

# Ocean – Atmosphere Interaction

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**LaCOAS**

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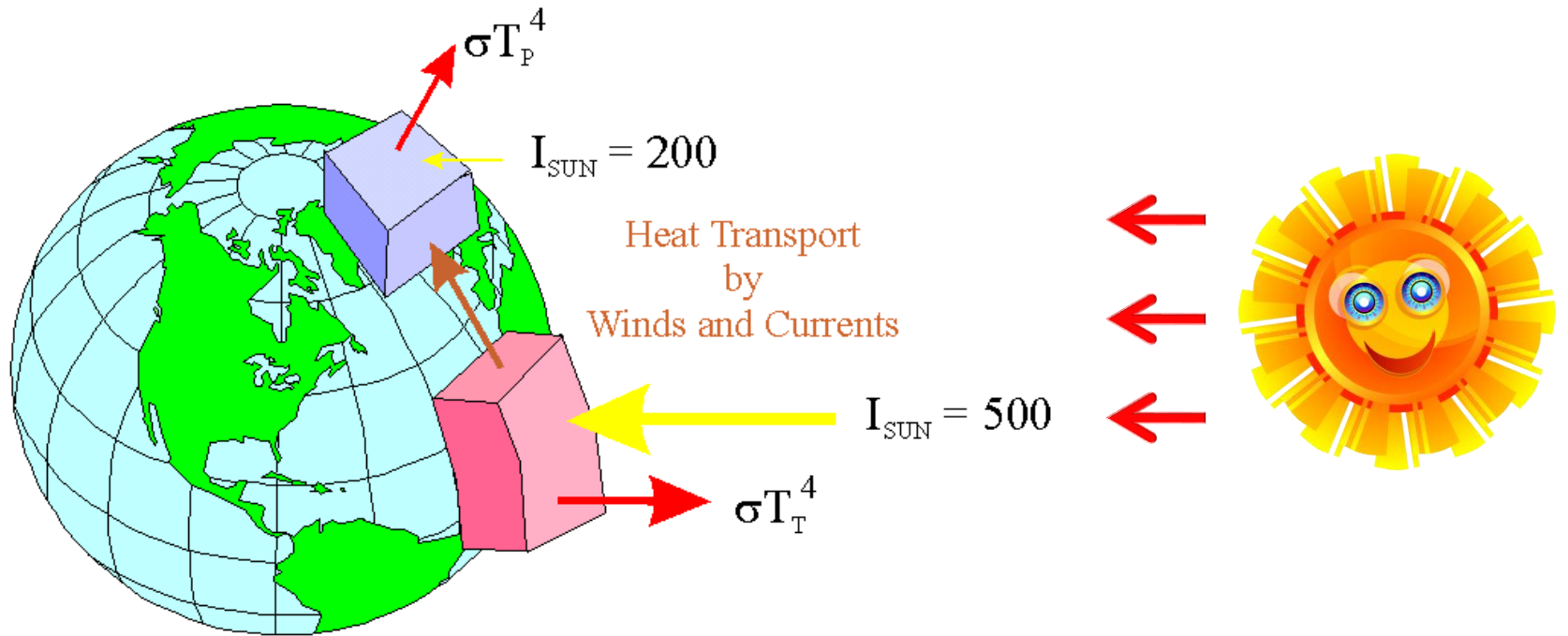
# Ocean-Atmosphere Interaction

1. Tropical-Extratropical, Interhemispheric Climate Interaction : Atmospheric Bridge and Oceanic Tunnel
2. Dynamics of Decadal Climate Variability and Tropical Decadal Variability
3. Ocean-Atmosphere Interaction: A Global Scale, Coupled Climate Dynamics and Bjerknes Compensation
4. Timescale and Reversibility of Climate Change

## Bjerknes补偿: 海气耦合系统本征模

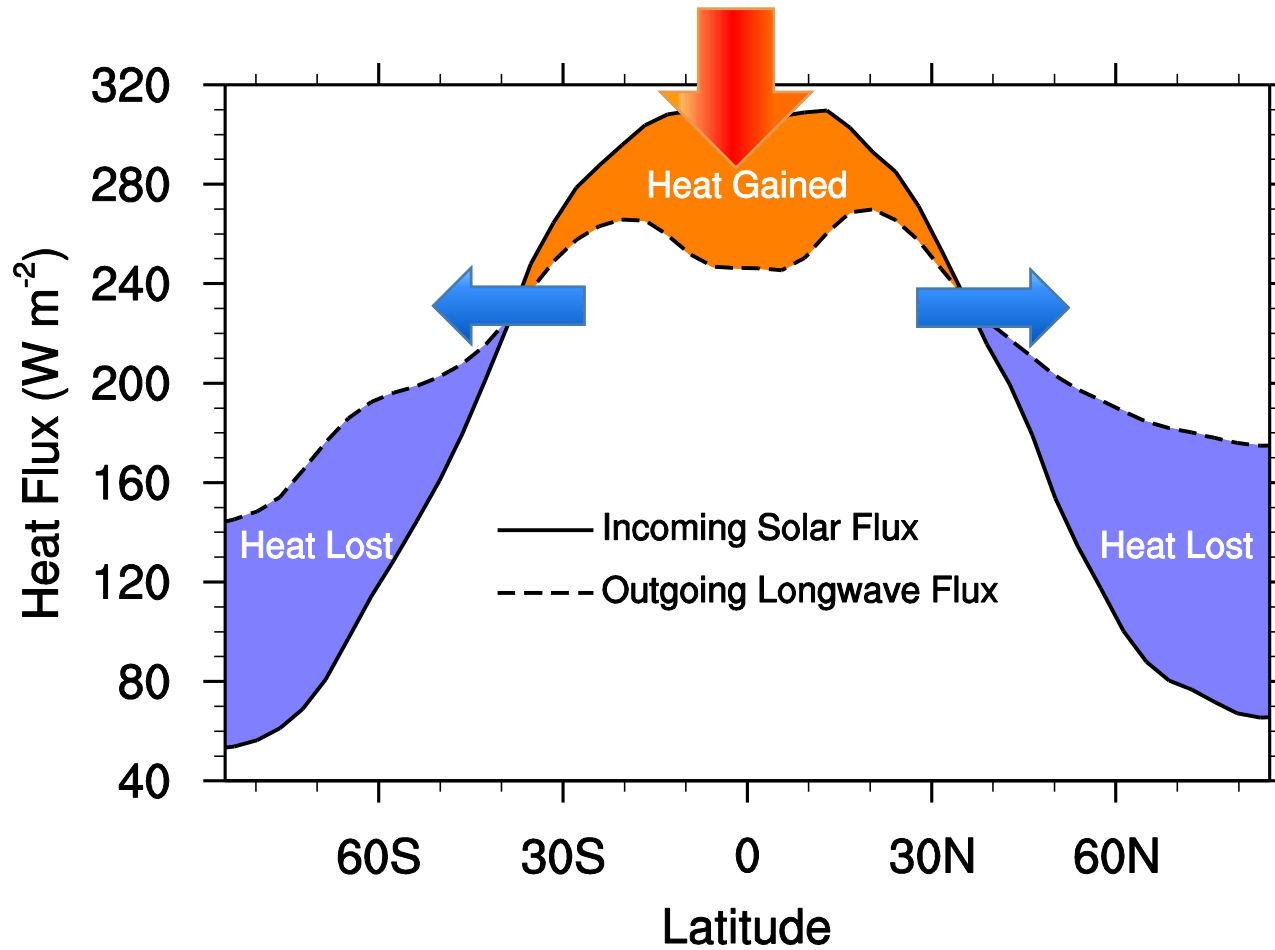
- Fundamentals
- Questions
- Hypothesis and Theory
- CGCM results
- Aquaplanet
- Summary

# Fundamentals





# Heat Budget at the TOA



## Fundamental Questions

# Energy

$$\text{Energy} = c_p T + L_v q + gz + \frac{(u^2 + v^2 + w^2)}{2}$$

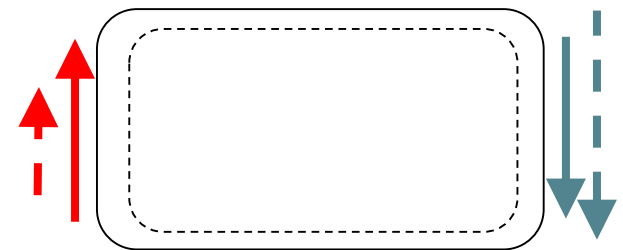
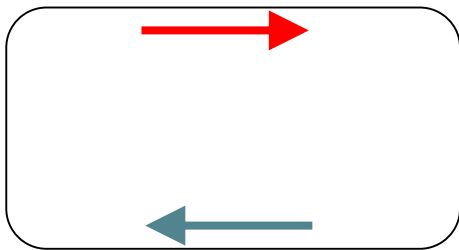
- **Sensible Heat / Latent heat**
  - **Potential energy / Kinetic energy**
1. **Kinetic energy transport is small**
  2. **In the ocean only sensible heat transport**

## Fundamental Questions

# Energy Transport Mechanisms

Energy multiply by meridional mass transport

$$F_E = \Psi C \Delta E$$



- Hadley Cell
- Ferrell Cell
- AMOC
- Wind-driven STC

- Monsoon Circulation
- Oceanic Gyres

## *Eddies:*

- Standing Waves
- Transient Storms
- Instability Waves
- Gulf Stream Rings...

# Ocean Heat Transport Calculation

## Temperature equation

$$\frac{\partial T}{\partial t} + \frac{\partial(u + u^* + u')T}{\partial x} + \frac{\partial(v + v^* + v')T}{\partial y} + \frac{\partial(w + w^* + w')T}{\partial z} = R(T) + D_v(T) + \frac{\partial Q}{\partial z}$$

Zonal and Vertical Integration

$$\iiint \frac{\partial T}{\partial t} dx dy dz + \iint (v + v^* + v')T dx dz = \iiint R(T) dx dy dz + \iint Q_0 dx dy$$

Storage

OHT<sub>VT</sub>

OHT<sub>diff</sub>

OHT<sub>HF</sub>

OHT<sub>eul</sub> + OHT<sub>bol</sub> + OHT<sub>sbm</sub>

# Ocean Heat Transport Calculation

$$\text{OHT} = \text{OHT}_{\text{VT}} = \text{OHT}_{\text{eul}} + \cancel{\text{OHT}_{\text{bol}}} + \cancel{\text{OHT}_{\text{sbm}}} = \text{OHT}_{\text{HF}} + \cancel{\text{OHT}_{\text{diff}}} - \cancel{\text{Storage}}$$

No Submesoscale Eddies                      Equilibrium

No Mesoscale Eddies                      No Mixing

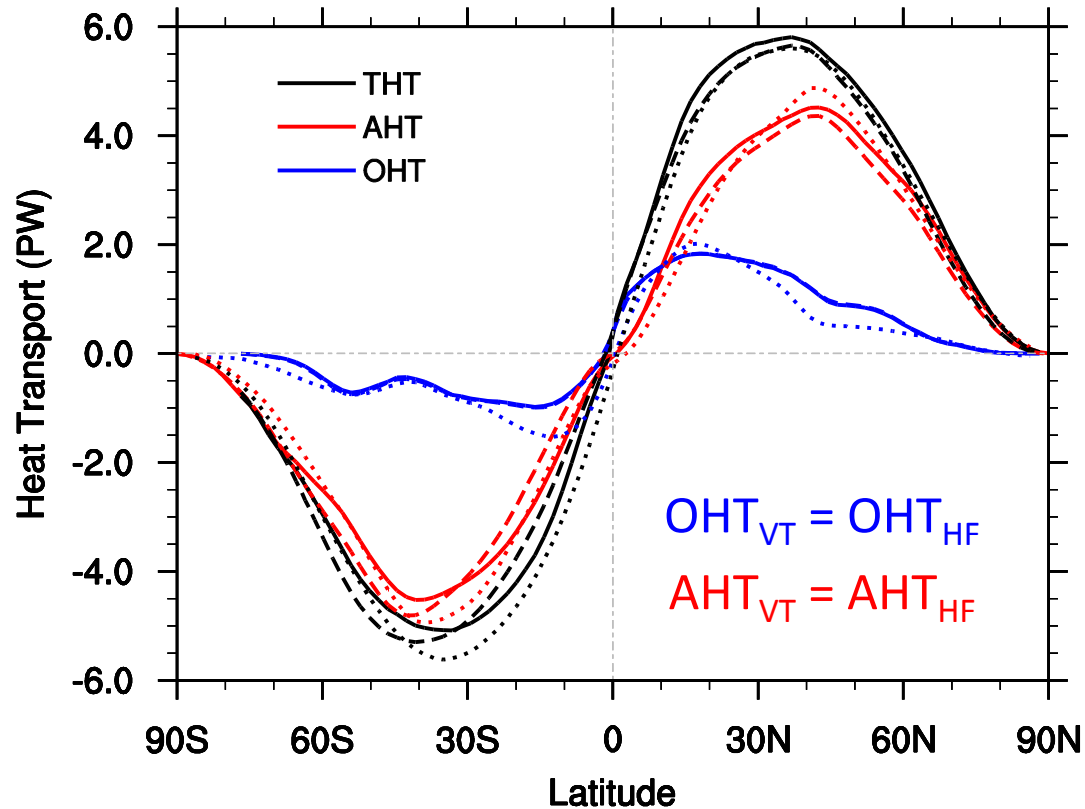


$$\text{OHT}_{\text{VT}} \approx \text{OHT}_{\text{HF}} \approx \text{OHT}_{\text{eul}}$$

# Calculation in CGCM

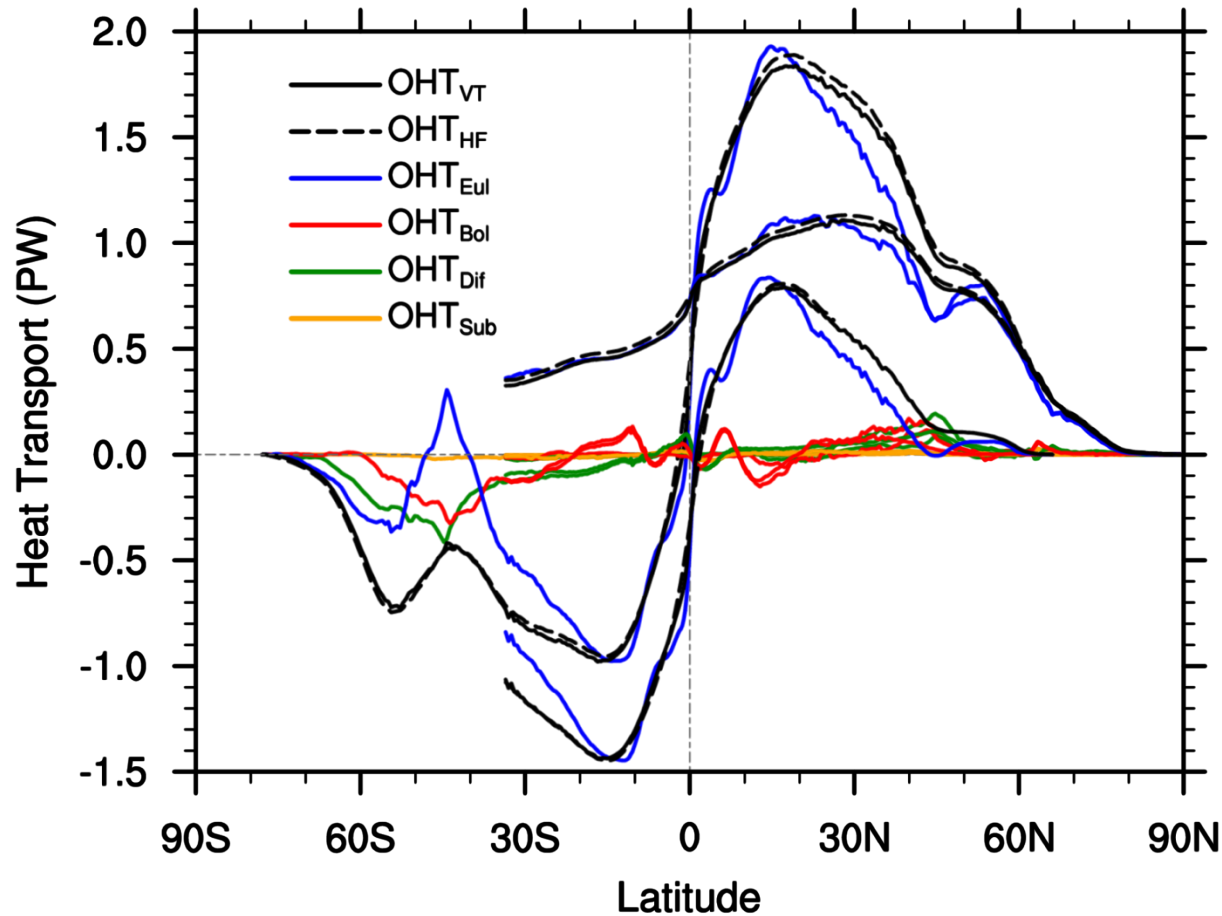
- ◇ **Real** heat transport by **Atmosphere** and **Ocean**
- ◇ OHT components:
  - ◇ Basin contribution / Wind-driven / Thermohaline
- ◇ AHT components:
  - ◇ **Dry air** VS. **Water vapor** / **Mean** VS. **Eddies**

# Meridional Heat Transport



Dotted lines from Obs. Heat Flux (Trenberth and Caron, 2001)

# Decomposing $OHT_{VT}$

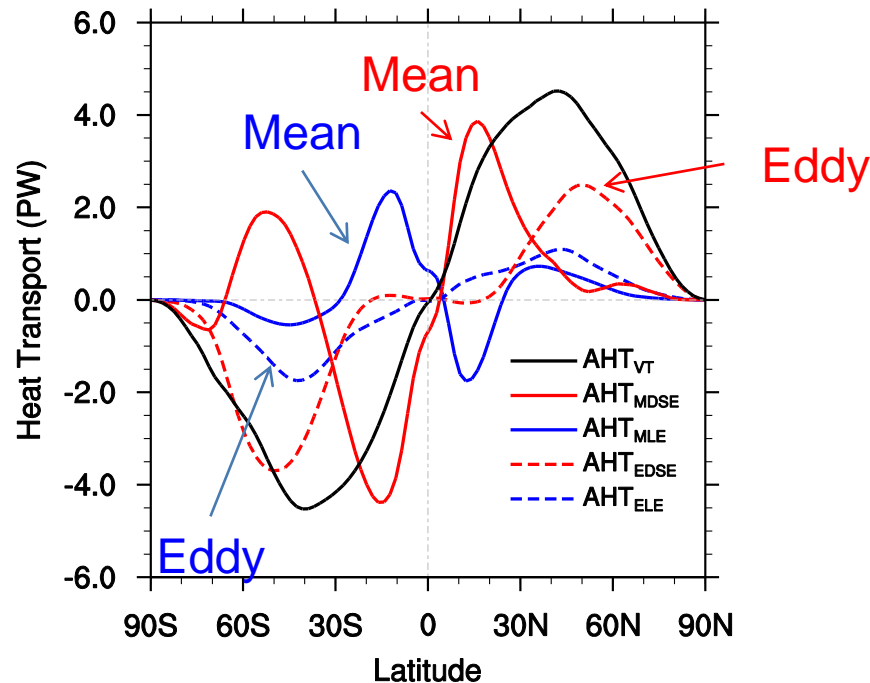
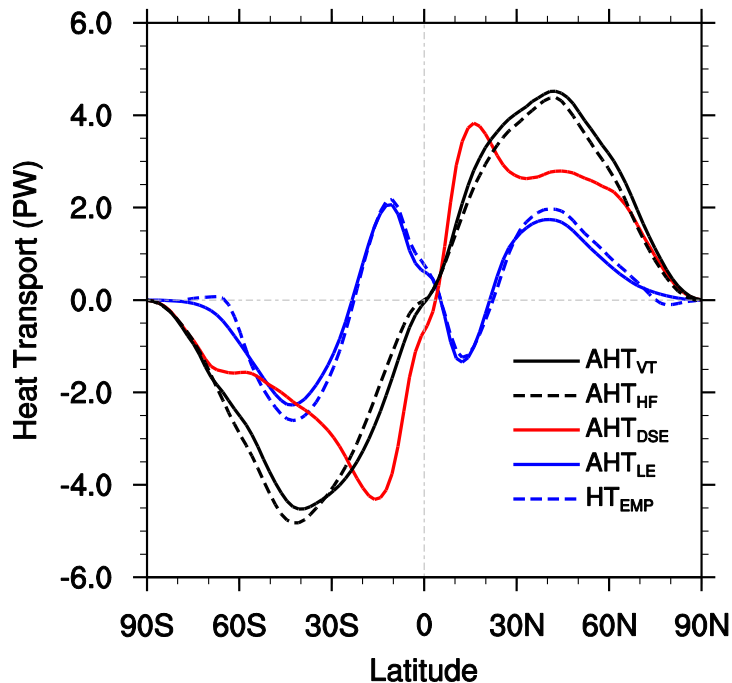


Consistency between  $OHT_{VT}$  and  $OHT_{HF}$   
Important role of Bolus and dissipation in ACC

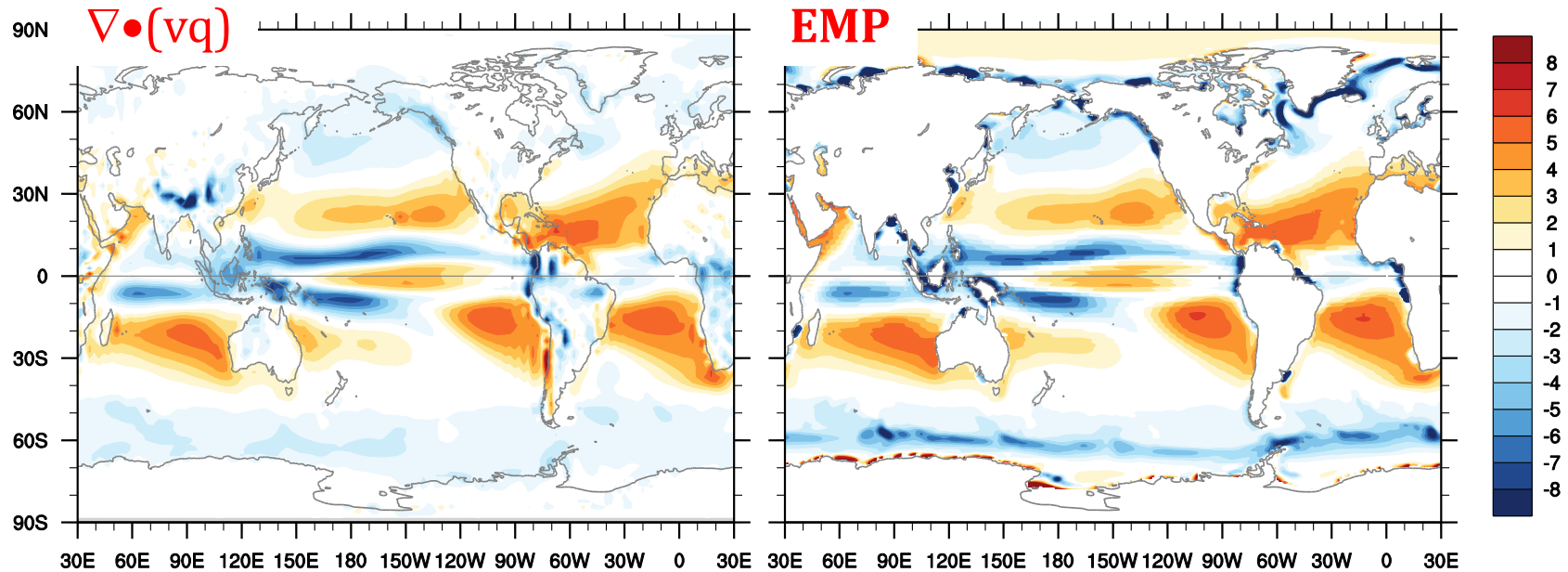
Yang and Li (2015)



