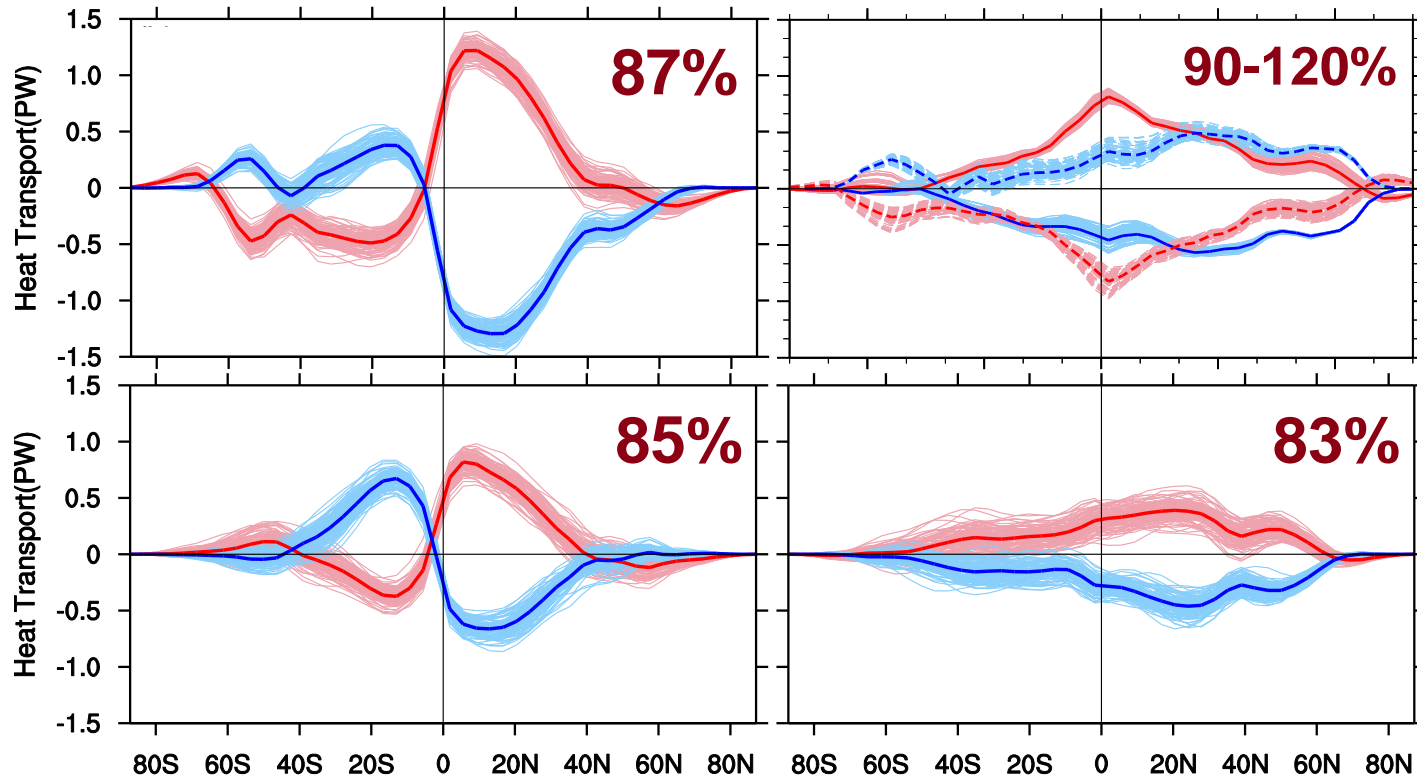


Zhao and Yang (2017)

第四届青年科学家论坛, 2017.10.26-27, 杭州

Summary: BJC in CESM

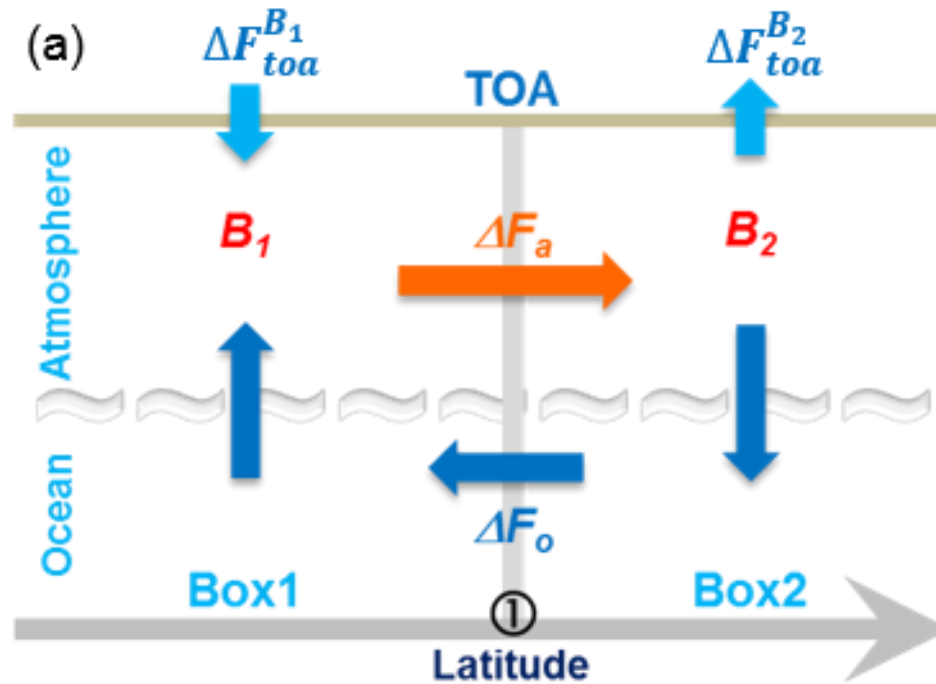
Surface Reason: *Out-of-phase* changes in Atmos-Ocean MOC → BJC



Yang and Dai (2015), Yang et al. (2013, 2016, 2017)

BJC Mechanism

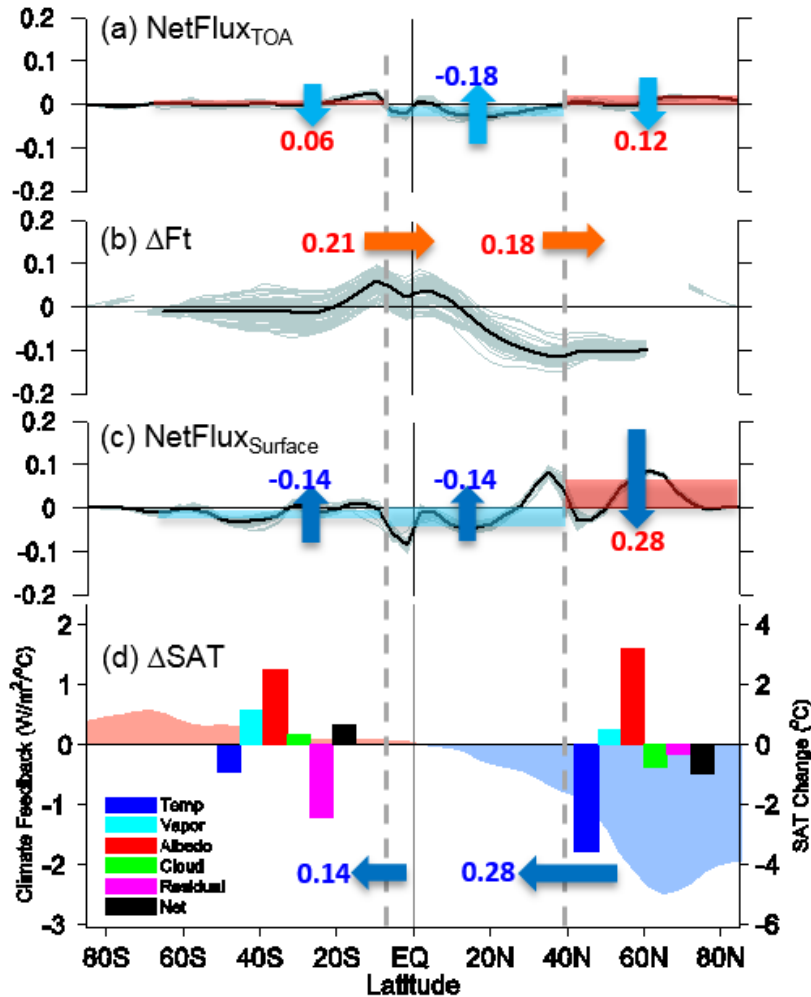
Fundamental Reason: Climate feedback + Energy constrain → BJC