# Decomposing $AHT_{VT}$



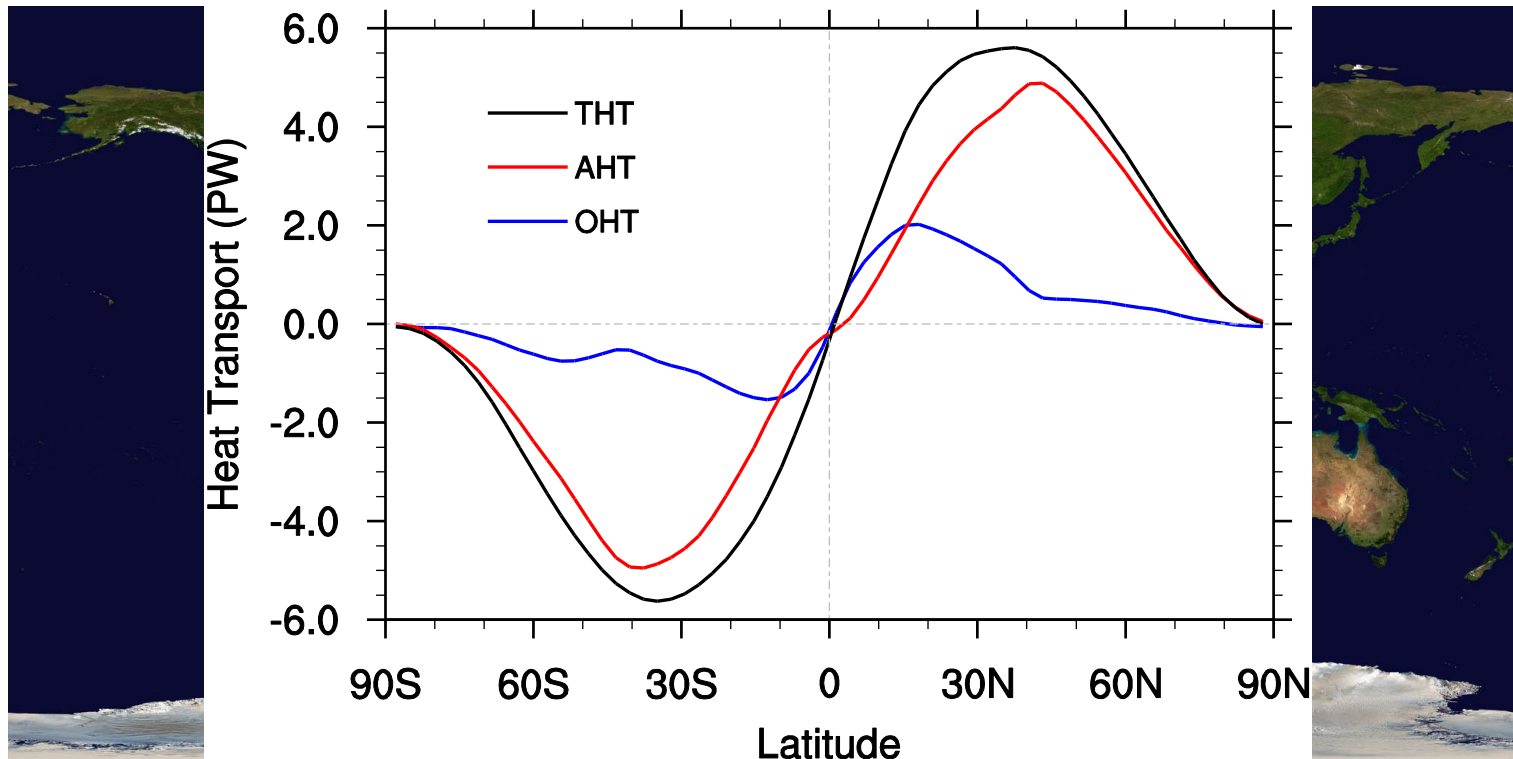
# Divergence of Water Vapor Transport



- Vertically integrated water vapor divergence  $\nabla \cdot (vq)$
- Comes from EMP over the global ocean (unit:  $10^{-5} \text{ kgm}^{-2}\text{s}^{-1}$ )

# Fundamental Questions

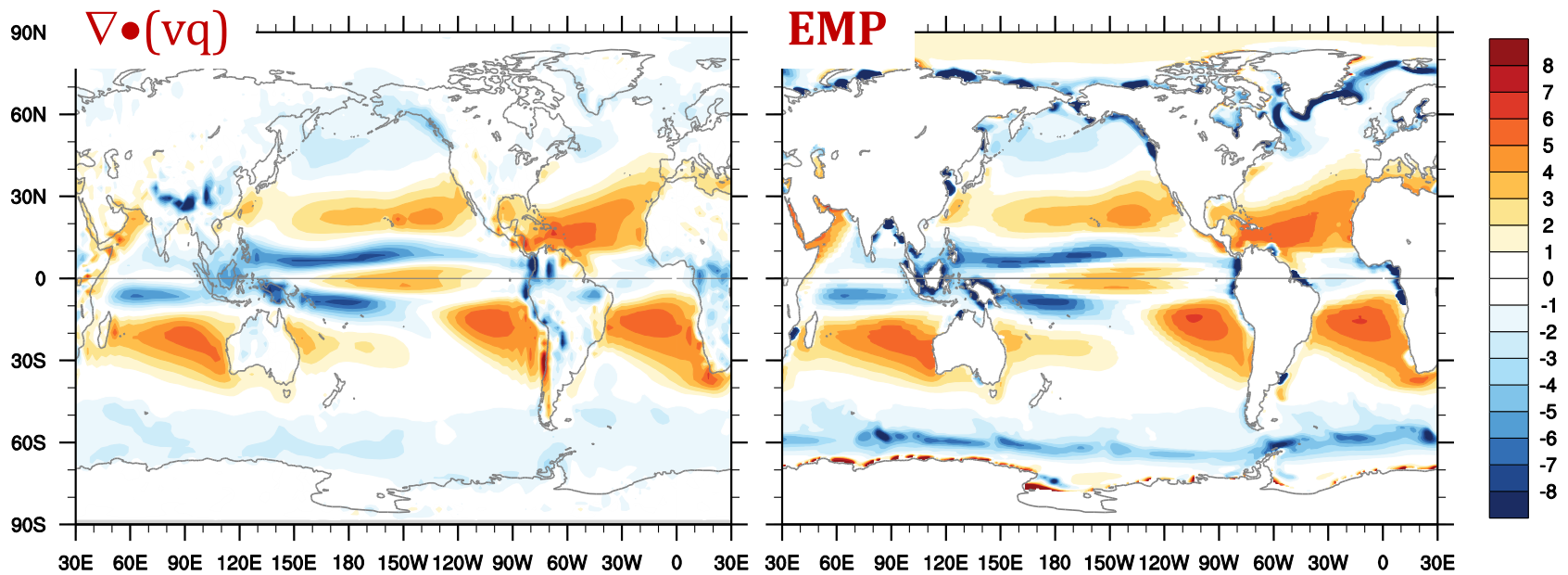
## 1. Antisymmetric MHT?



**Aquaplanet → Real Earth**

Trenberth and Caron (2001)

## 2. “Real” Oceanic Contribution?

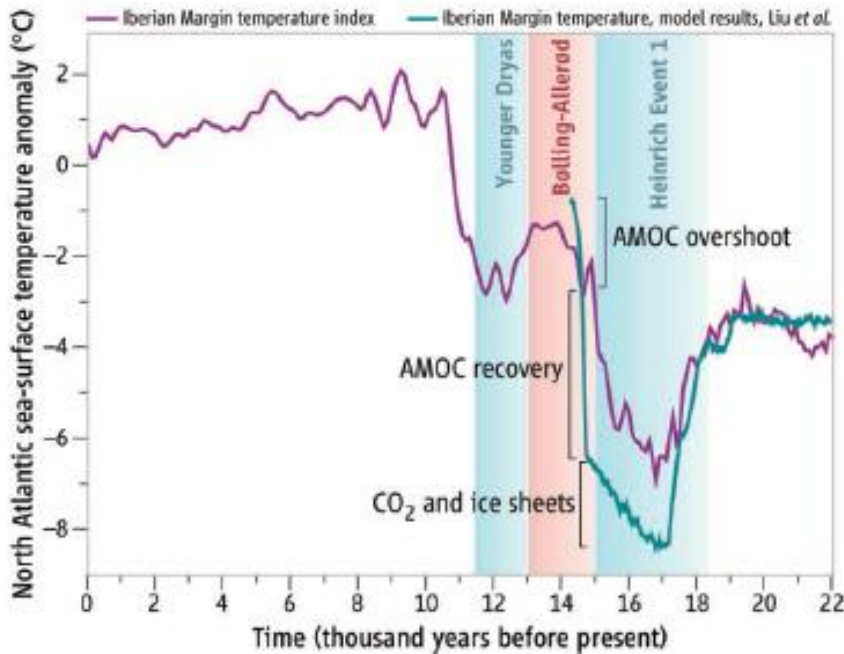


Yang and Li (2015)

# Fundamental Questions

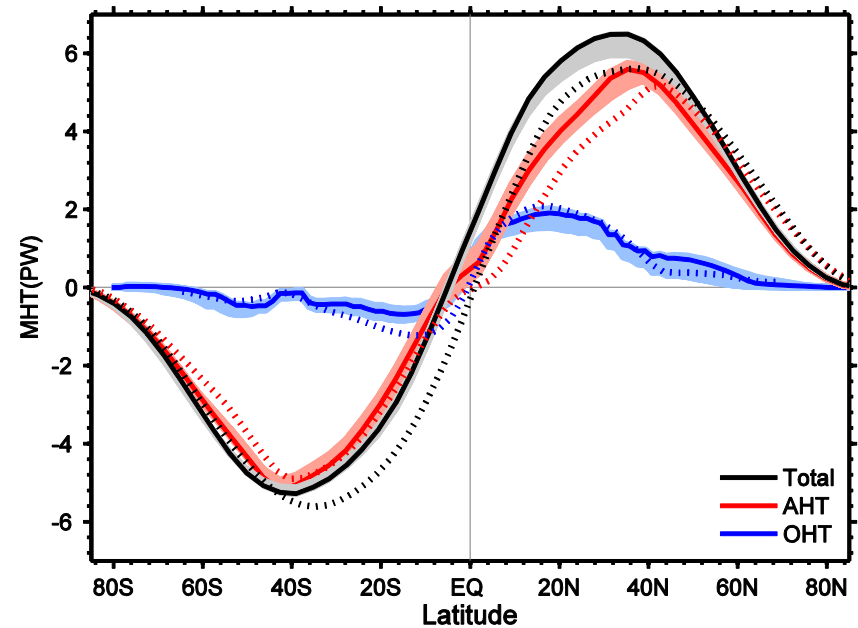
## 3. Relationship between OHT and AHT Changes?

### Earth Climate Stability Mechanism



Climate Change during Past 22 kyr

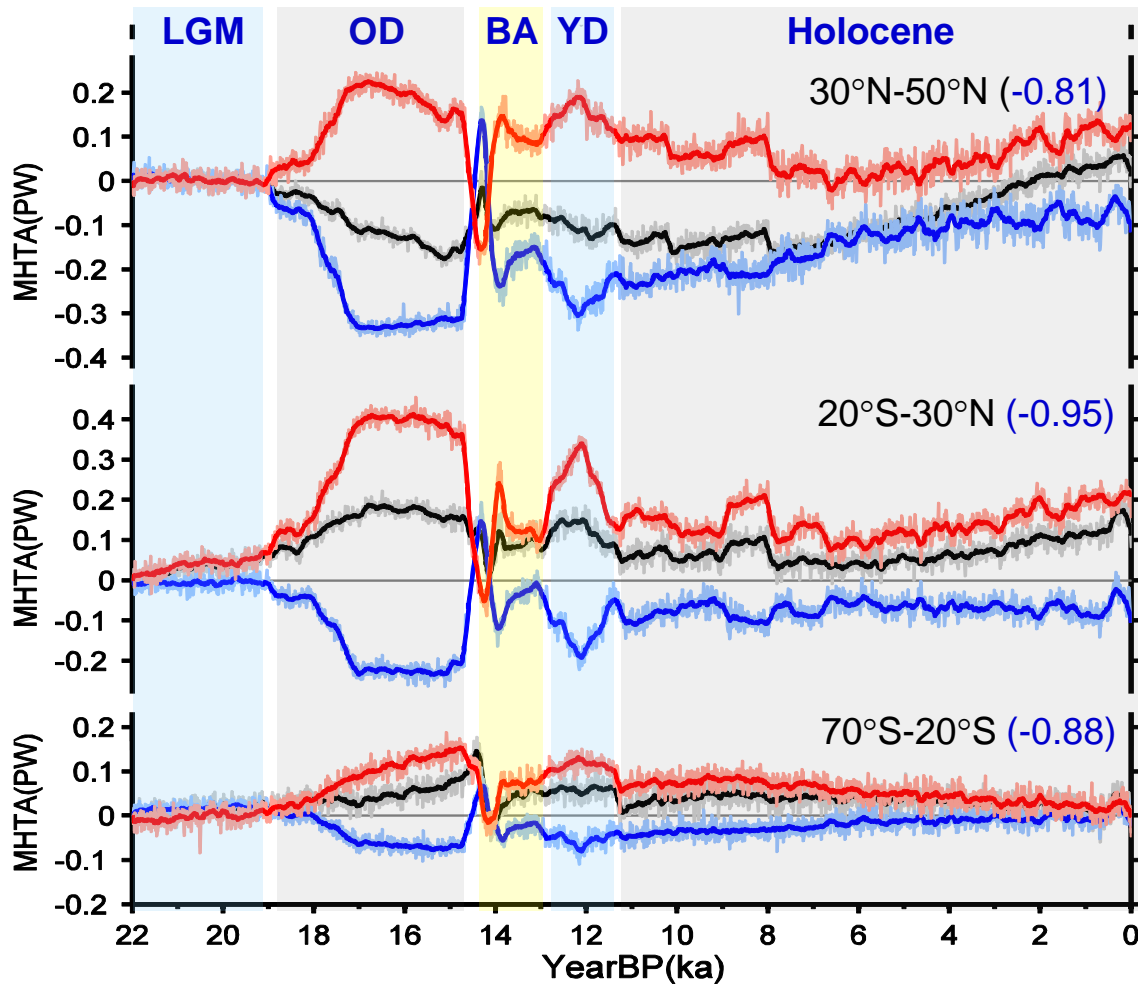
Timmermann (2009), Science



MHT from CCSM3 simulation TraCE-21K, From LGM to present

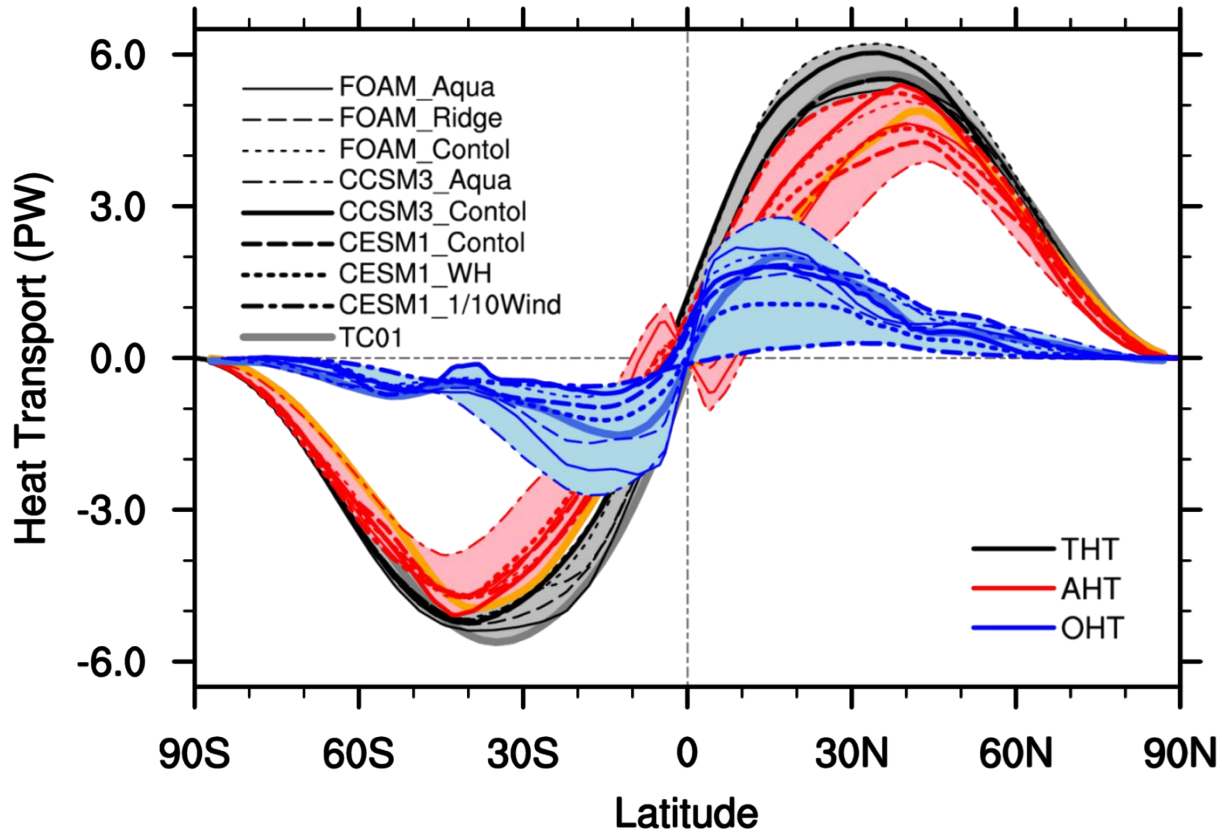
Liu et al. (2009); He (2011)

# MHT Change Since LGM



Yang et al. (2015)

# Compensation between AHT and OHT



Note: TC01 is from Trenberth and Caron (2001)



# Hypothesis: Bjerknnes Compensation

Jacob Aal Bonnevie Bjerknnes  
1897-1975

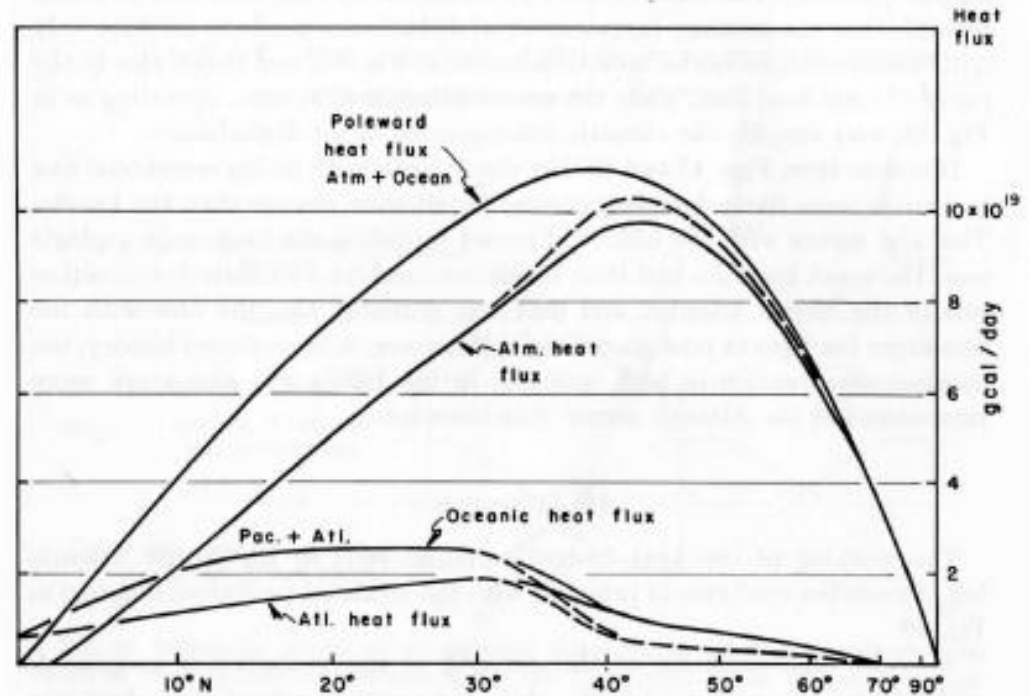
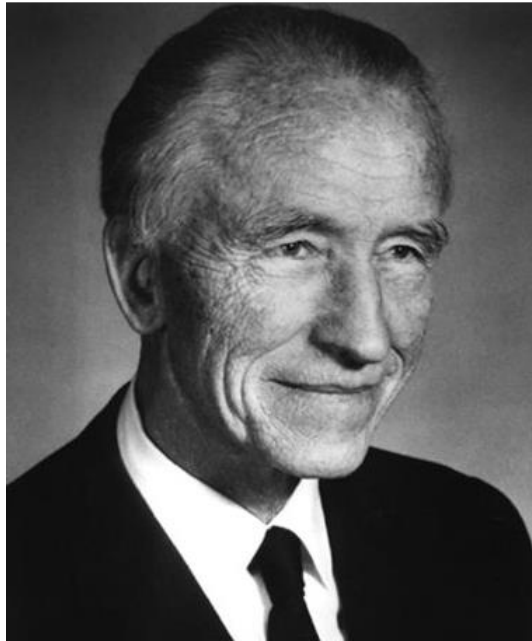


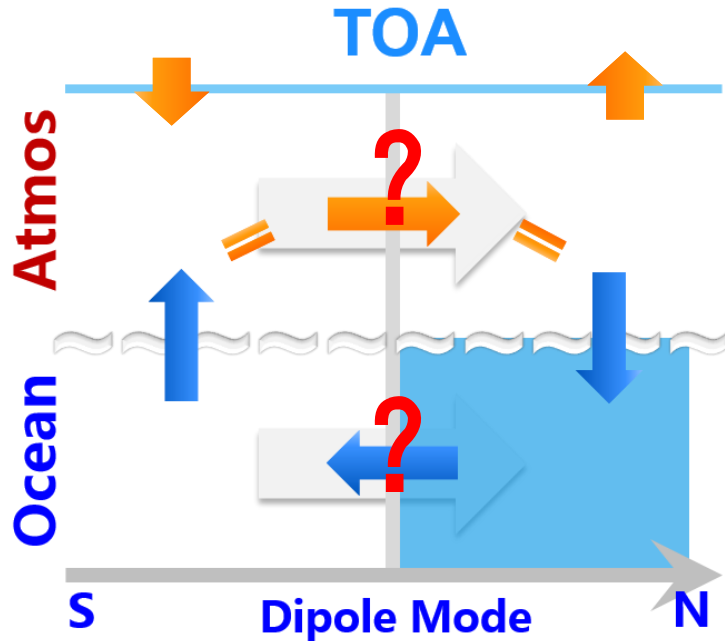
FIG. 48. Solid lines: flux data from Fig. 47 pertaining to present climatic conditions. Dashed lines refer to a sketchy model of the conditions around 1800 A.D. and show qualitative estimate of curtailed Atlantic and total oceanic heat flux as well as increased heat flux by low index atmospheric circulation. The anomalies of heat flux in oceans and atmosphere are assumed to cancel, leaving total heat flux and radiation budget unchanged. Actually, some change in the radiation budget is also likely to have taken place, but it could well have been quite small.

Bjerknes, 1964: Atlantic Air-Sea Interaction, *Advances in Geophysics*, Vol. 10, P77



# Hypothesis: Bjerknes Compensation

Question: How Climate Feedback Determines BJC?



$$A + B = 0 \rightarrow A = -B$$

but  $A + B + C = 0$

C: climate feedback

Then  $A = -(B + C)$

Energy Conserved

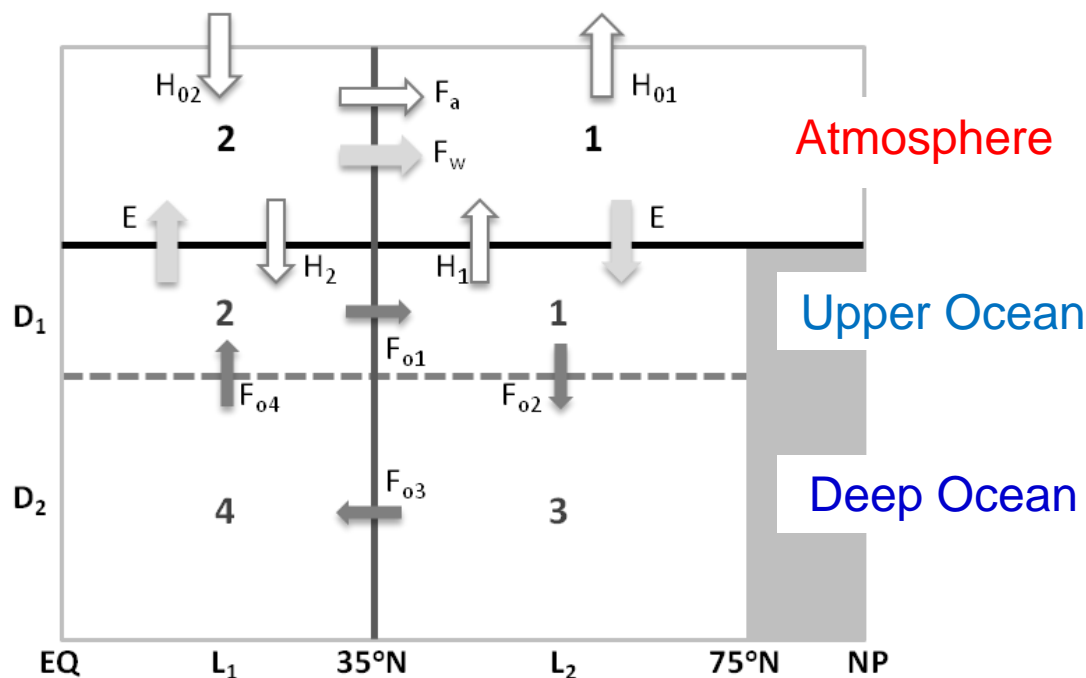
# Theory for **Equilibrium** Change

1. **Coupled Multi-Box Model**
2. **1-D Energy Balance Model (EBM)**

**Go to Final Equations**

# Coupled Multi-Box Model

Yang, Zhao and Liu, 2016: Understanding Bjerknes compensation in atmosphere and ocean heat transports using a coupled box model. *J. Climate*



Stommel (1961); Nakamura et al. (1994); Marotzke and Stone (1995);  
Tziperman et al. (1994); Tziperman and Ioannou (2002)

**Go to Final Equations**

# Equations and Dynamics

$$T_{1\dots 2\dots 3\dots 4\dots}$$

$$S_{1\dots 2\dots 3\dots 4\dots}$$

$$\text{Heat Flux at TOA: } H_{1,2} = A_{1,2} - B_{1,2}T_{1,2}$$

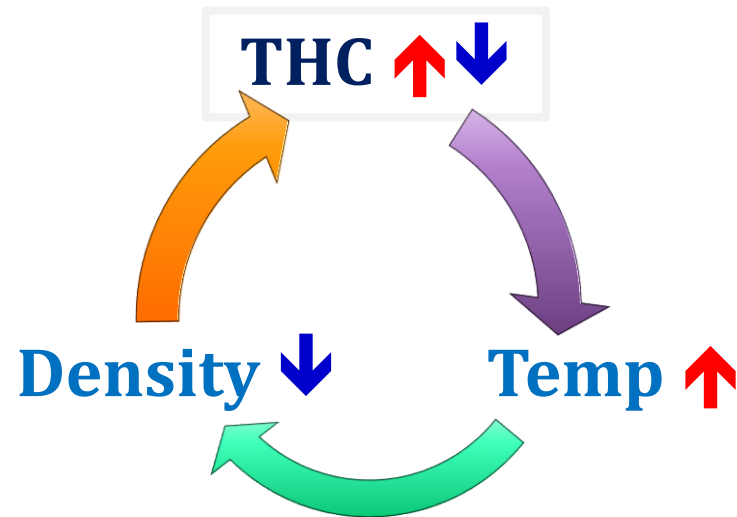
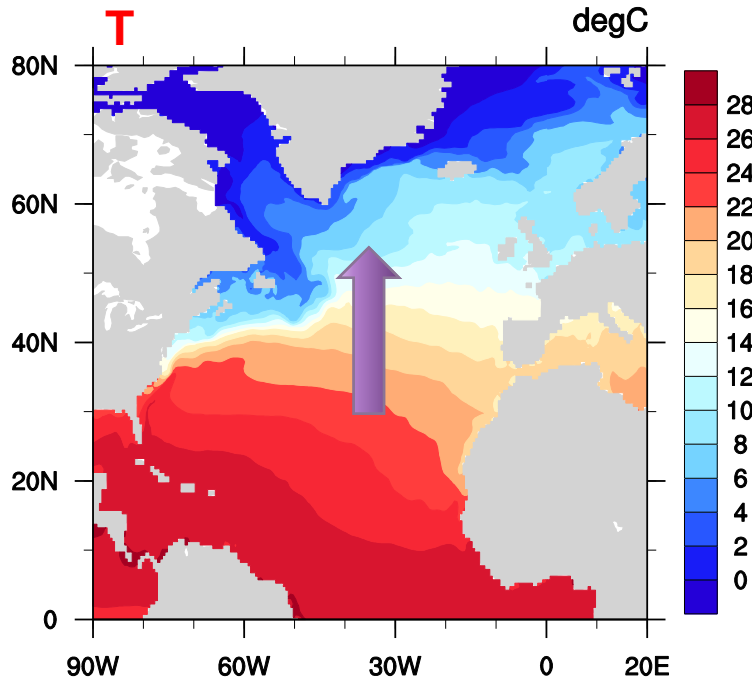
$$\text{Fresh Water Flux: } H_{fw} = \gamma(T_2 - T_1)$$

$$\text{Thermohaline: } q = \kappa[\alpha(T_2 - T_1) - \beta(S_2 - S_1)]$$

$$\text{AHT: } H_d \sim (T_2 - T_1) \quad \text{OHT: } O_d \sim q^*(T_2 - T_1)$$

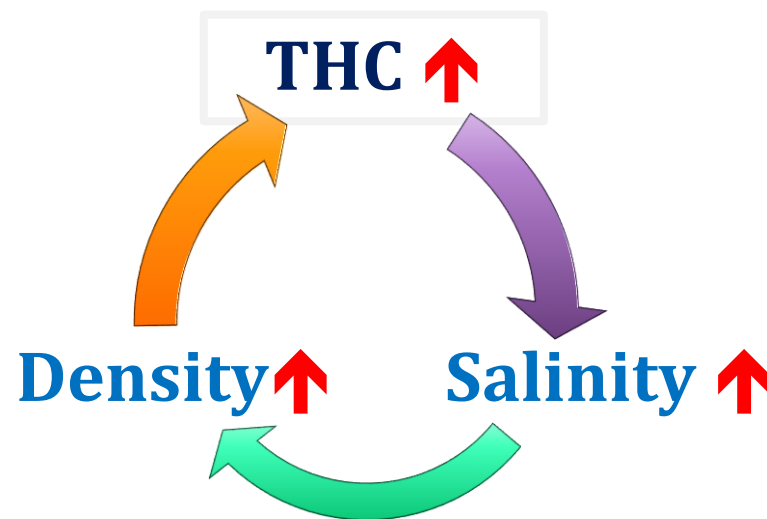
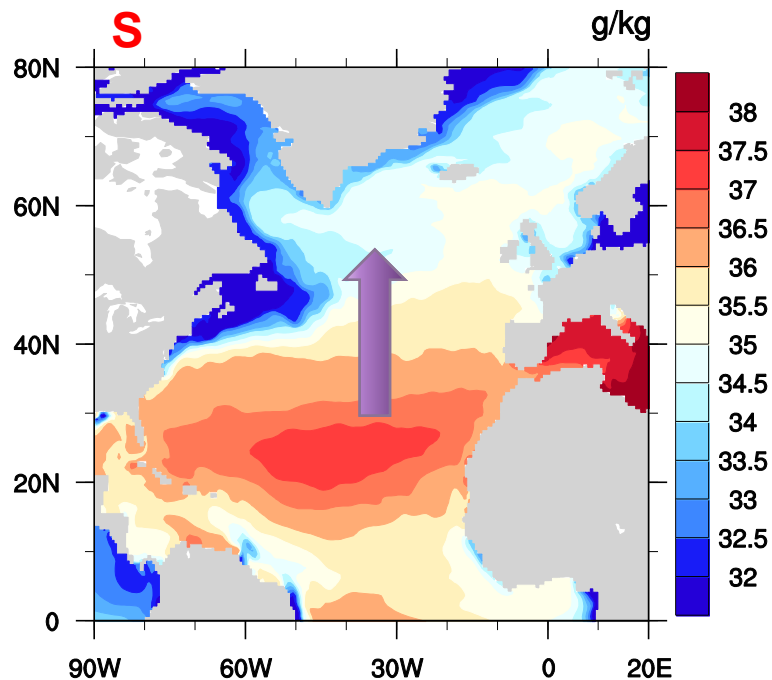
Yang, H., Y. Zhao, and Z. Liu, 2016: Understanding Bjerknes compensation in atmosphere and ocean heat transports using a coupled box model. *J. Climate*, 29(6), 2145-2160, doi: 10.1175/JCLI-D-15-0281.1.

# Negative Feedback: *THC* vs *T*



Willebrand (1993)

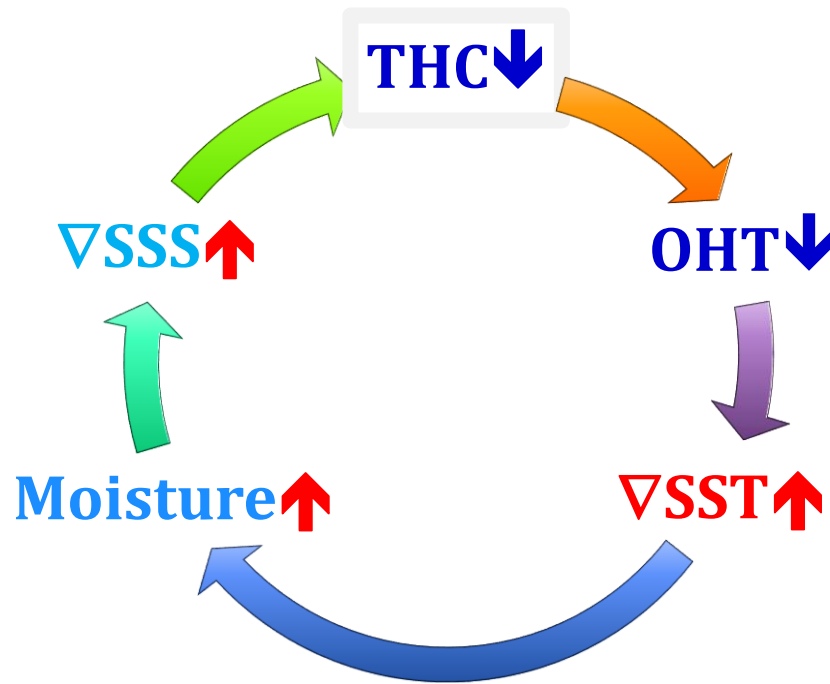
# Positive Feedback: *THC* vs *S*



Willebrand (1993)

# Positive Feedback: *THC* vs *EMT*

## EMT: Atmosphere Eddy Moisture Transport



Nakamura et al. (1994)

# Analytical Solution: BJC Rate

$$C_R \equiv \Delta H_a / \Delta H_o = -(B_1 + B_2)\chi / [B_1 B_2 + (B_1 + B_2)\chi]$$

if  $B_1 = B_2$

$$C_R = -1 / [1 + B/2\chi] < 0 \sim \text{Intrinsic Rate}$$

Intrinsic parameters:

- $B_{1,2} \sim$  Local feedback between  $T$  and  $HF$  at TOA
- $\chi \sim$  Atmospheric heat transport efficiency.



# Intrinsic Rate

$<1$ , if  $-B_1, -B_2 < 0$ , Undercompensation

$|C_R| = 1$ , if  $B_1 B_2 = 0$ , Full Compensation

$>1$ , if either  $-B_1$  or  $-B_2 > 0$ , Overcompensation

$B_{1,2} \sim$  Local climate feedback **VITAL!**

# 1-D Slab-Ocean Energy Balance Model

*Liu, Yang, He and Zhao, 2016: A theory for Bjerknes compensation: the role of climate feedback. J. Climate*

## Non-dimensional Equation

$$\partial_{xx}[M(x)T] - b(x)T + f(x) = 0, \quad \text{for } 0 < x < 1$$

## With Non-dimensional OHT and AHT

$$f(x) = -\partial_x H_O,$$

$$H_A = -\partial_x [M(x)T].$$

Stommel (1961); North, (1975)

# Analytical Solution: BJC Rate

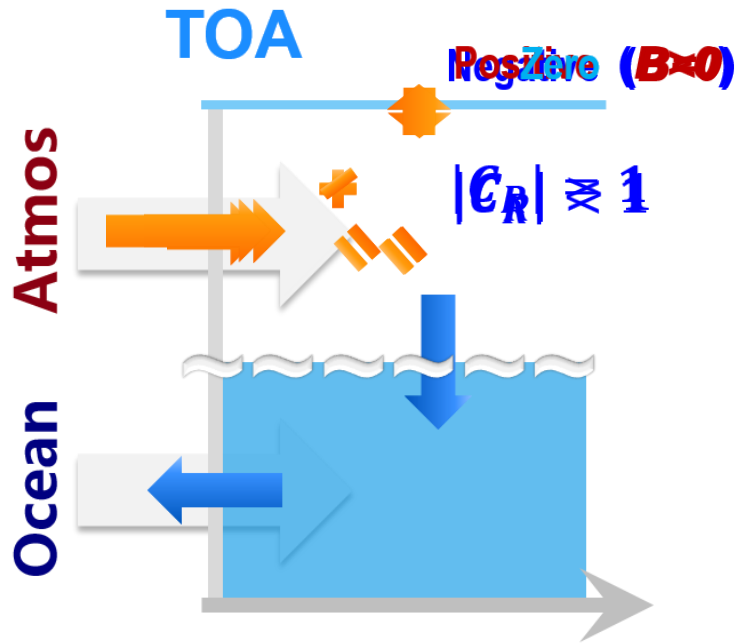
## Intrinsic Rate

$$C_R \equiv \Delta H_a / \Delta H_o = -1 / [1 + B / (n\pi)^2] < 0, n=1, 2, \dots$$

- $B$  ~ Intrinsic parameter, Local feedback between  $T$  and  $HF$  at TOA
- $n$  ~ Forcing scale.

# Coupled Intrinsic Mode

## Thermohaline-Climate Feedback-Energy Balance



$$C_R \equiv \frac{\Delta F_a}{\Delta F_o} = -\frac{1}{1-B} < 0$$

Local climate feedback  $B(y)$

Yang, Zhao and Liu (2016)  
Zhao, Yang and Liu (2016)