$$C_R = -(B_1 + B_2)\chi / [B_1 B_2 + (B_1 + B_2)\chi]$$

BJC: *Theory* vs *CGCM*

CESM Wind Perturbation experiments



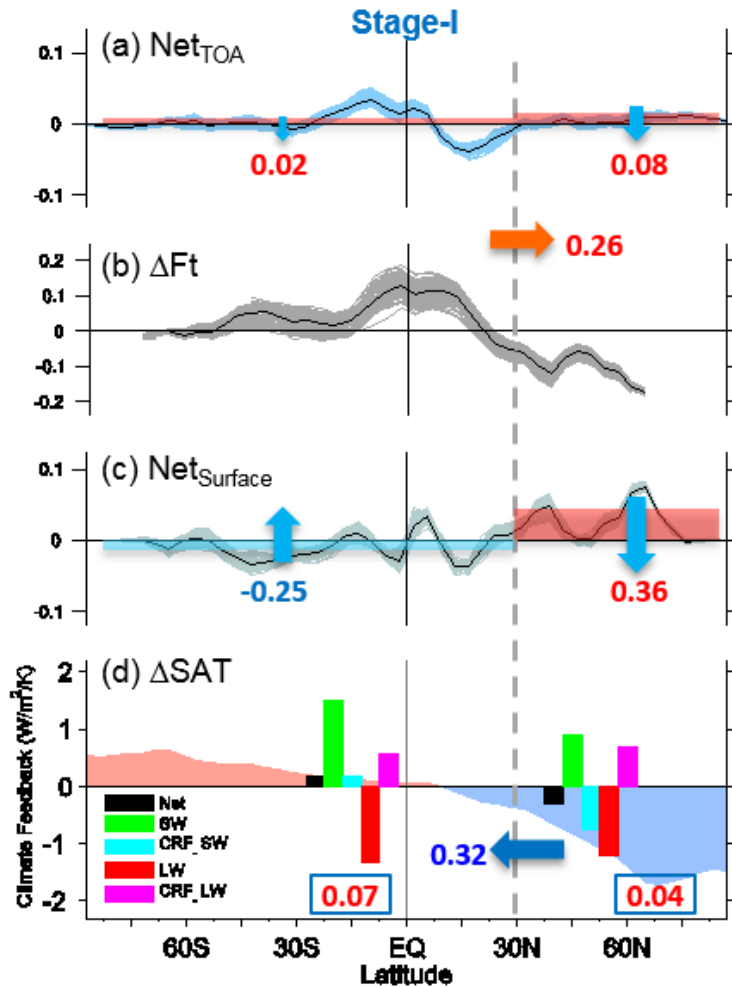
	Wind	Temp	Albedo	Cloud	C_{Rmodel}	$C_{Rtheory}$
0.1A	NH	-1.80	1.30	-0.23	-1.10	-1.09
	SH	-0.44	1.16	-0.07		
	Global	-2.20	1.34	-0.28	-0.83	-0.71
0.1P	NH	-1.87	1.30	0.34	-1.85	-1.61
	SH	-2.14	0.39	0.57		
	Global	-1.88	0.95	0.27	-0.85	-0.77
0.1G	NH	-1.84	1.05	-0.08	-0.95	-0.91
	SH	-1.70	1.96	-0.29		
	Global	-1.77	1.51	-0.18	-0.87	-0.81

$$C_{Rmodel} \approx C_{Rtheory}$$

Dai et al. (2017)

BJC: *Theory* vs *CGCM*

CESM Freshwater experiments



Freshwater		Global	SH	NH	90°S-30°N	30°N-90°N
Stage-I	Net CF	-0.63	0.89	0.08	0.18	-0.30
	C_{Rmodel}	-0.97	-1.36		-0.88	
	$C_{Rtheory}$	-0.83	-1.05		-1.43	
Stage-II	Net CF	1.96	0.66	0.35	0.16	-0.28
	C_{Rmodel}	-1.11	-1.90		-0.90	
	$C_{Rtheory}$	-2.88	-1.18		-1.33	

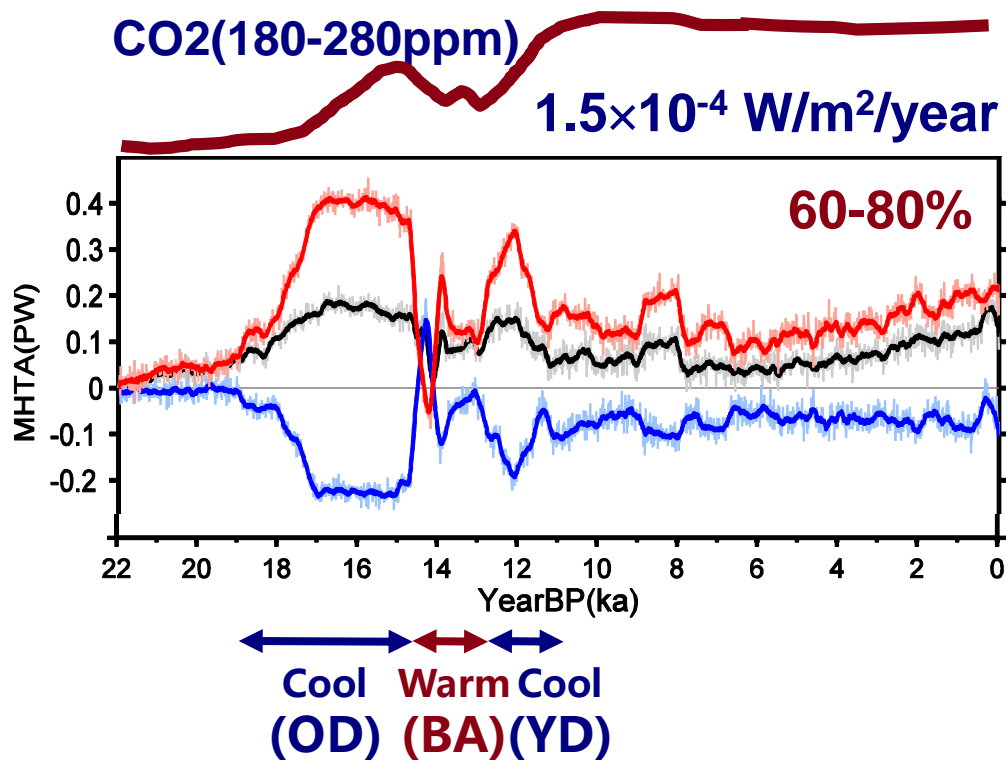
$$C_{Rmodel} \approx C_{Rtheory}$$

Yang et al. (2017)

BJC: Coupled *Intrinsic* Mode

3. Relationship between OHT and AHT Changes? **Answered!**

All-in-One Simulation since LGM



BJC helps to maintain overall Earth climate stability

Yang et al. (2015), Sci. Rep.