**Climate Feedback + MHT → Earth Energy Balance**

# Coupled Intrinsic Mode

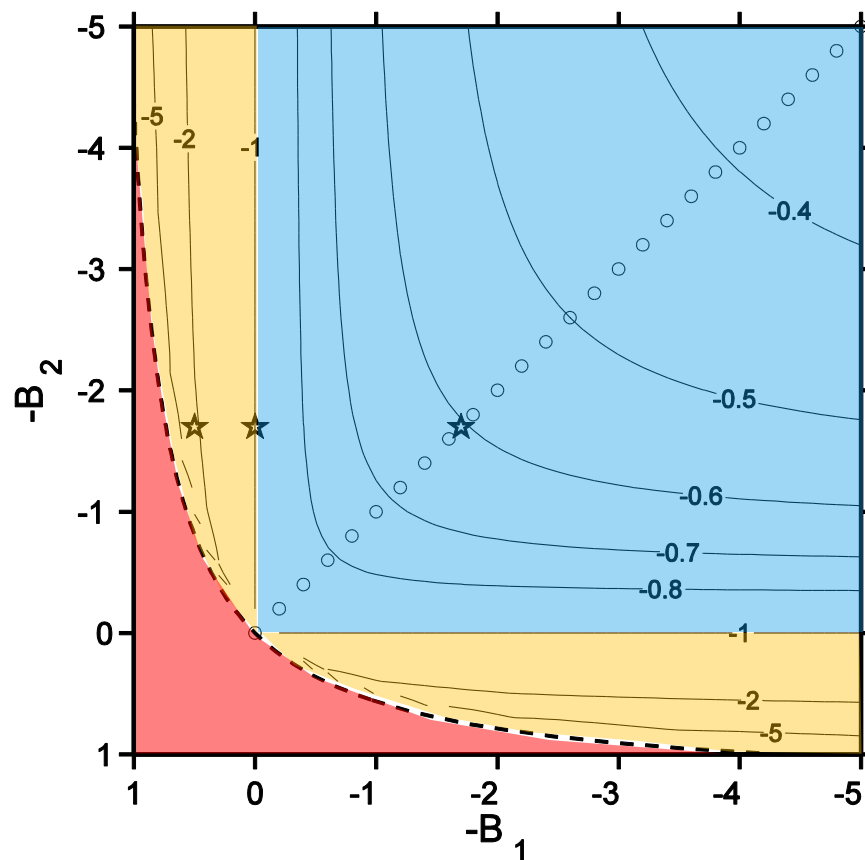
能量补偿  $\Leftrightarrow$  体重保持



$$C_R = -\frac{1}{1-B}$$

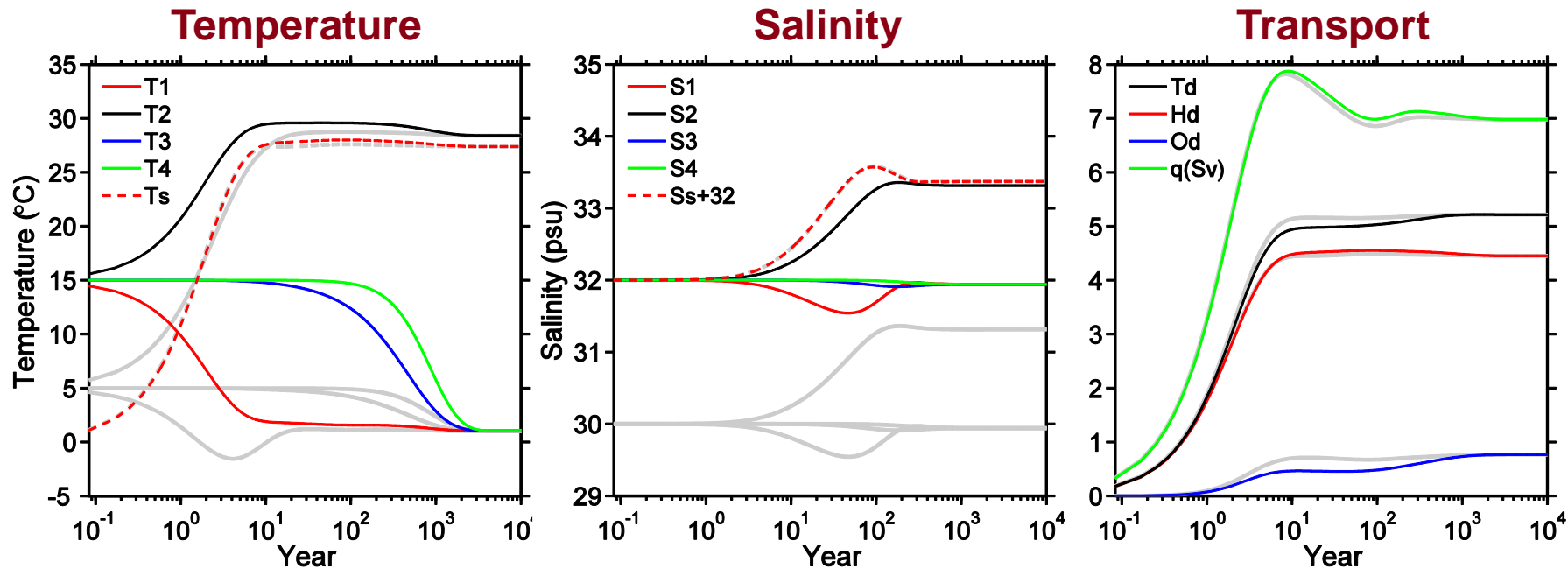
Go to BJC for Climate Variability

# Intrinsic Rate

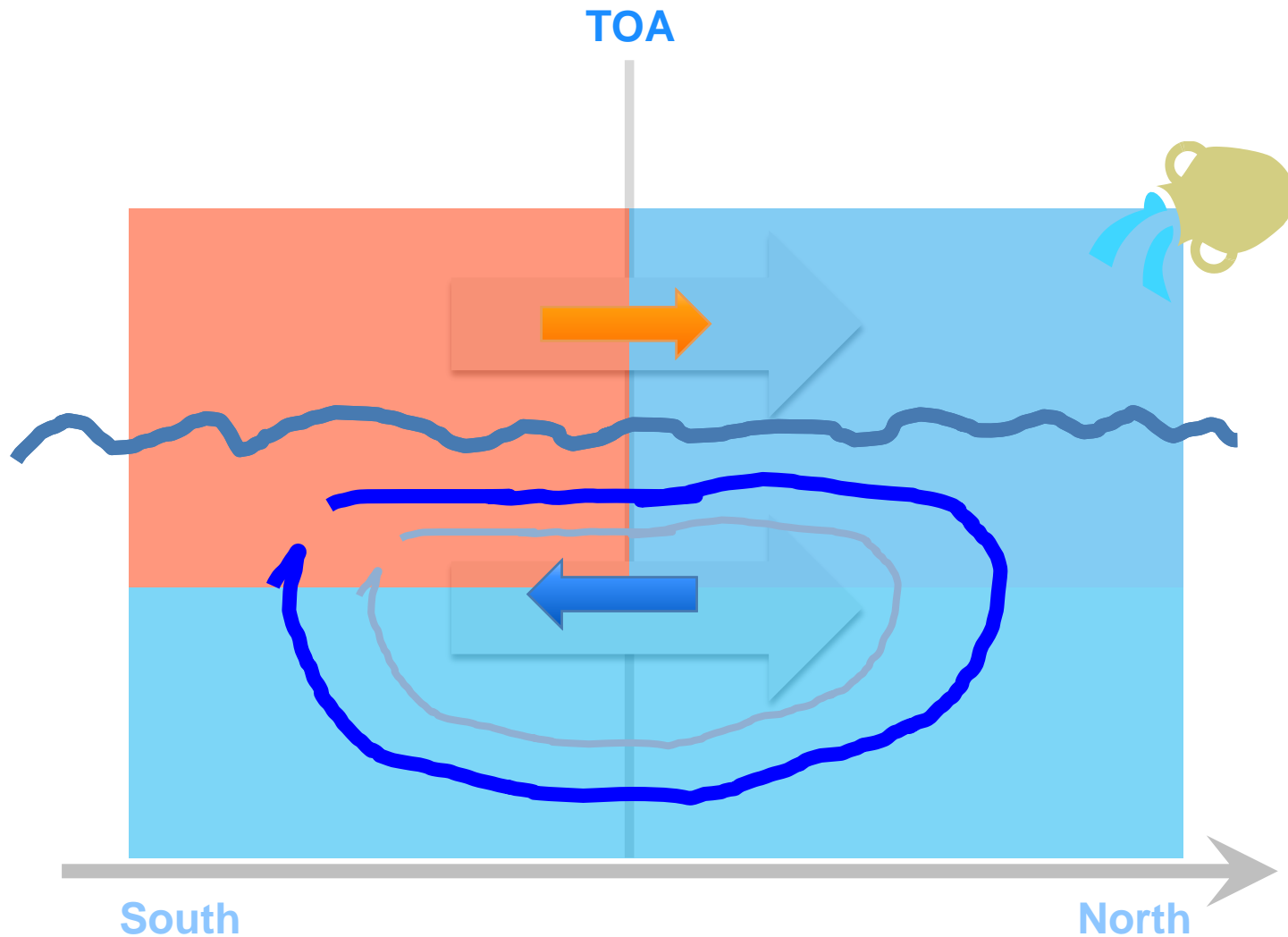


$$C_R = -(B_1 + B_2)\chi / [B_1 B_2 + (B_1 + B_2)\chi]$$

# Mean Climate

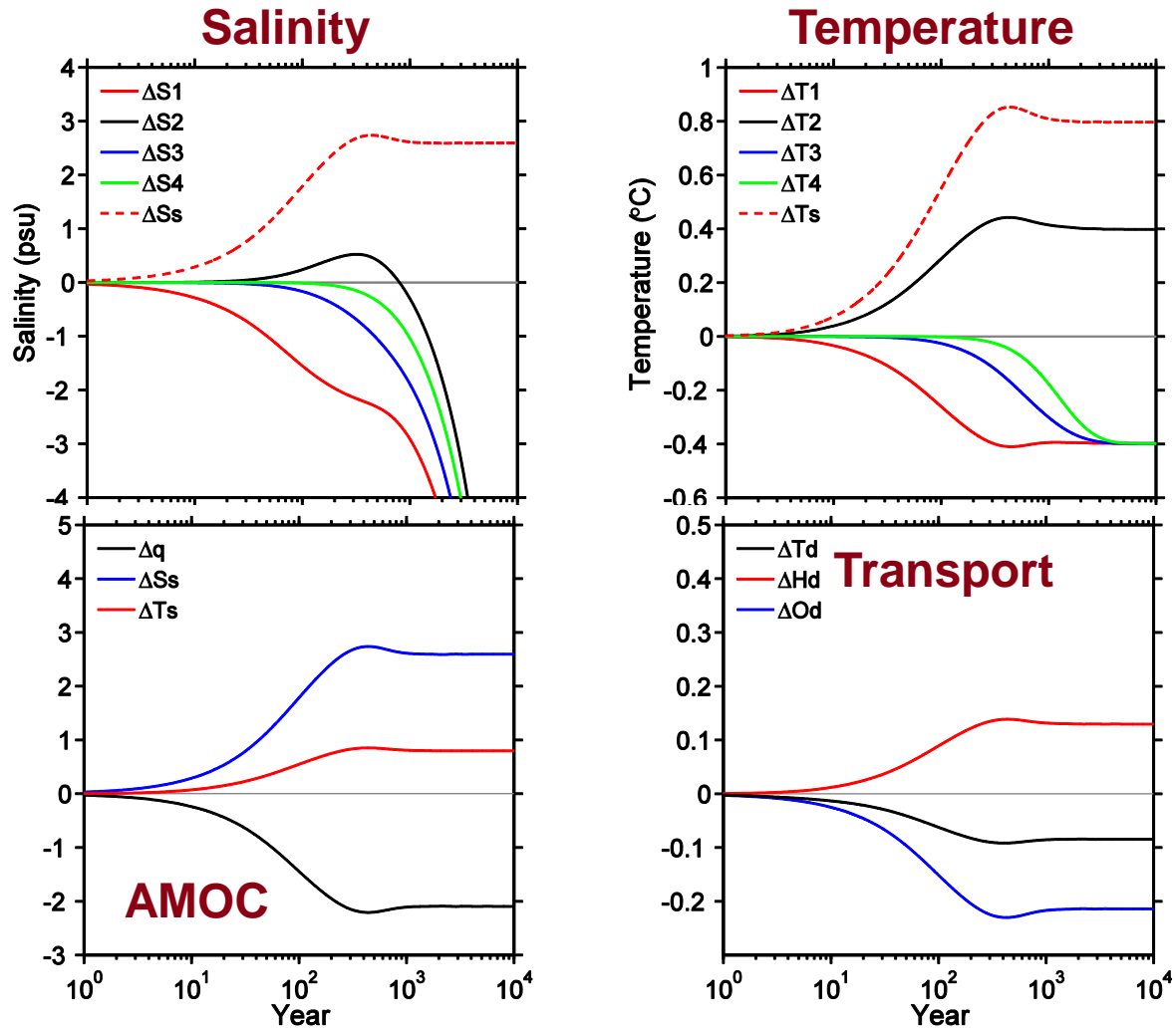


# How BJC Occurs: Fresh Water



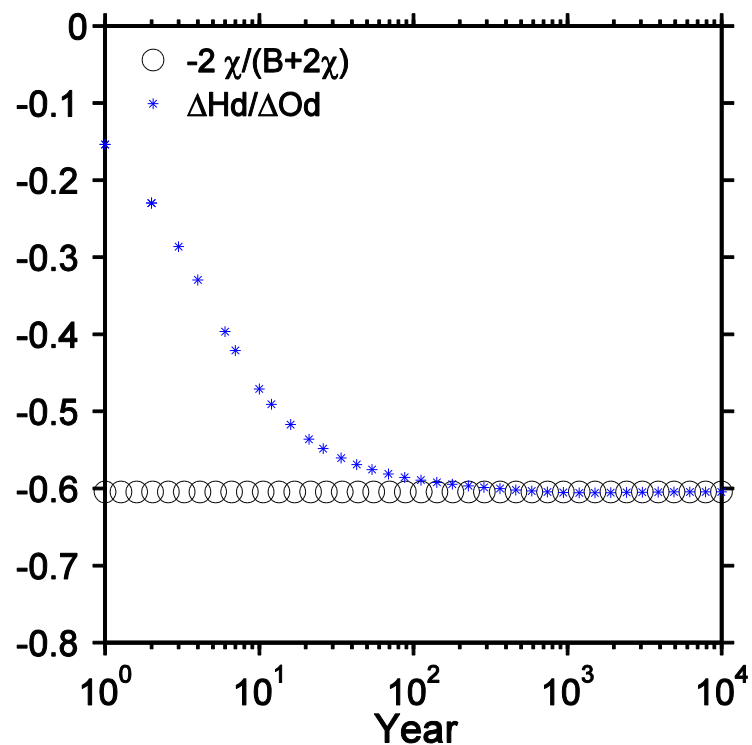


# Climate Change under Fresh Water



# BJC under Negative Feedback

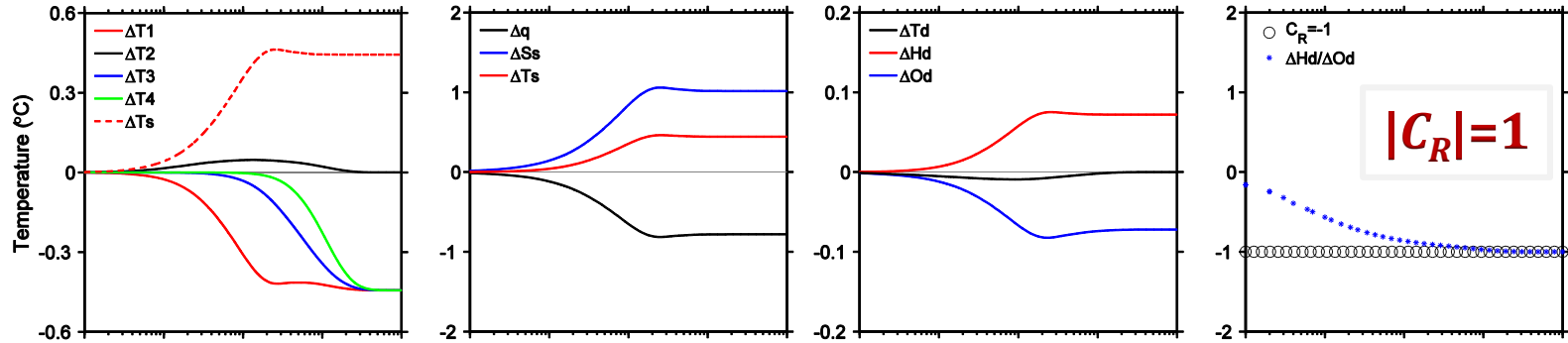
**Compensation Rate: Constant!**



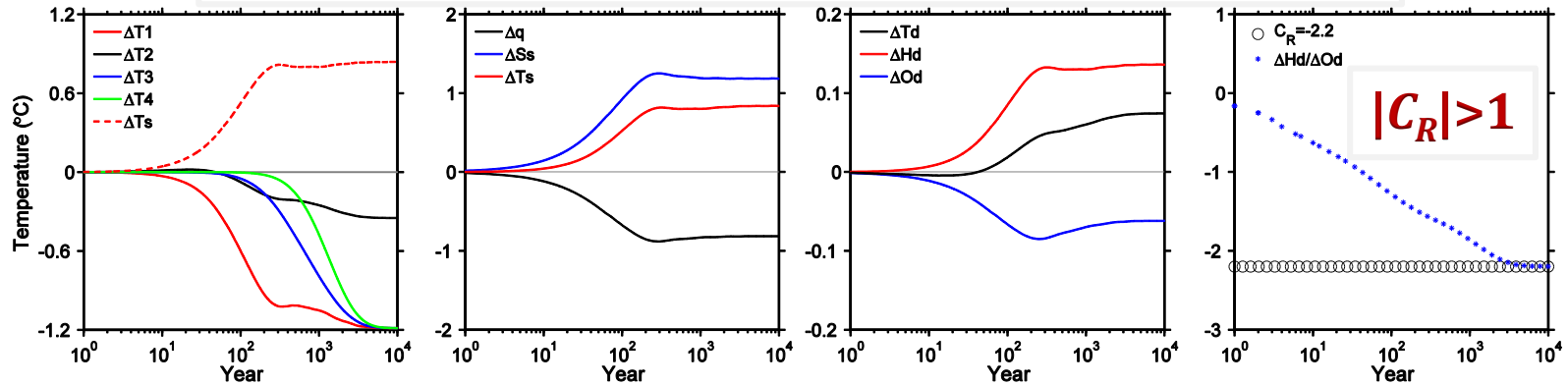
**Under-Compensation ( $-B_{1,2} < 0$ )**