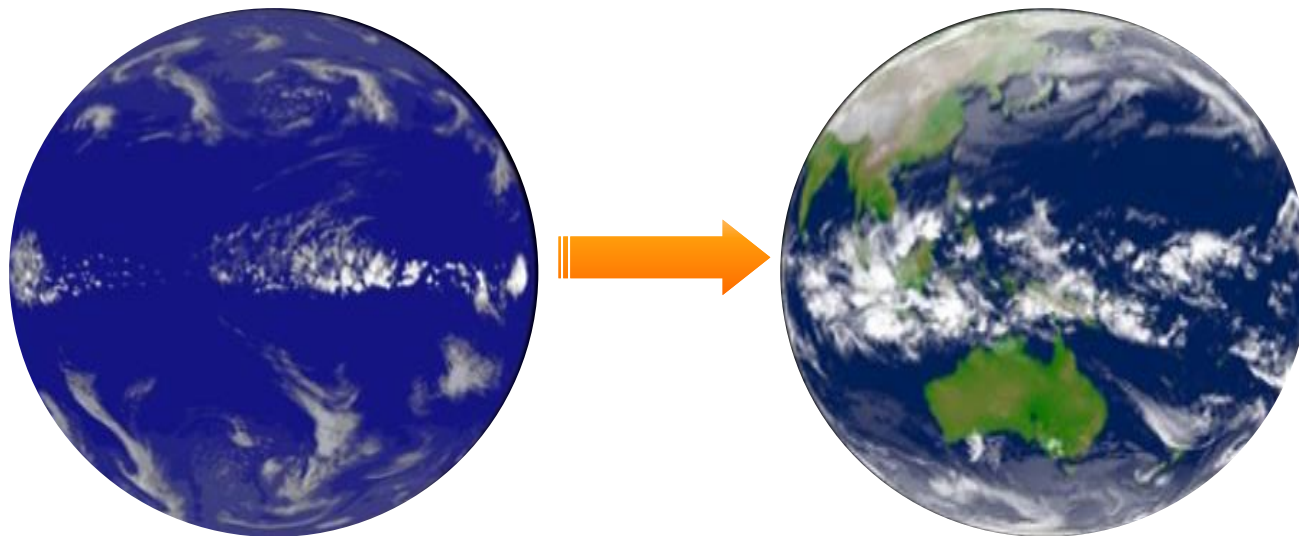
第四届青年科学家论坛, 2017.10.26-27, 杭州

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Aquaplanet → Real Earth

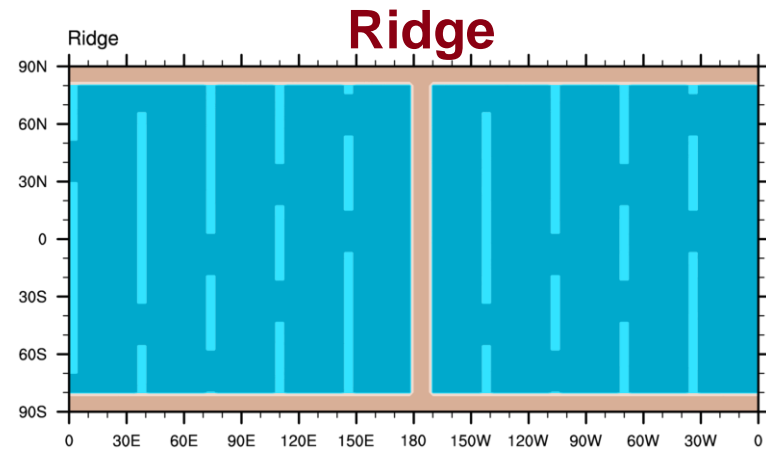
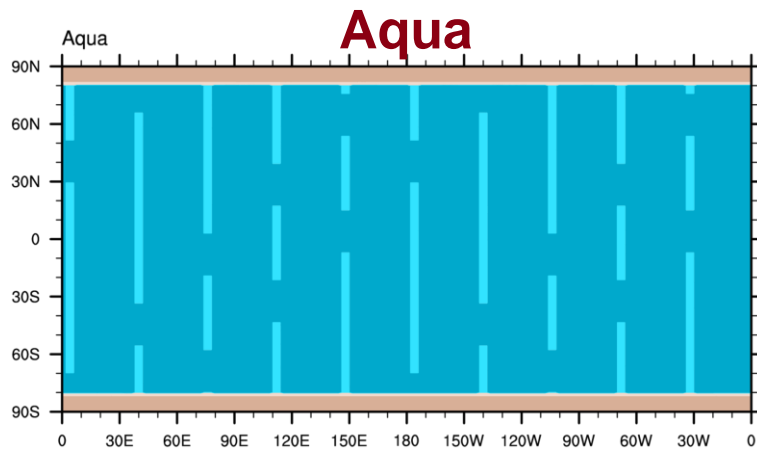
Why anti-symmetric MHT?



Try to answer this fundamental question

Topo for Aqua and Ridge

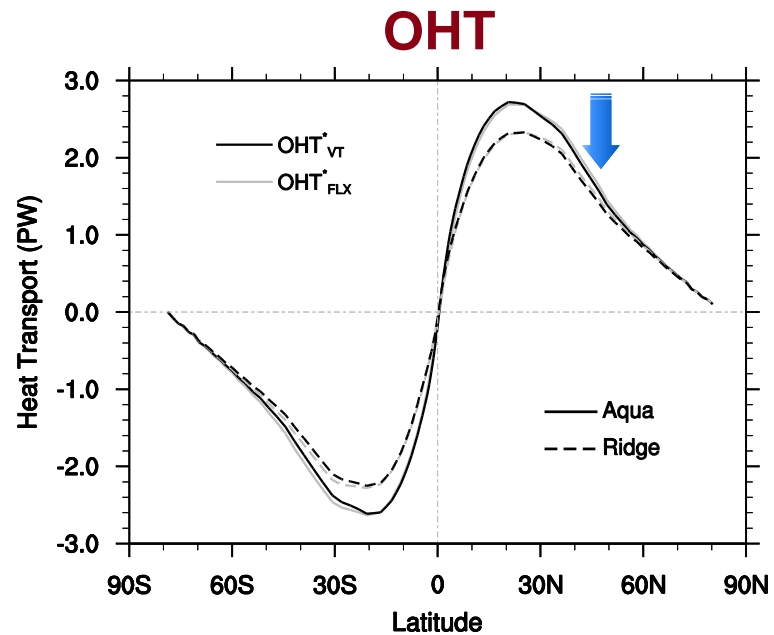
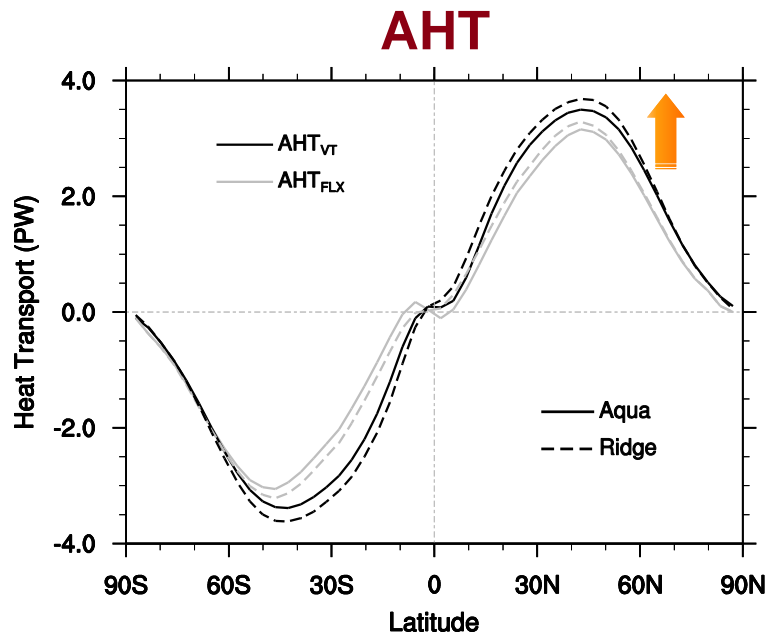
Land: 10 m; Ocean: 5000 m; Bottom random ridge: 500 m



Li and Yang (2018)

[Go to Summary](#)

Symmetric AHT and OHT

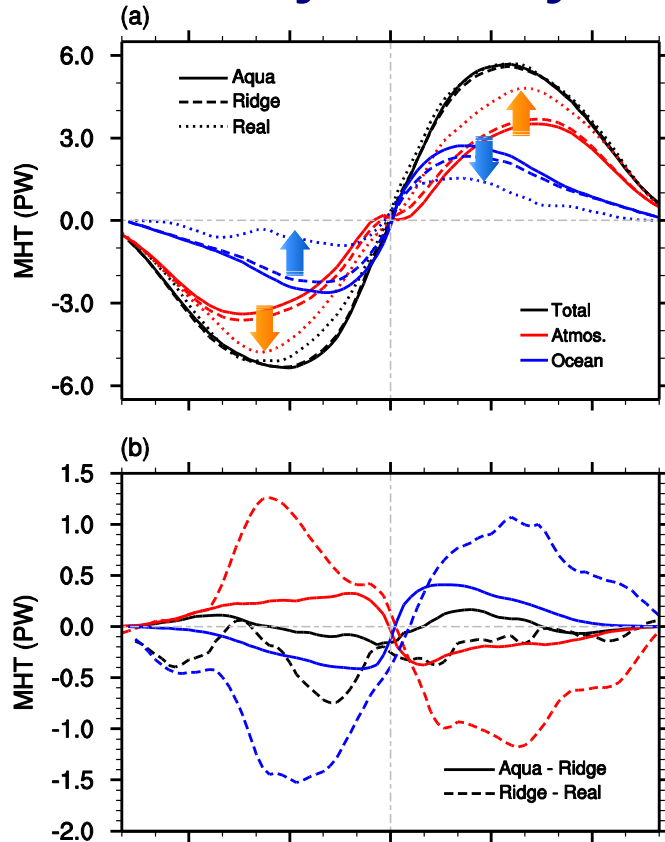


From *Aqua* to *Ridge* → OHT ↓ and AHT ↑

Bjerknes Compensation

Aquaplanet → Real Earth

Why anti-symmetric MHT? Answered



From *Aqua* to *Real*

1. OHT ↓ and AHT ↑
2. OHT → asymmetric, NH>SH, AMOC + Weaker baroclinic
3. AHT → asymmetric, SH>NH, Stronger baroclinic dT/dy ↑

→ Total MHT *unchanged*

BJC maintains antisymmetric MHT!

Summary and Discussion

- ◇ **Bjerknes compensation**
 - ◇ Intrinsic mode
 - ◇ Atmospheric physics ↔ Physical oceanography
 - ◆ Climate feedback ↔ Thermohaline circulation
- ◇ **Self-constraint mechanism**
 - ◇ Climate didn't drift too much
- ◇ **If feedback → Reversibility of climate**
 - ◇ Invisible hand (?)



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北京大学气候与海-气实验室

谢谢