# Climate Change under Fresh Water

## Full Compensation (-B1=0, Zero Feedback)



## Overcompensation (-B1=0.5, Positive Feedback)



# Modeling MHT and OHT in Past 22ka

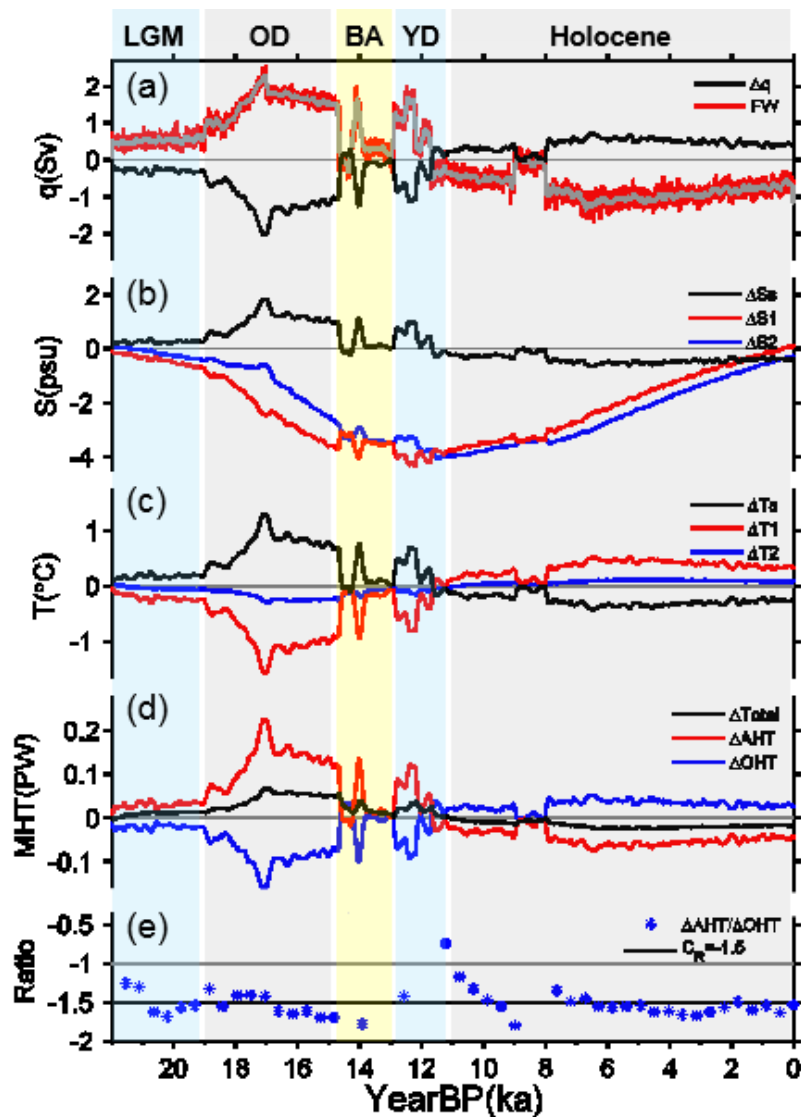
Freshwater Forcing

Salinity Change

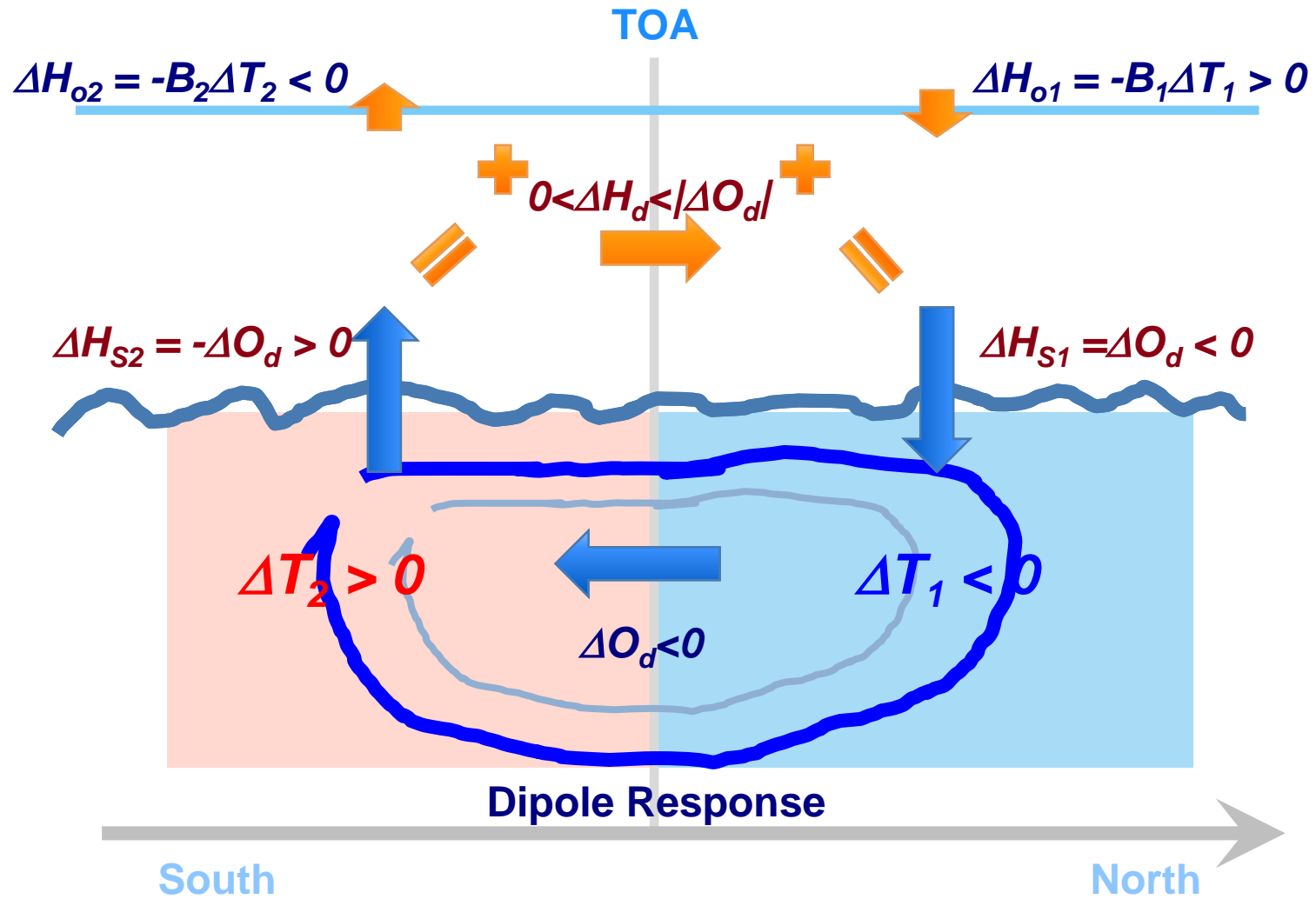
Temperature Change

AHT and OHT

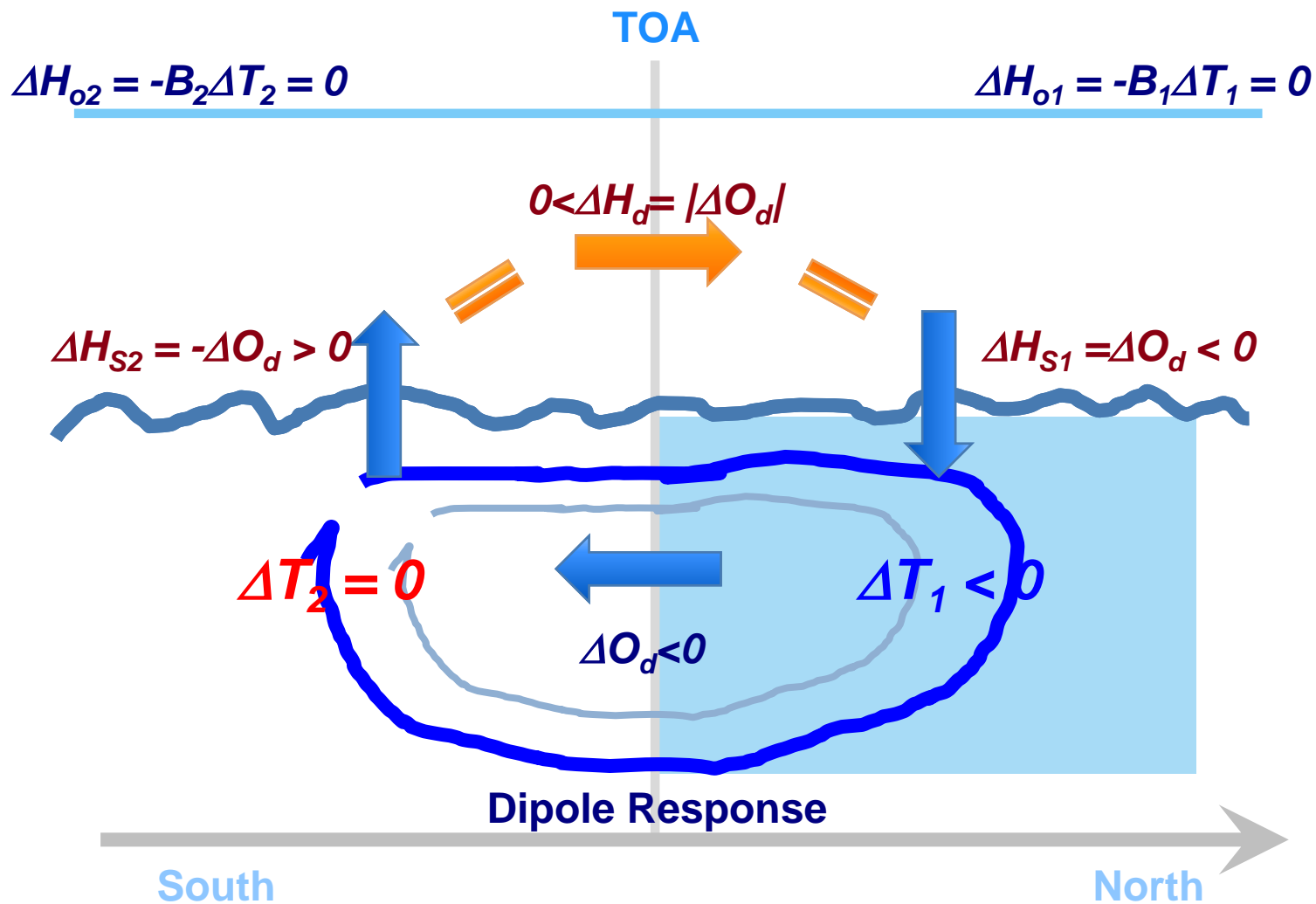
BJC = -1.5



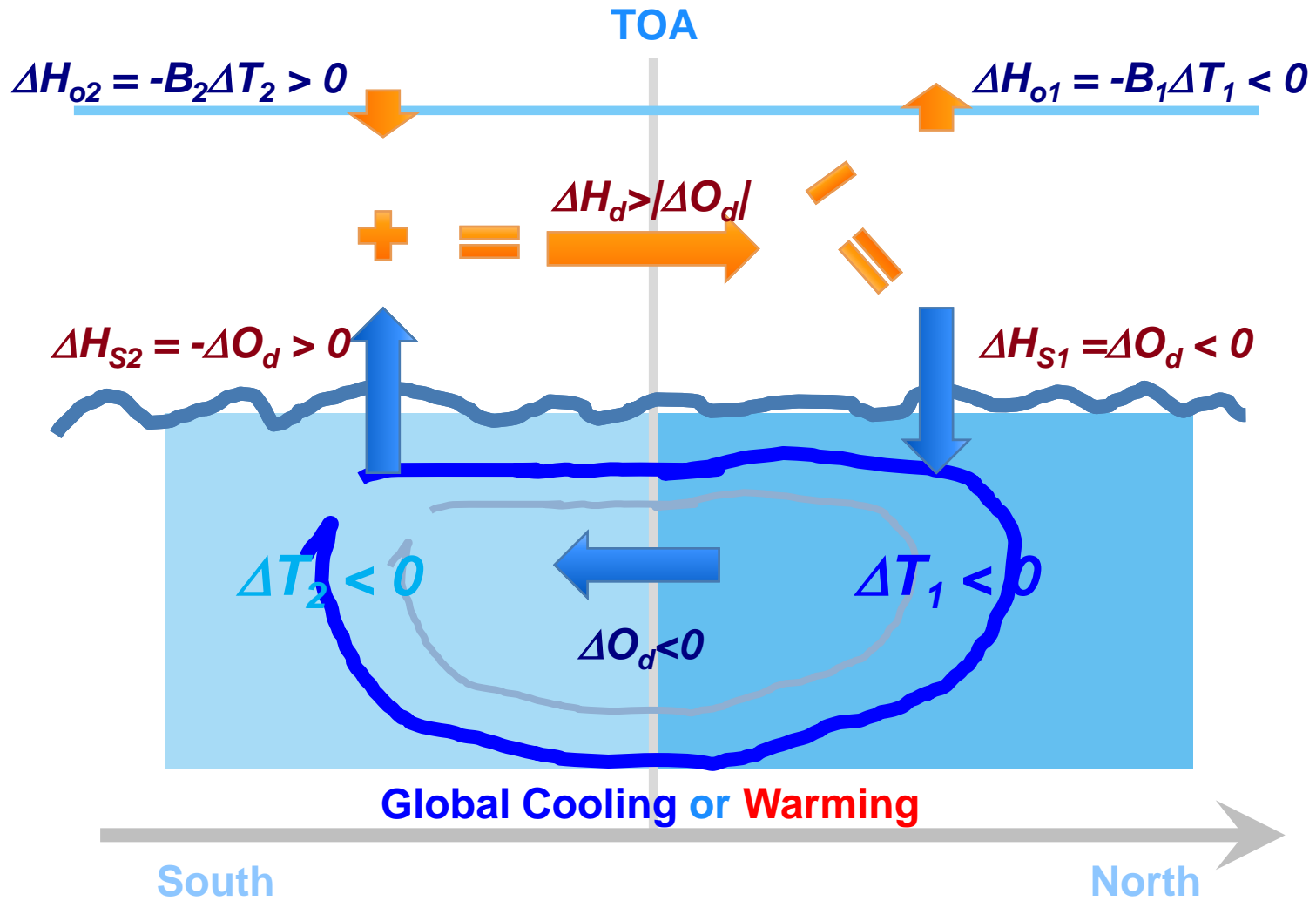
# Mechanism for Undercompensation



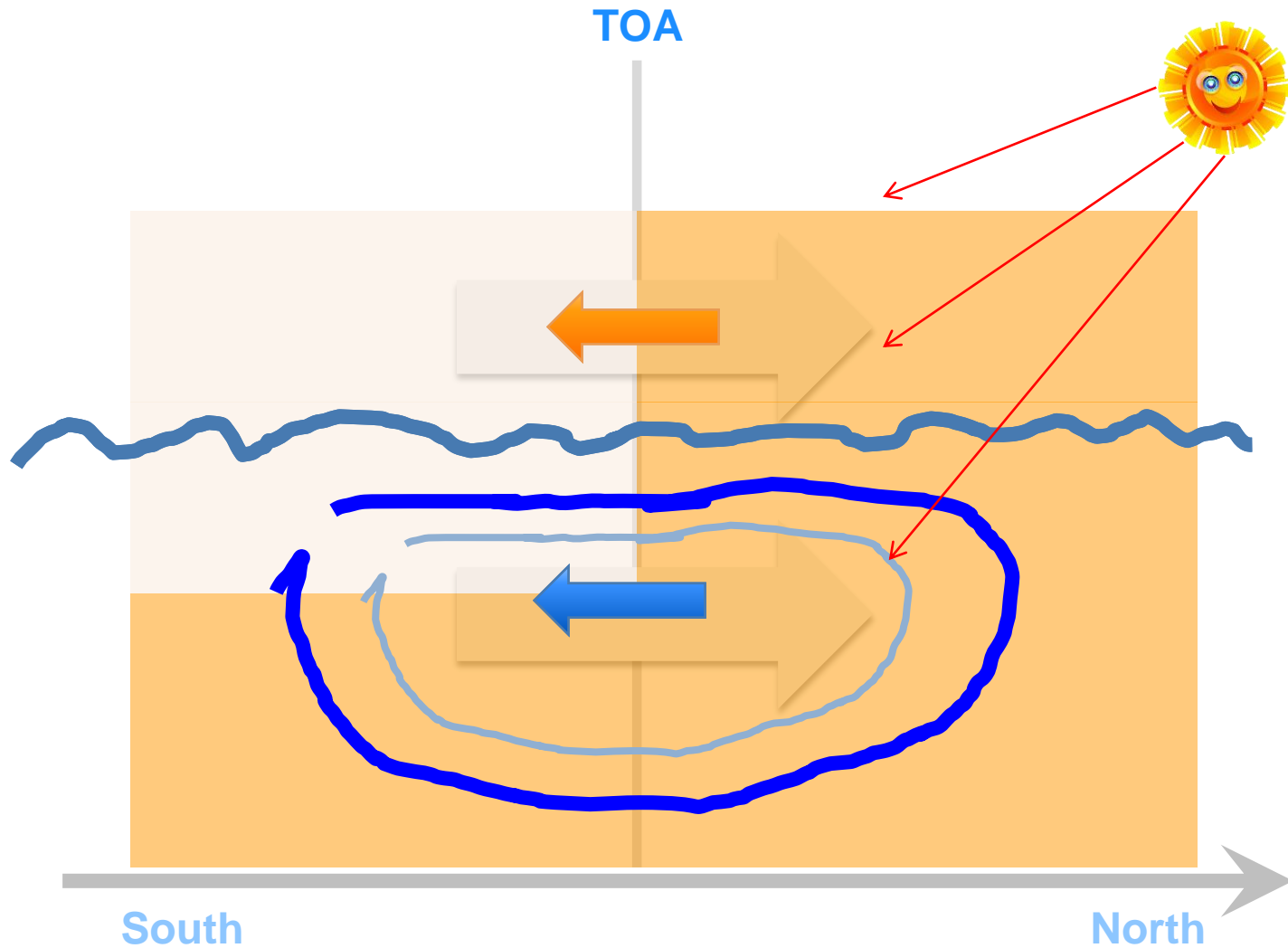
# Mechanism for Full compensation



# Mechanism for Overcompensation



# Will BJC Occur under Heating?





# Analytical Solution: BJC Rate under Heating

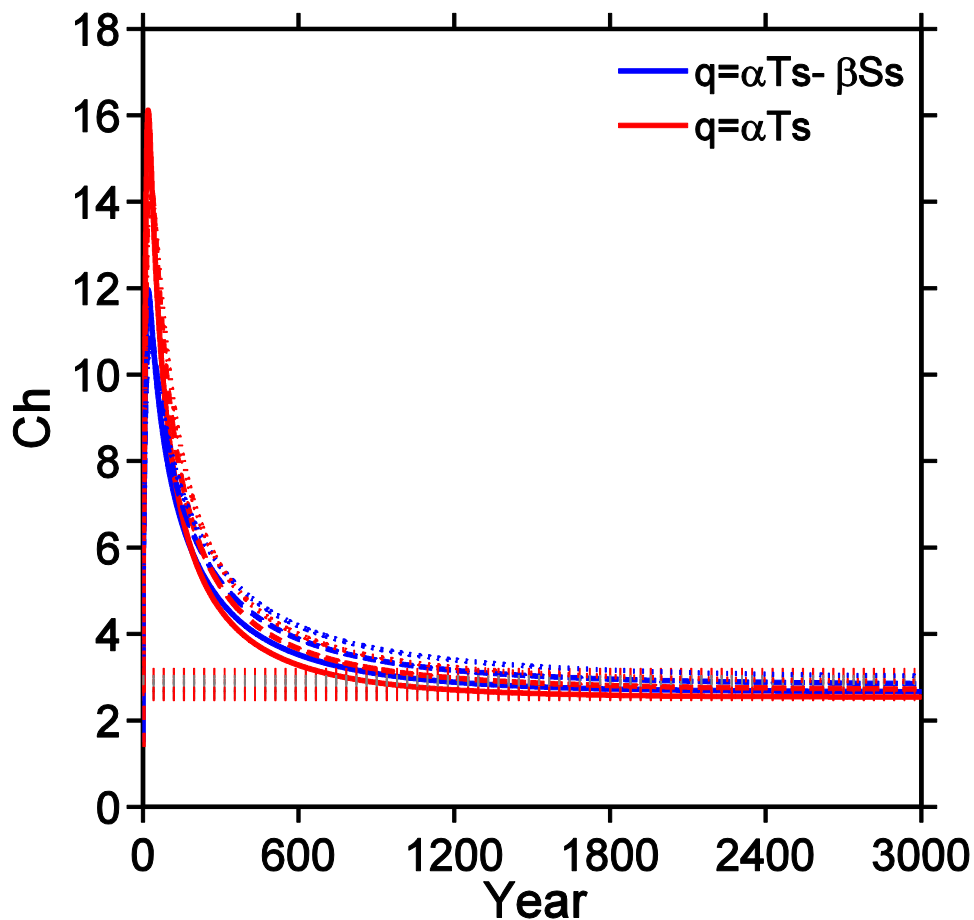
$$C_h \equiv \Delta H_a / \Delta H_o = \left\{ 1 / [1 + (B_2 - B_1) \Delta A / \Delta T_s [B_1 B_2 + (B_1 + B_2) \chi]] \right\} C_R$$

if  $B_1 = B_2$  global uniform feedback

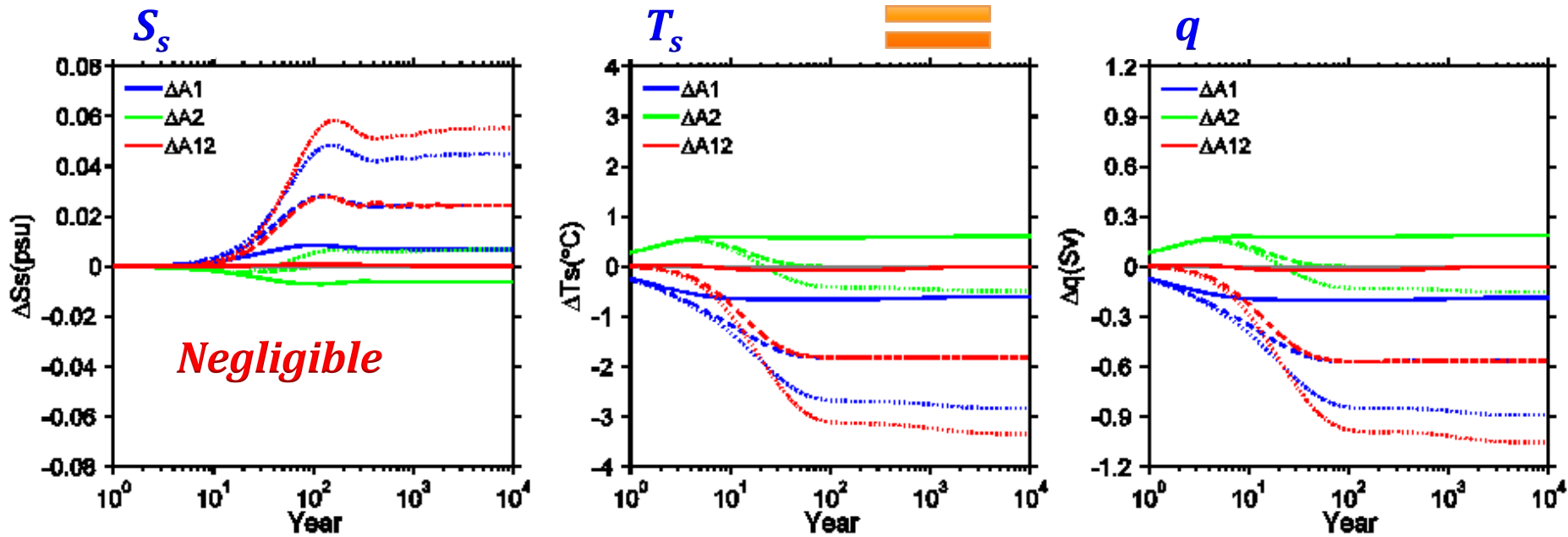
$$C_h = C_R < 0$$

# “BJC Rate” under Heating

No thermohaline dynamics → No Compensation!



# Why **No** BJC under Heating?



$$q \sim T_s \rightarrow O_d \sim q * T_s \sim T_s * T_s$$

# Why **No** BJC under Heating?

$$q \sim T_s \rightarrow O_d \sim q * T_s \sim T_s * T_s$$



$$C_q \equiv \Delta H_a / \Delta H_o = H_a / 2H_o$$



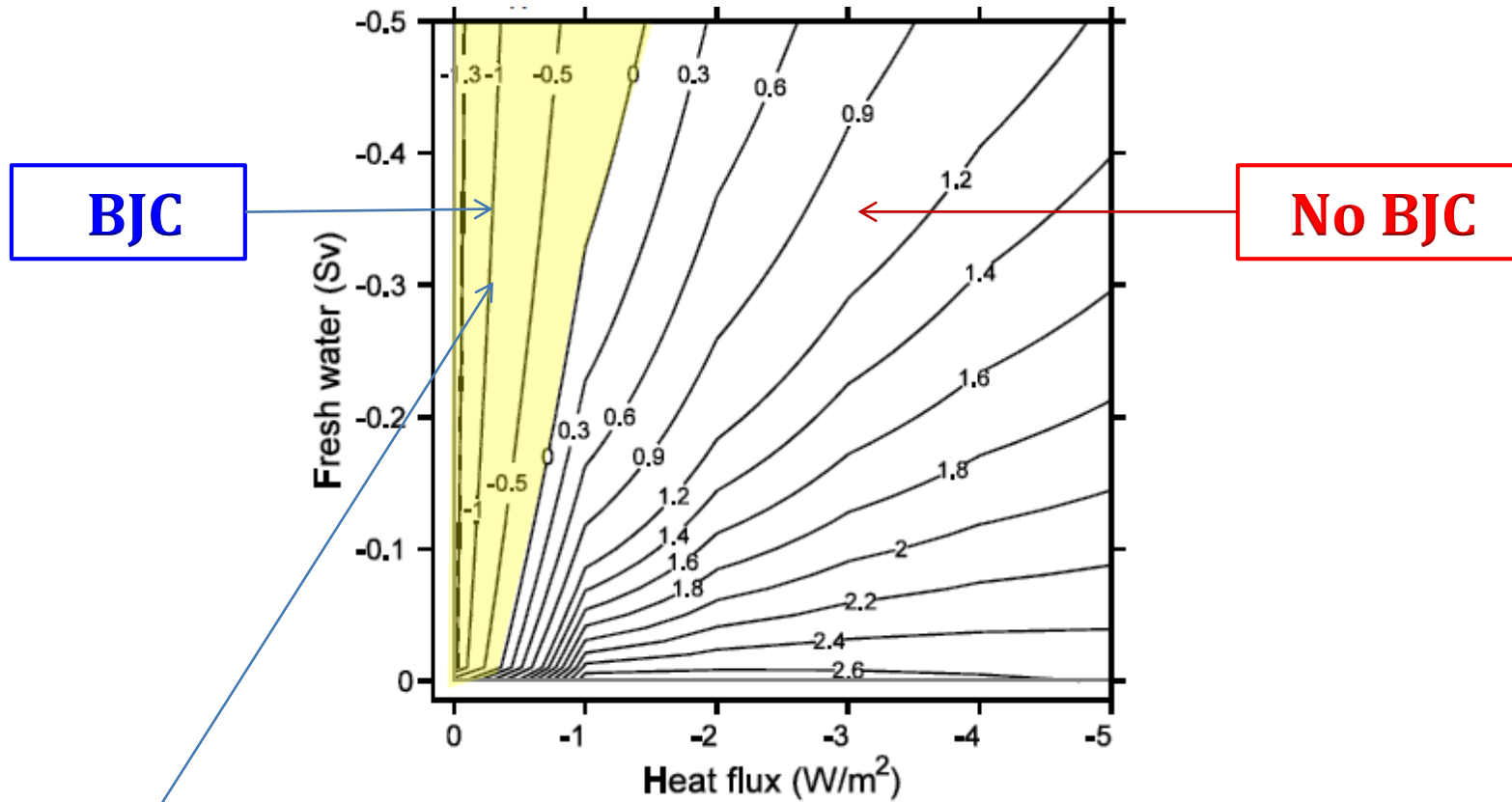
**No Compensation!  $C_q > 0$  &  $C_q \sim \text{Constant}$**



**No thermohaline dynamics**

# BJC Possible under Freshwater + Heating?

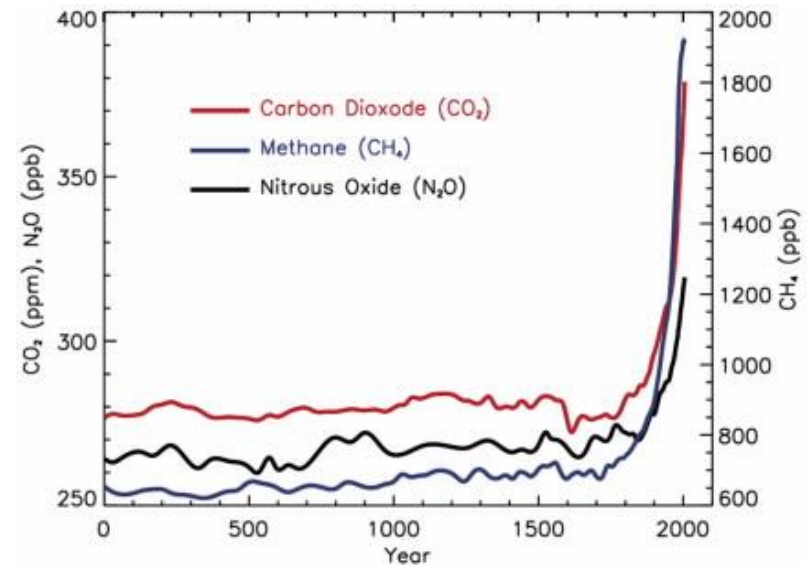
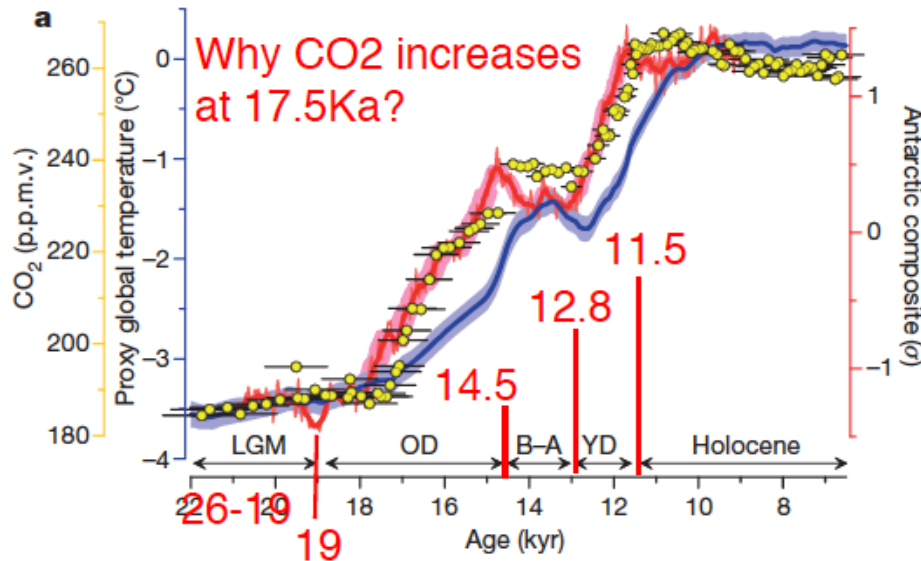
Valid for weak heating



Positive Feedback:  $S1 \uparrow \rightarrow THC \uparrow \rightarrow S1 \uparrow \rightarrow THC \uparrow \rightarrow T_s \downarrow$

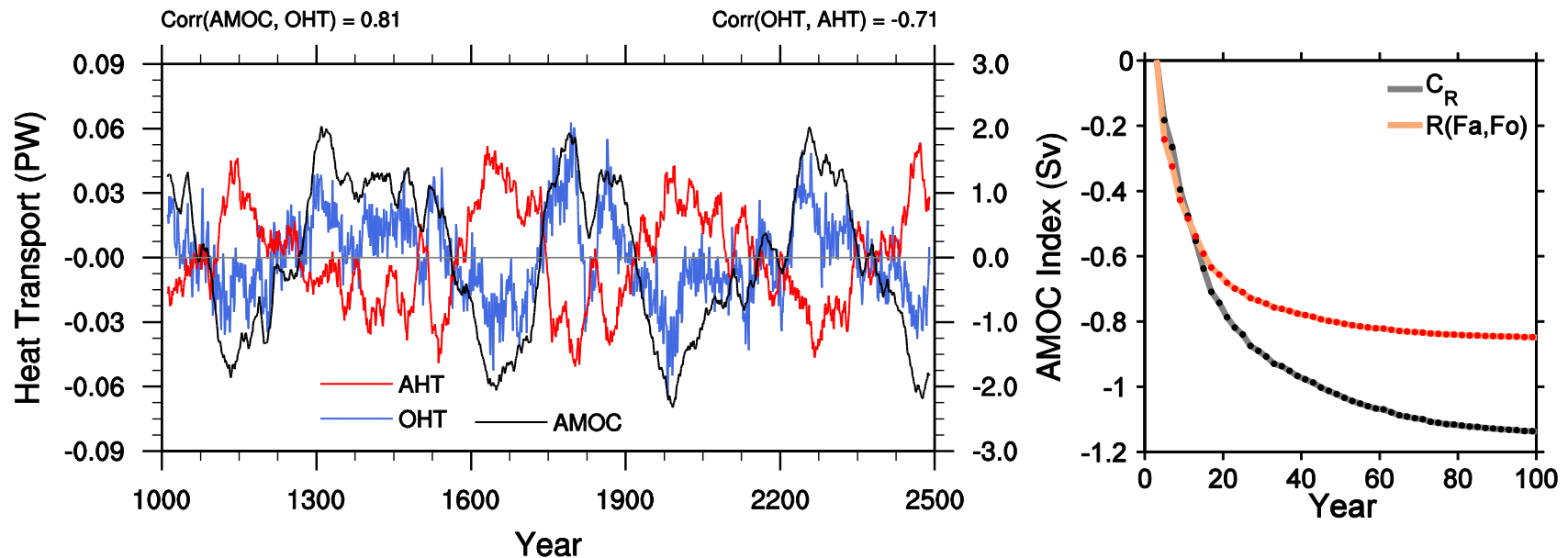
# CO2 since the LGM

Since LGM:  $1.5 \times 10^{-4} \text{ W/m}^2/\text{year}$  (Shakun et al., 2012)



Since 1770:  $1 \times 10^{-2} \text{ W/m}^2/\text{year}$  (IPCC, 2007)

# Climate Variability and BJC in CESM



Define:

$$C_R \equiv r \frac{\sigma_{F_a}}{\sigma_{F_o}} \quad (1)$$

# Theory for **Transient** Climate Variability

$$\begin{aligned}\dot{T}_s &= \frac{1}{\epsilon c \rho_0 D_1} [(A_2 - A_1 - BT_s) - 2\chi T_s] - 2qT_s, \\ \dot{S}_s &= \frac{2S_0}{\epsilon_w D_1} \gamma T_s - 2qS_s + h_{fw}.\end{aligned}$$



Linearization:  $T = \bar{T} + T'$  and  $S = \bar{S} + S'$

$$\frac{\partial}{\partial t} \begin{pmatrix} T'_s \\ S'_s \end{pmatrix} = M \begin{pmatrix} T'_s \\ S'_s \end{pmatrix} + \begin{pmatrix} 0 \\ h_0 e^{i\omega t} \end{pmatrix}$$

If  $h_{fw} = \text{const.} \rightarrow C_{R0} = -\frac{1}{1+B/2\chi} \quad (2)$



# BJC for Climate Variability

Zhao, Yang and Liu, 2016: Assessing Bjerknes compensation for climate variability and its timescale dependence. *J. Climate*

$$C_{Rp} \equiv \frac{F'_a}{F'_o} = \text{Re}(C_{R0}e^{i\delta}) = r_\delta * C_{R\omega}$$

$$r_\delta \equiv \cos\delta = -\frac{F}{\sqrt{\omega^2 + F^2}}$$

$$C_{R\omega} = \frac{2\chi}{\epsilon c \rho_0 D_1 \sqrt{\omega^2 + F^2}}$$

=

$$C_R \equiv r \frac{\sigma_{F_a}}{\sigma_{F_o}}$$



$\omega \rightarrow 0$   
→

$$C_{R0} = -\frac{1}{1 + B/2\chi}$$

# BJC for Climate Variability

$$\omega \rightarrow \infty \Rightarrow r_{\delta} \rightarrow \mathbf{0}; C_{R0} \rightarrow \mathbf{0}; C_{Rp} \rightarrow \mathbf{0}$$

No correlation and No BJC

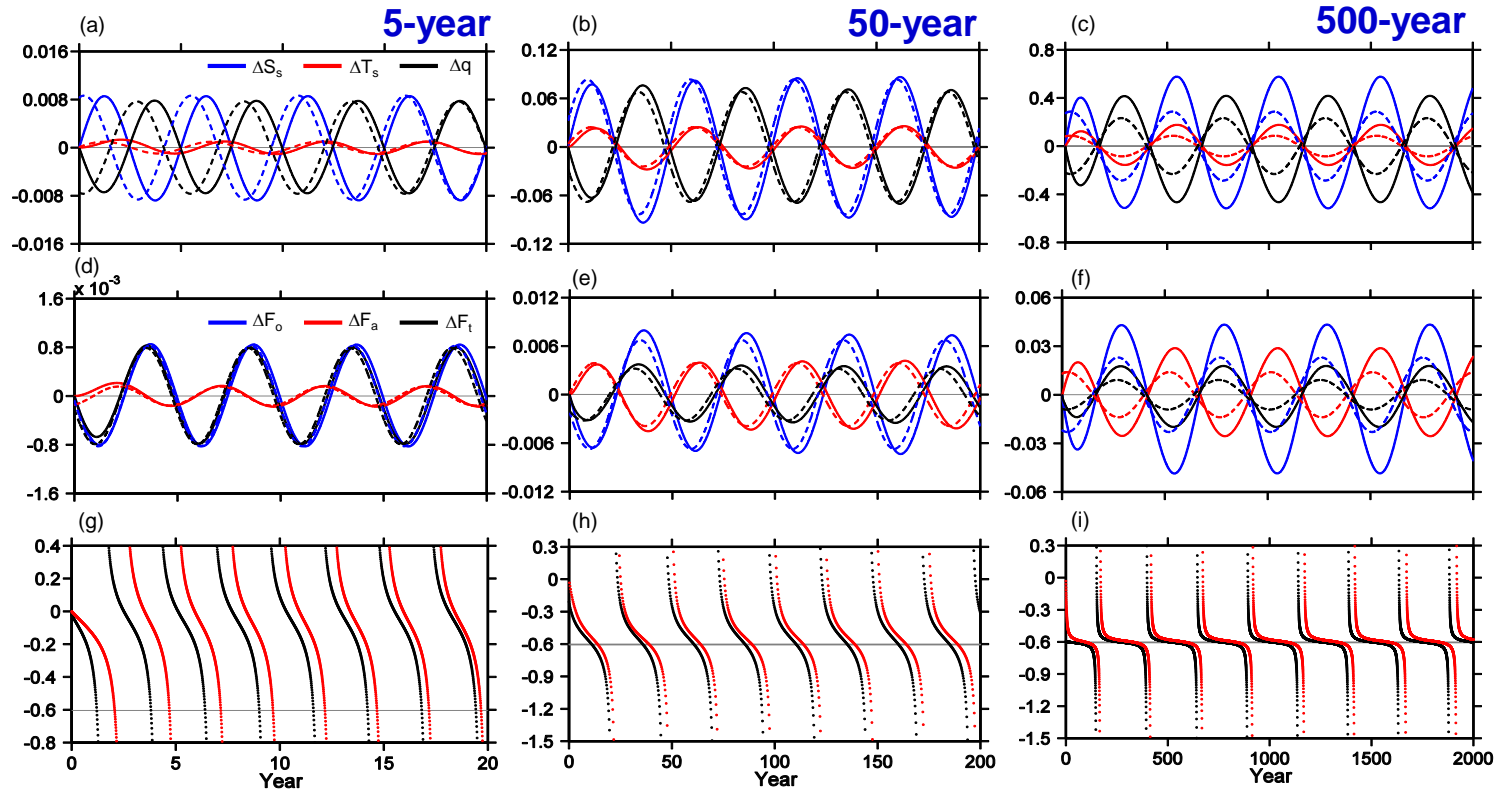
$$\omega \rightarrow \mathbf{0} \Rightarrow r_{\delta} \rightarrow \mathbf{-1}; C_R(\mathbf{1}) \approx C_{R0}(\mathbf{2}) \approx C_{Rp}(\mathbf{3})$$

Full correlation and equilibrium BJC

Go to Climate Variability Validation

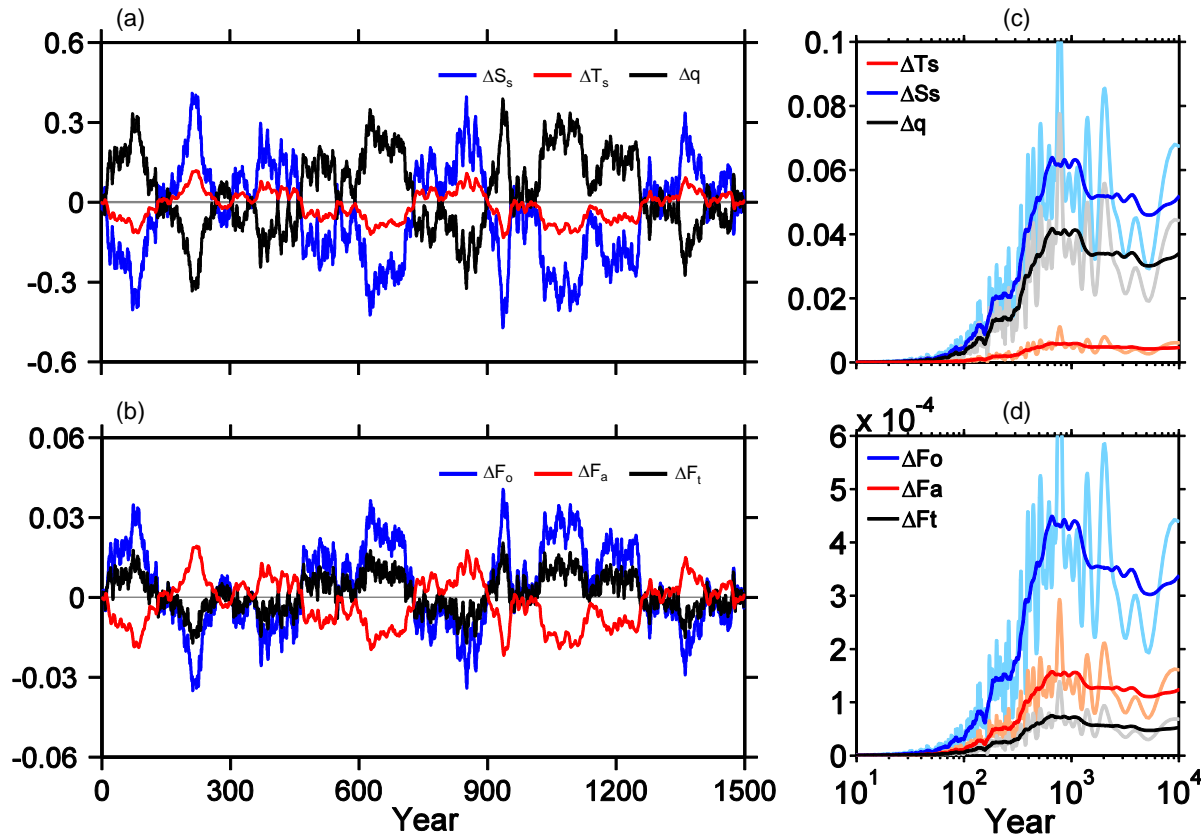
# BJC for Climate Variability

Under periodic forcing:  $h_{fw} = \text{Re}(h_0 e^{i\omega t})$

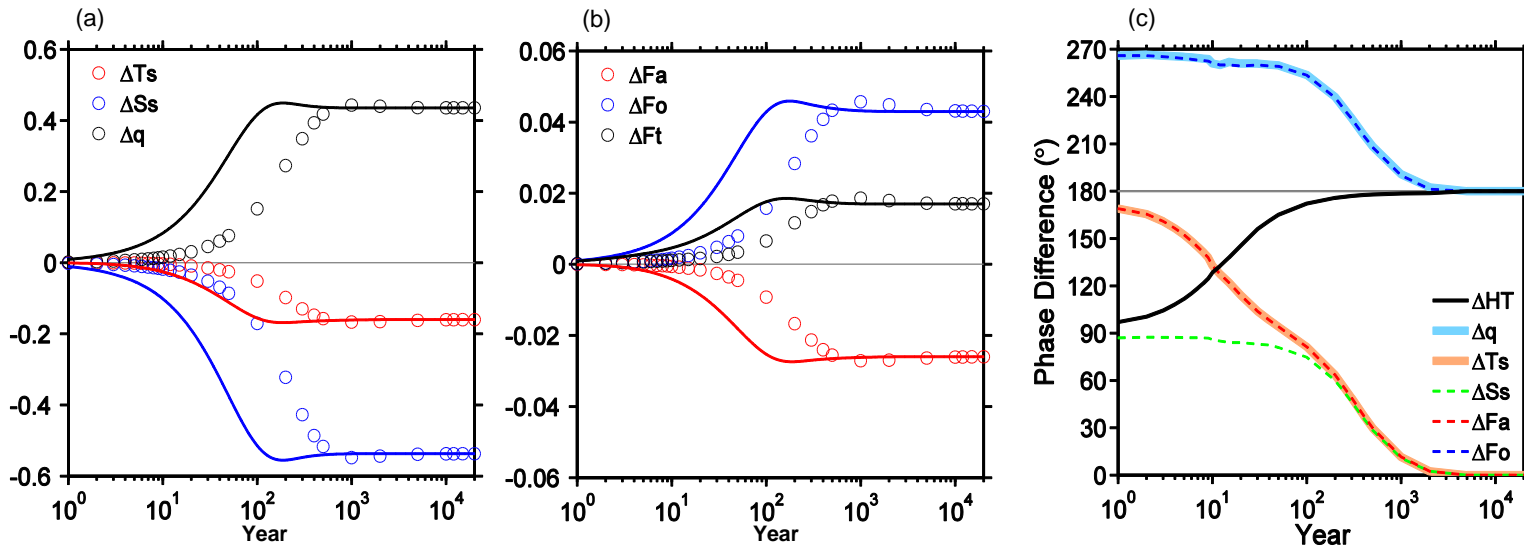


# BJC for Climate Variability

Under stochastic forcing:  $h_{f\omega} = h_0 \int_{\omega=0}^{\omega=\infty} e^{i\omega t} d\omega$

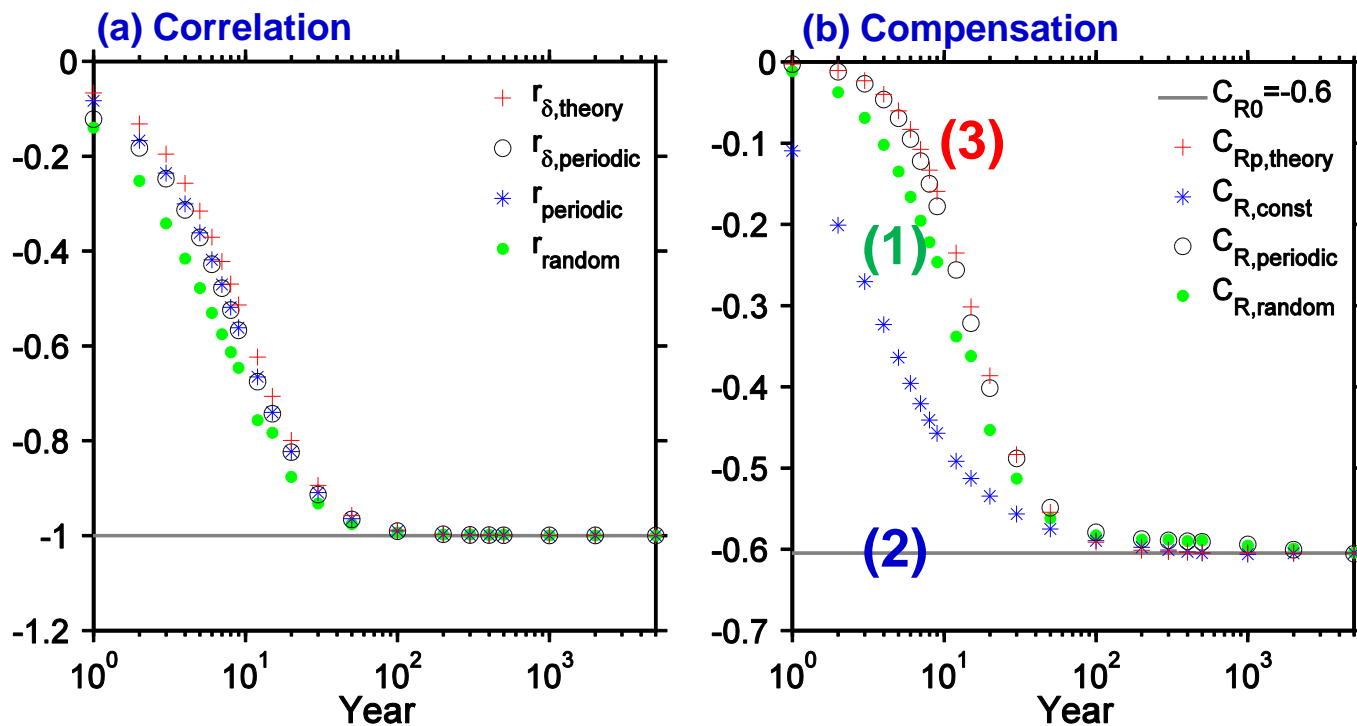


# BJC for Climate Variability



Forcing frequency  $\omega \rightarrow 0 \Rightarrow$  Equilibrium solution

# BJC Theory **Valid** for Climate Variability



Beyond *decadal* timescale, AHT and OHT out of phase, BJC established

# Outline

- **Fundamentals**
- **Questions**
- **Hypothesis and Theory**
- **CGCM results**
- **Aquaplanet**
- **Summary**

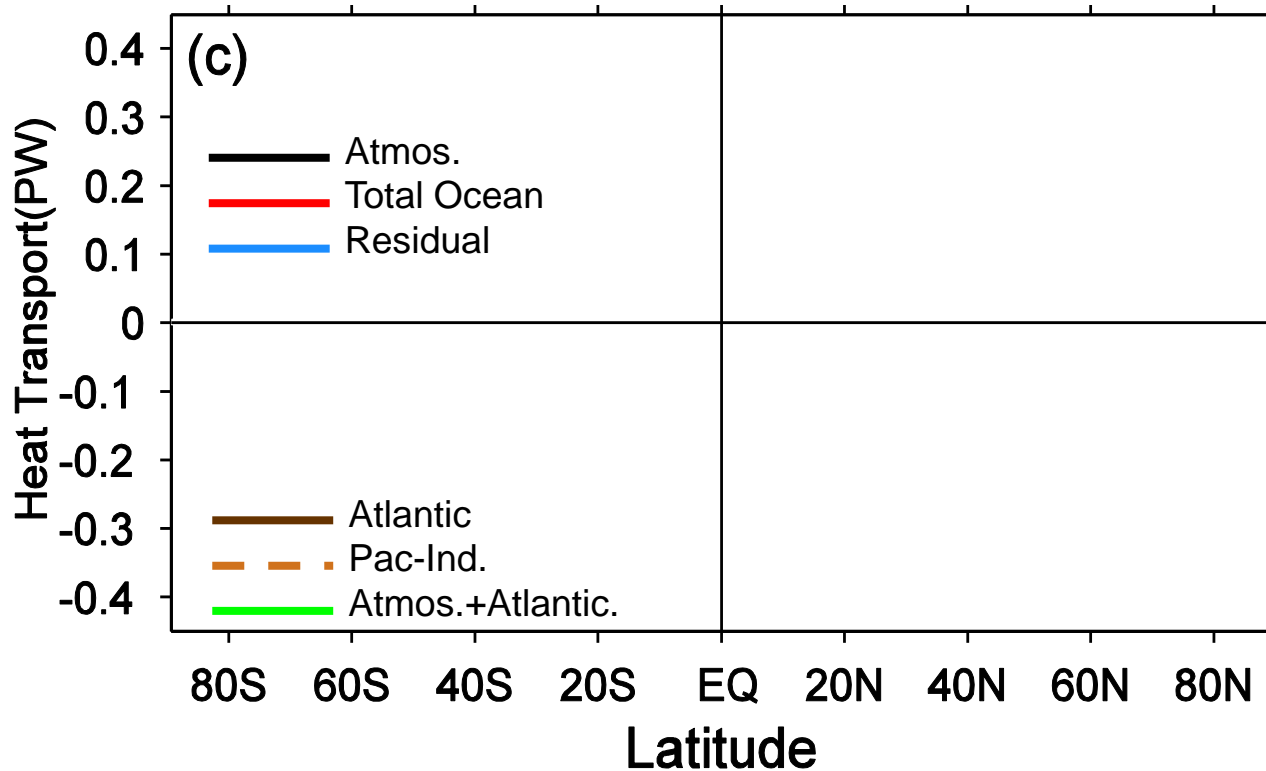
# CESM Experiment and Mechanism

- ◇ **Fresh-water experiments**
- ◇ **Wind-perturbation experiments**
- ◇ **Global warming experiments**
- ◇ **Internal variability from a long control run**

Yang and Dai (2015), Yang et al. (2013, 2016, 2017)



# BJC under **Freshwater** in CESM

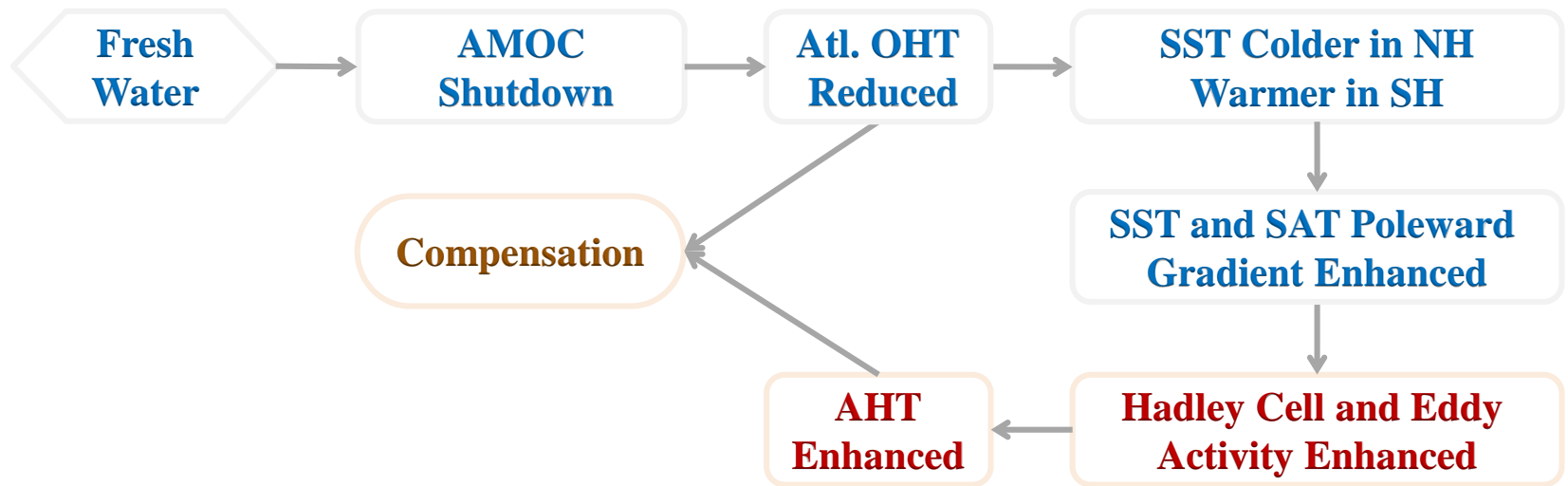


**80-90%**

Atlantic OHT ↓ ⇒ AHT ↑ ⇒ Pac-Ind. OHT ↑

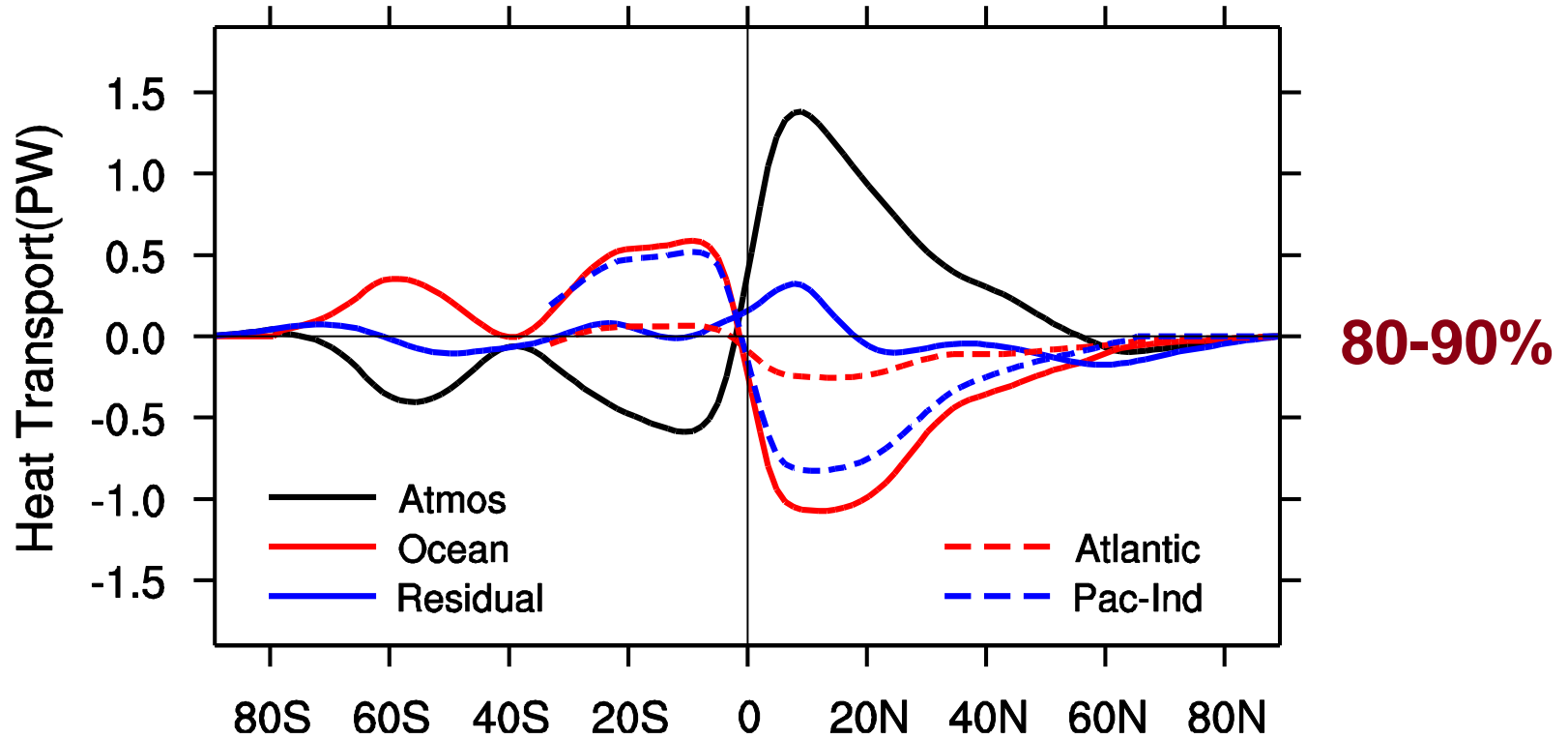
Atlantic OHT ≈ AHT; Pac-Ind. OHT ≈ Overcompensation

# “Mechanism”



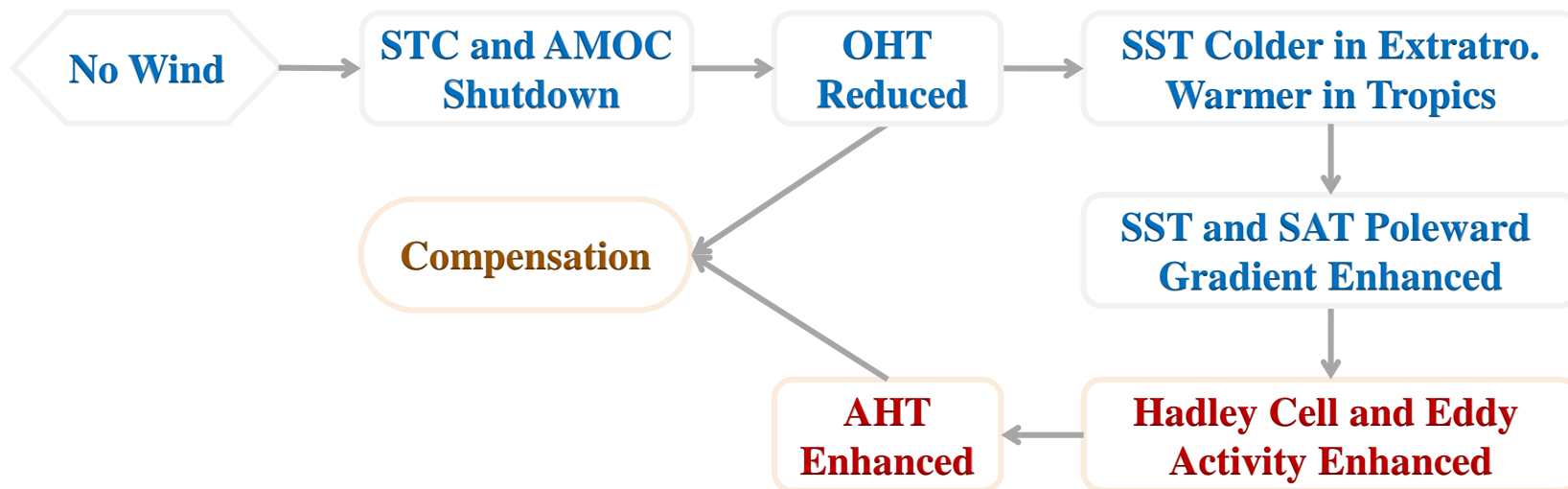
Yang et al. (2013, 2017)

# BJC under Wind Perturbation in CESM



Pacific-Indian OHT ↓ ⇒ Ty ↑ ⇒ HC ↑ ⇒ AHT ↑  
 Nearly Compensation

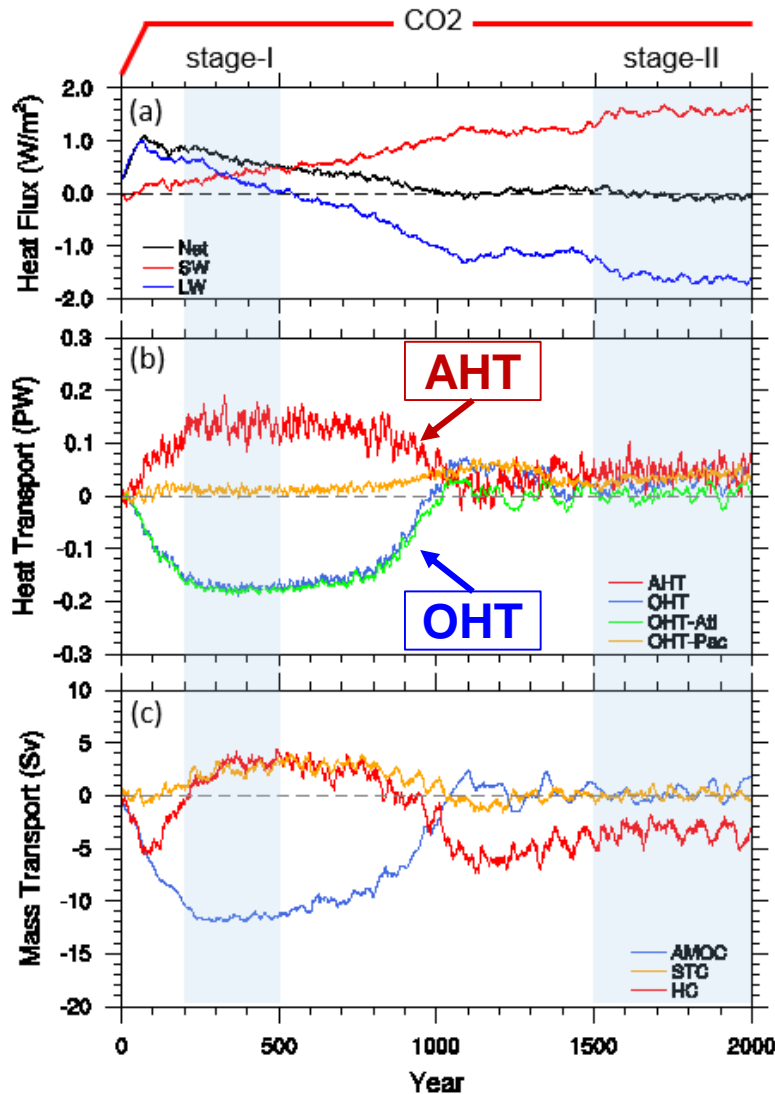
# “Mechanism”



Yang and Dai (2015), Dai et al. (2017)

# BJC under Global Warming in CESM

85%

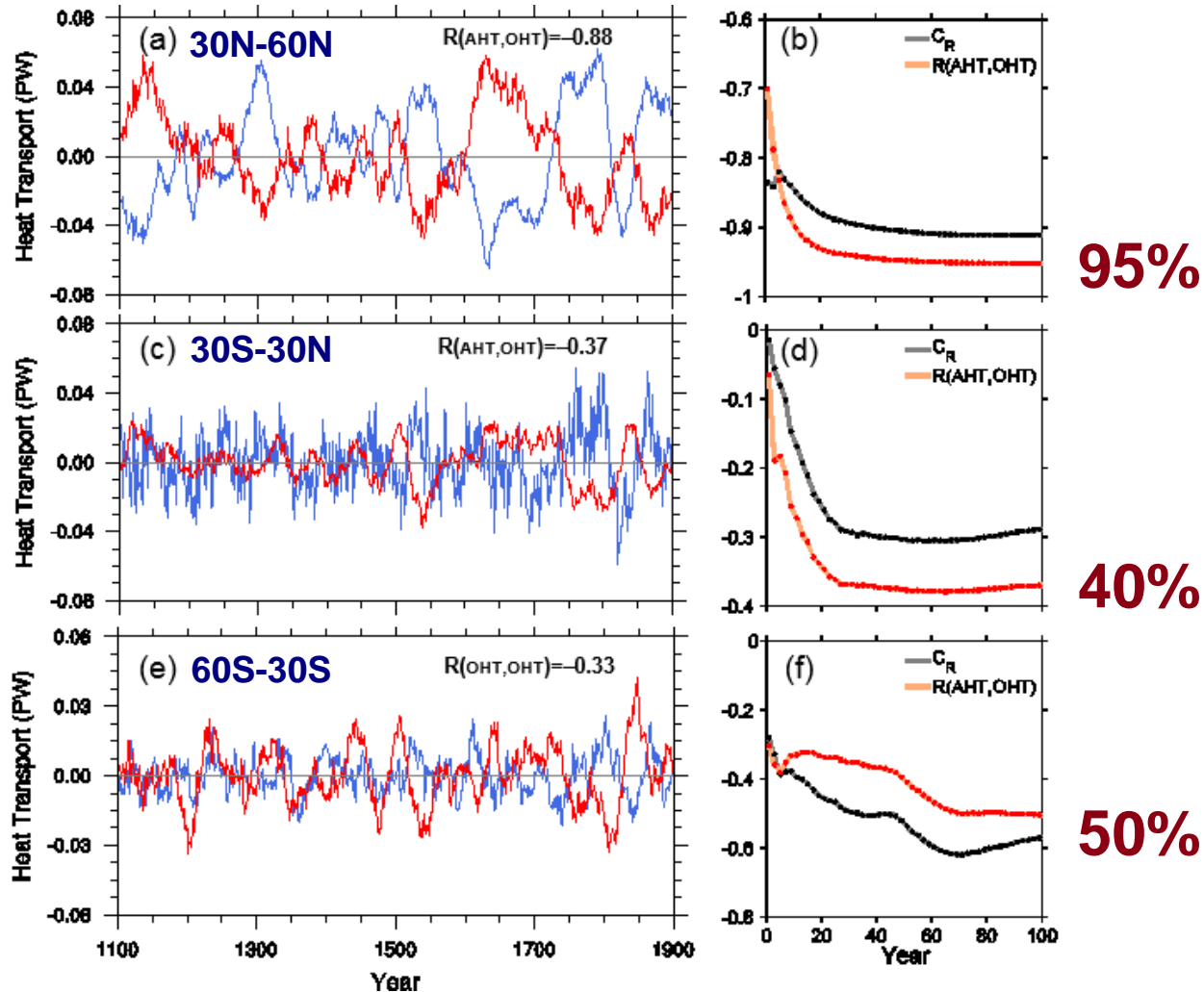


Under **2 X CO2** forcing  
BJC valid due to  
*thermohaline dynamics!*

Yang et al. (2017)

# BJC in Natural Variability in CESM

## 2000-year CESM control run

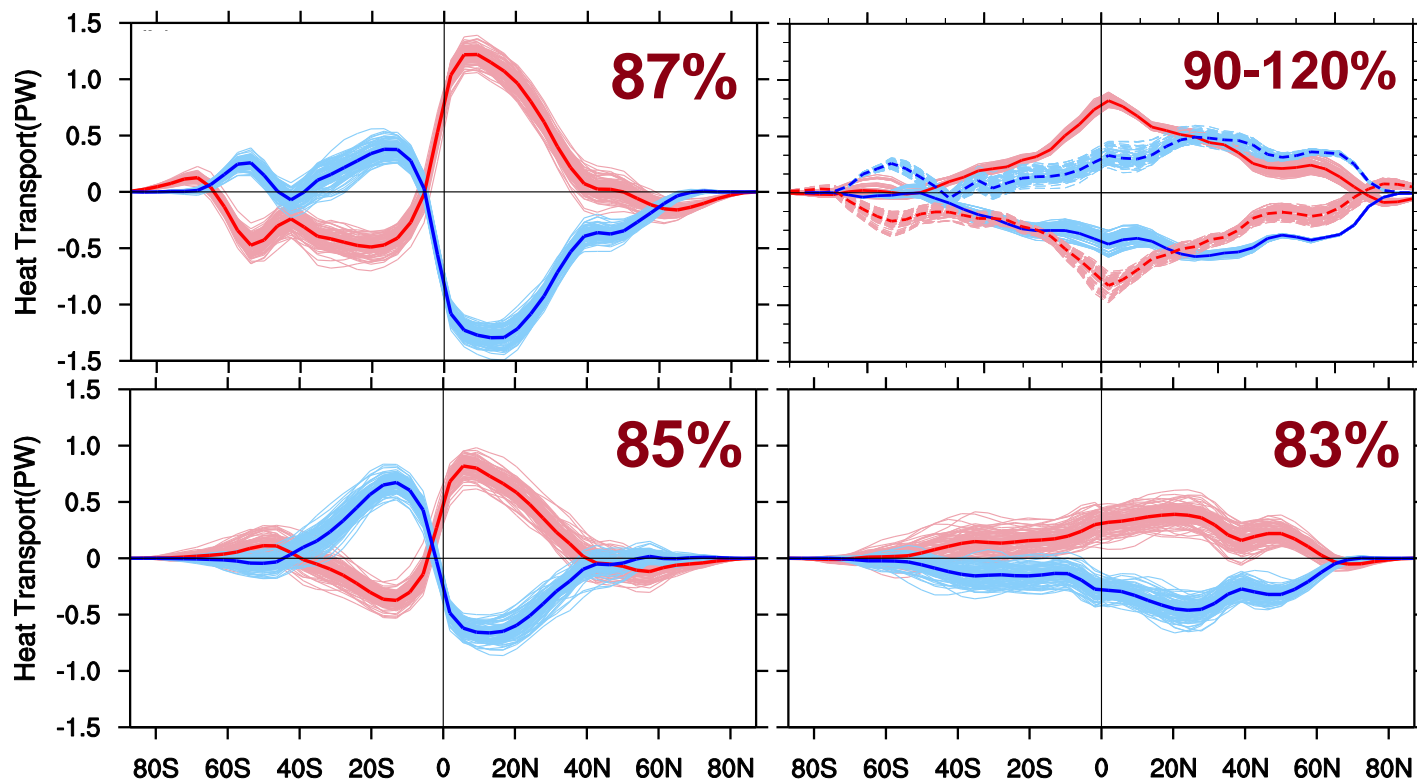


Zhao and Yang (2017)

复旦大学大气-海洋科学系, 2019.03.28, 上海

# Summary: BJC in CESM

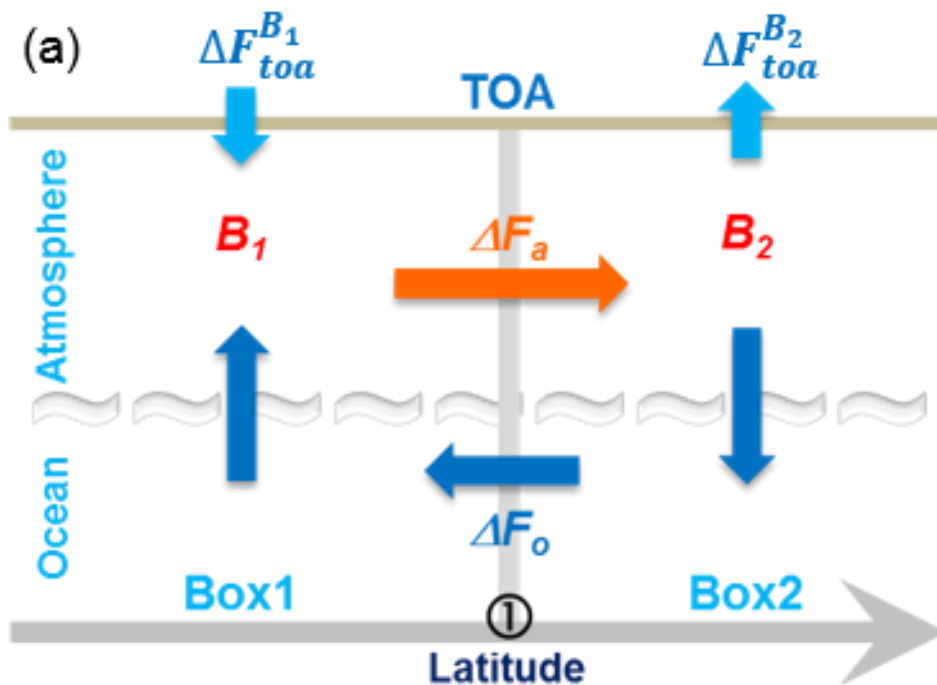
Surface Reason: *Out-of-phase* changes in Atmos-Ocean MOC → BJC



Yang and Dai (2015), Yang et al. (2013, 2016, 2017)

# BJC Mechanism

Fundamental Reason: Climate feedback + Energy constrain → BJC

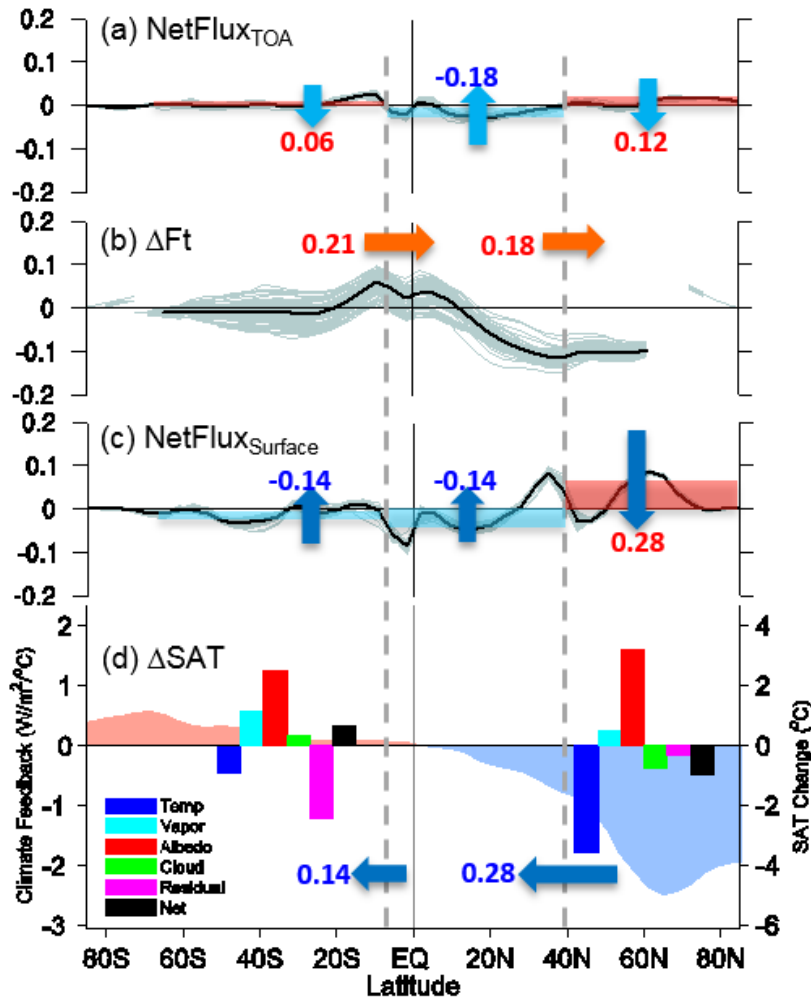


$$C_R = -(B_1 + B_2)\chi / [B_1 B_2 + (B_1 + B_2)\chi]$$



# BJC: *Theory* vs *CGCM*

## CESM Wind Perturbation experiments



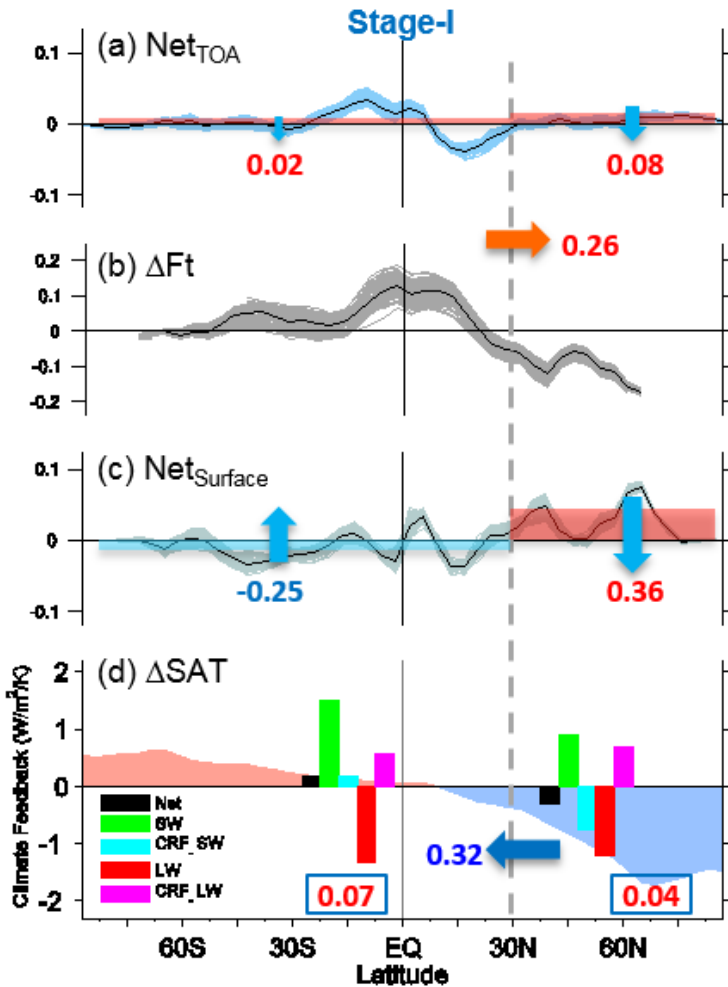
	Wind	Temp	Albedo	Cloud	$C_{Rmodel}$	$C_{Rtheory}$
0.1A	NH	-1.80	1.30	-0.23	-1.10	-1.09
	SH	-0.44	1.16	-0.07		
	Global	-2.20	1.34	-0.28	-0.83	-0.71
0.1P	NH	-1.87	1.30	0.34	-1.85	-1.61
	SH	-2.14	0.39	0.57		
	Global	-1.88	0.95	0.27	-0.85	-0.77
0.1G	NH	-1.84	1.05	-0.08	-0.95	-0.91
	SH	-1.70	1.96	-0.29		
	Global	-1.77	1.51	-0.18	-0.87	-0.81

$$C_{Rmodel} \approx C_{Rtheory}$$

Dai et al. (2017)

# BJC: *Theory* vs *CGCM*

## CESM Freshwater experiments



Freshwater		Global	SH	NH	90°S-30°N	30°N-90°N
Stage-I	Net CF	-0.63	0.89	0.08	0.18	-0.30
	$C_{Rmodel}$	-0.97	-1.36		-0.88	
	$C_{Rtheory}$	-0.83	-1.05		-1.43	
Stage-II	Net CF	1.96	0.66	0.35	0.16	-0.28
	$C_{Rmodel}$	-1.11	-1.90		-0.90	
	$C_{Rtheory}$	-2.88	-1.18		-1.33	

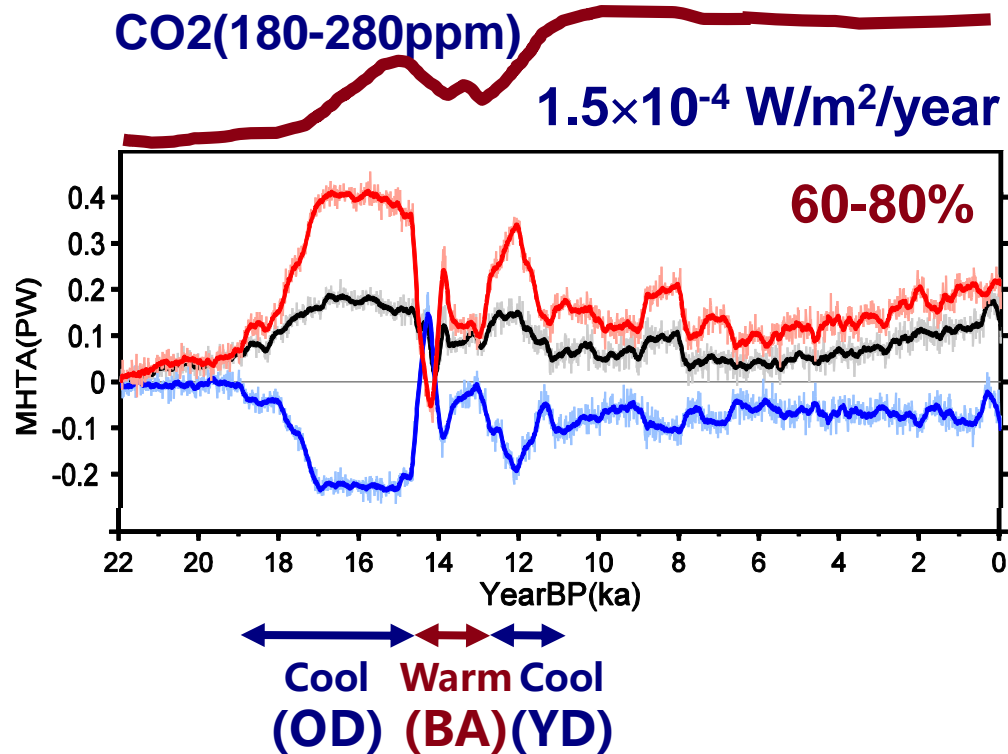
$$C_{Rmodel} \approx C_{Rtheory}$$

Yang et al. (2017)

# BJC: Coupled *Intrinsic* Mode

## 3. Relationship between OHT and AHT Changes? **Answered!**

*All-in-One* Simulation since LGM



BJC helps to maintain overall Earth climate stability

Yang et al. (2015), Sci. Rep.

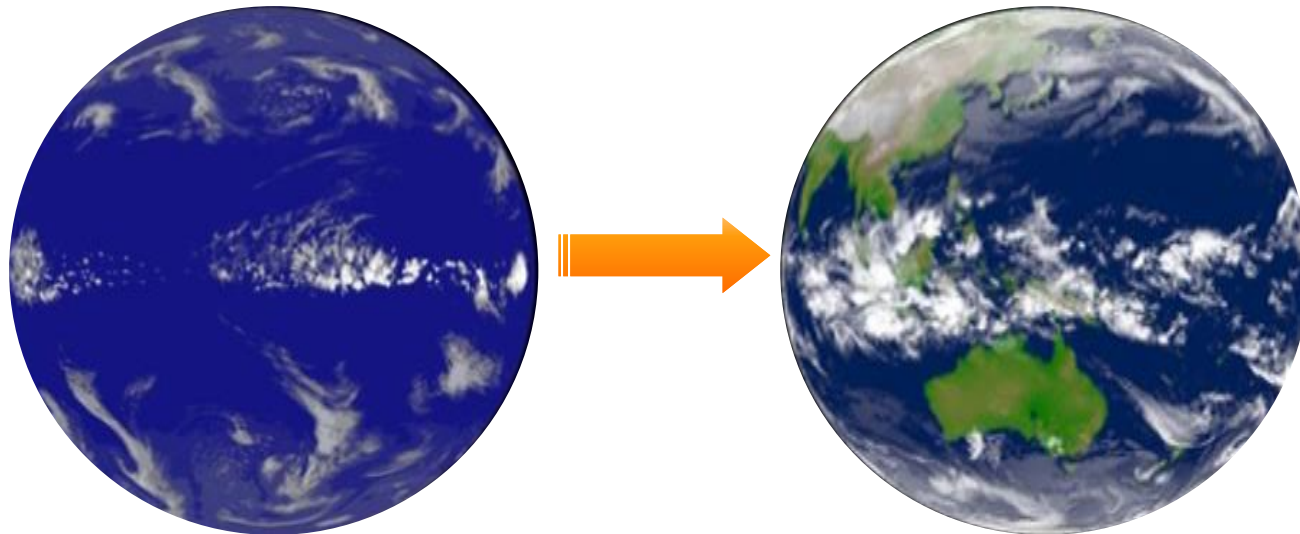
复旦大学大气-海洋科学系, 2019.03.28, 上海

# Outline

- **Fundamentals**
- **Questions**
- **Hypothesis and Theory**
- **CGCM results**
- **Aquaplanet**
- **Summary**

# Aquaplanet → Real Earth

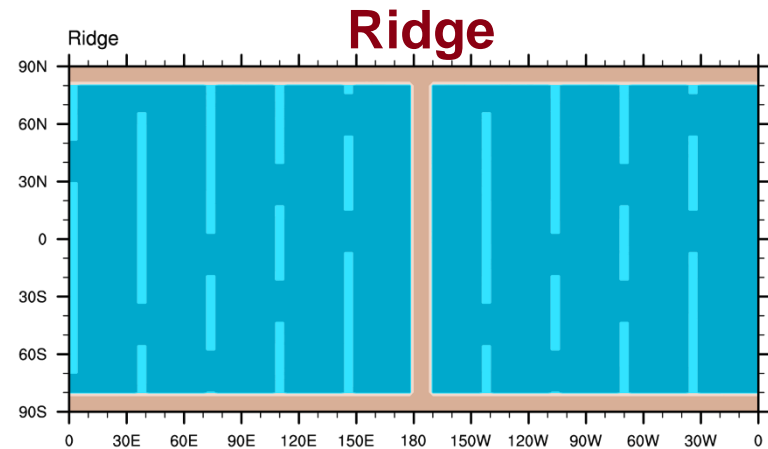
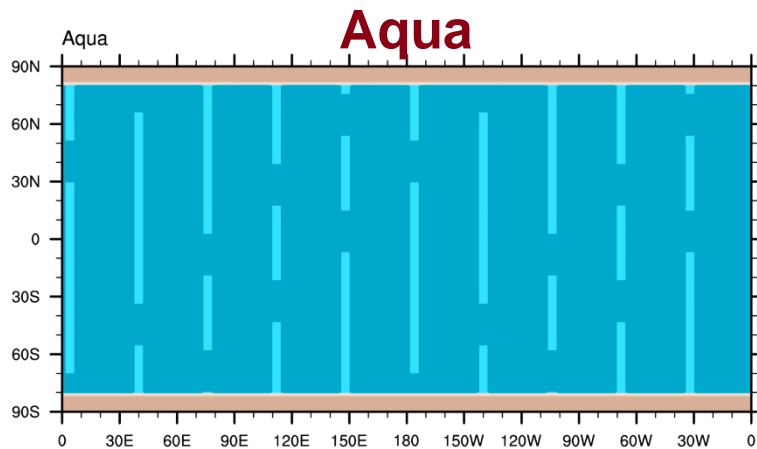
## Why anti-symmetric MHT?



Try to answer this fundamental question

# Topo for Aqua and Ridge

Land: 10 m; Ocean: 5000 m; Bottom random ridge: 500 m

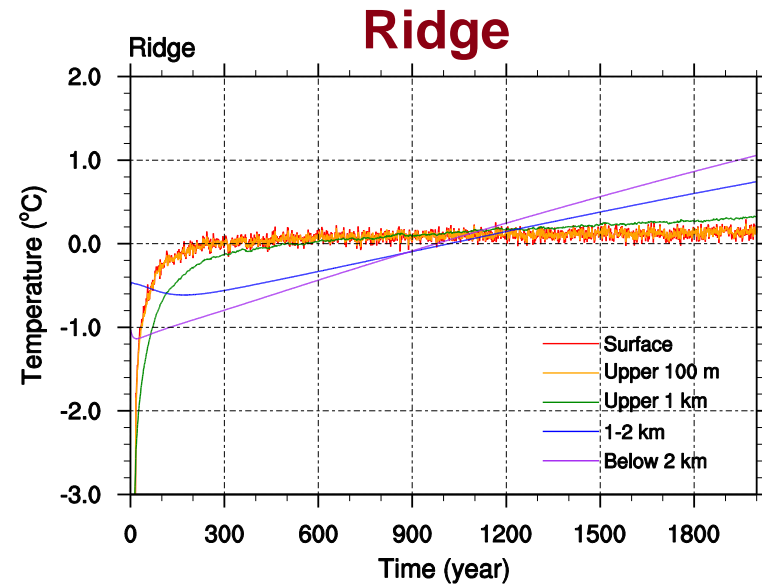
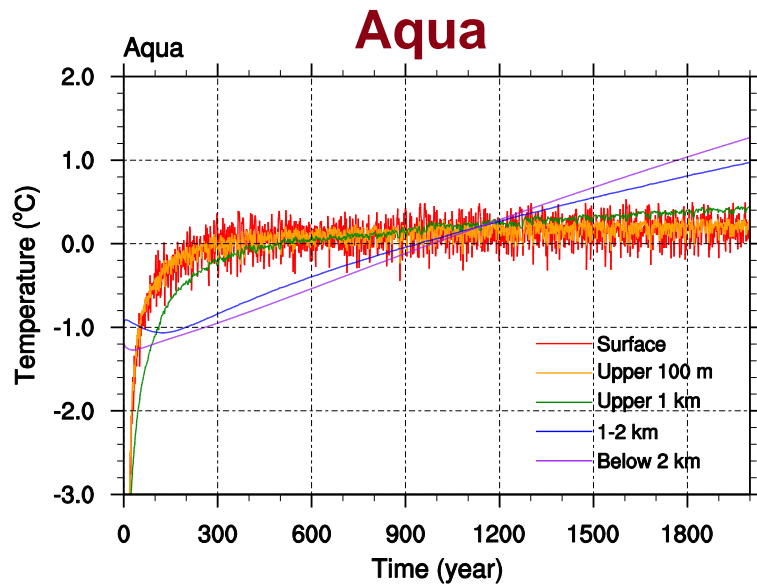


Li and Yang (2018)

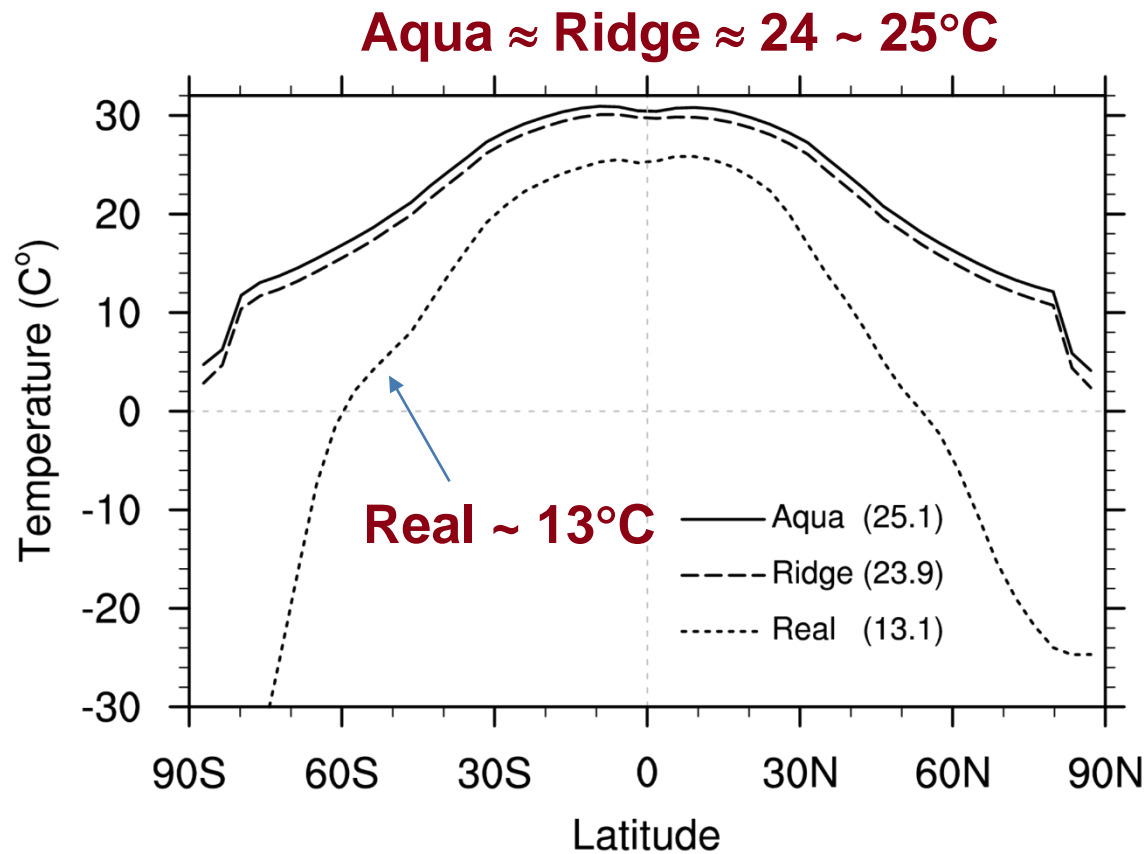
[Go to Summary](#)

# Hard to Reach Equilibrium

## 2000-year Simulation using CESM

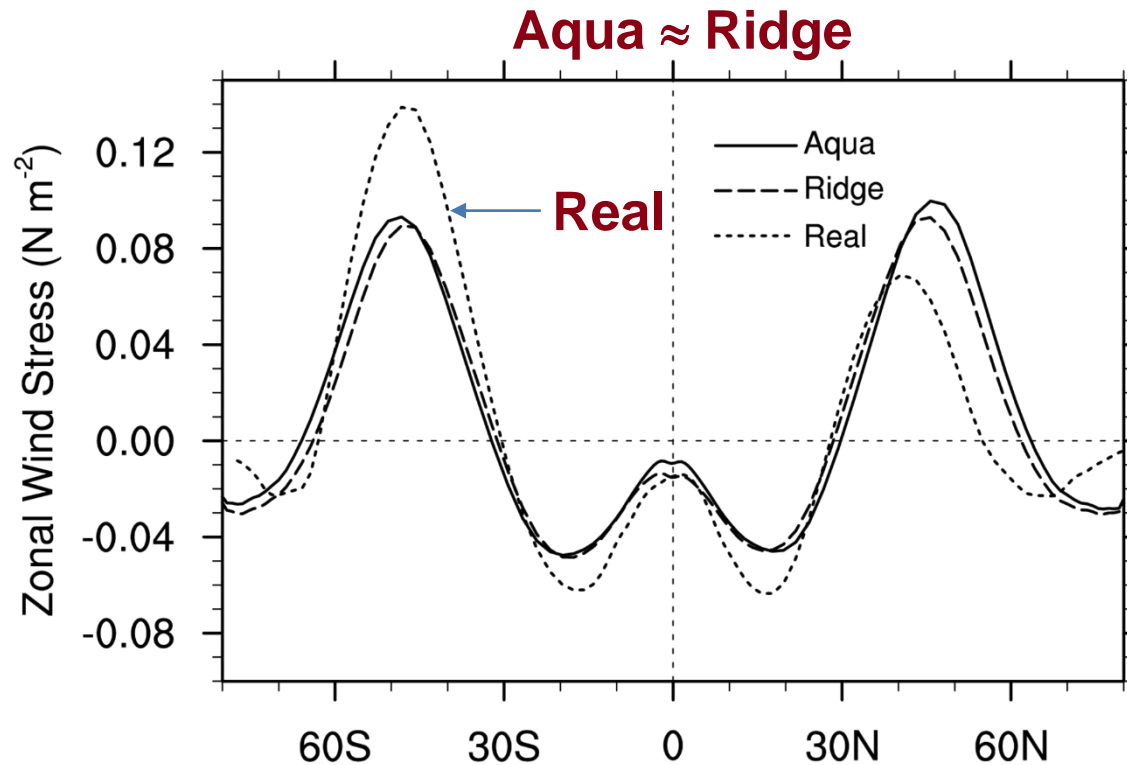


# SAT: Warmer Climate



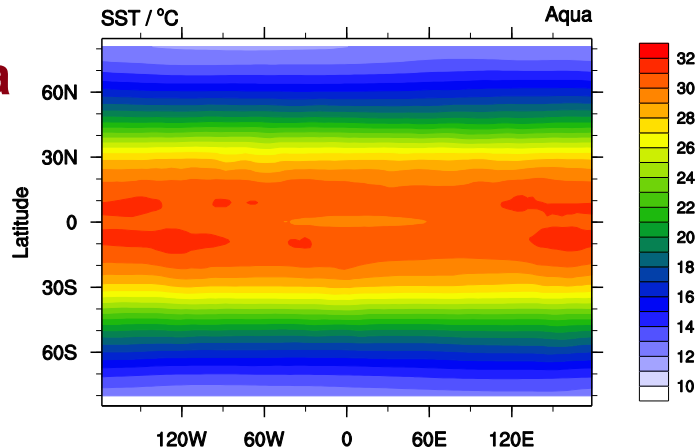


# Symmetric Zonal Surface Wind Stress

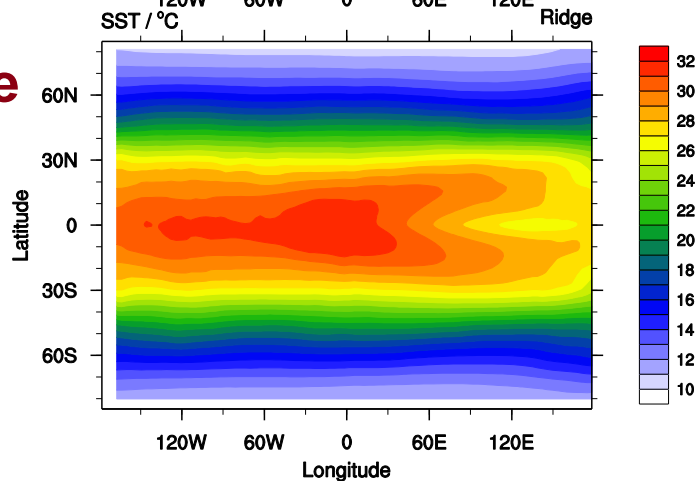


# Symmetric SST and Hadley Cell

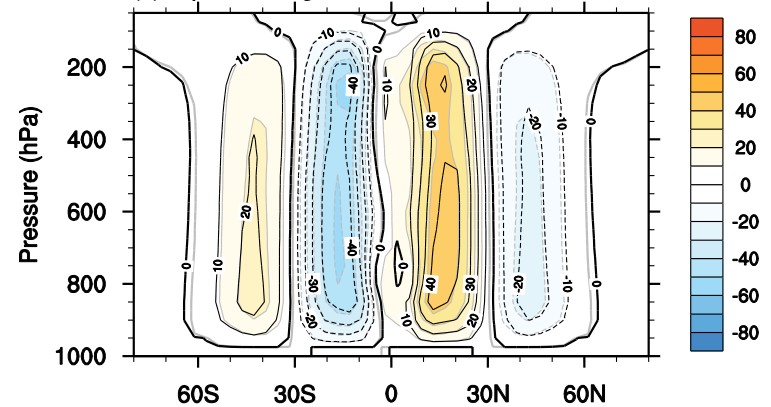
Aqua



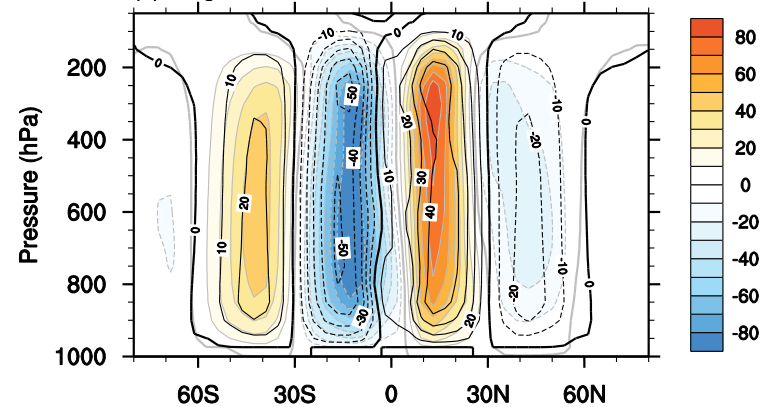
Ridge



(a) Aqua vs. Ridge



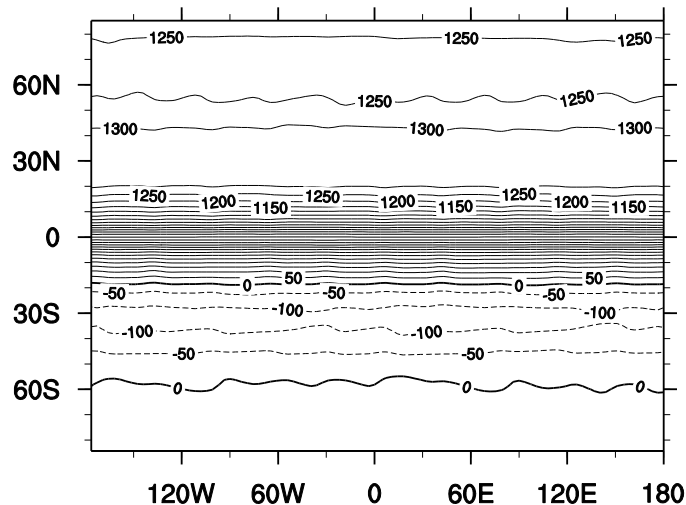
(b) Ridge vs. Real



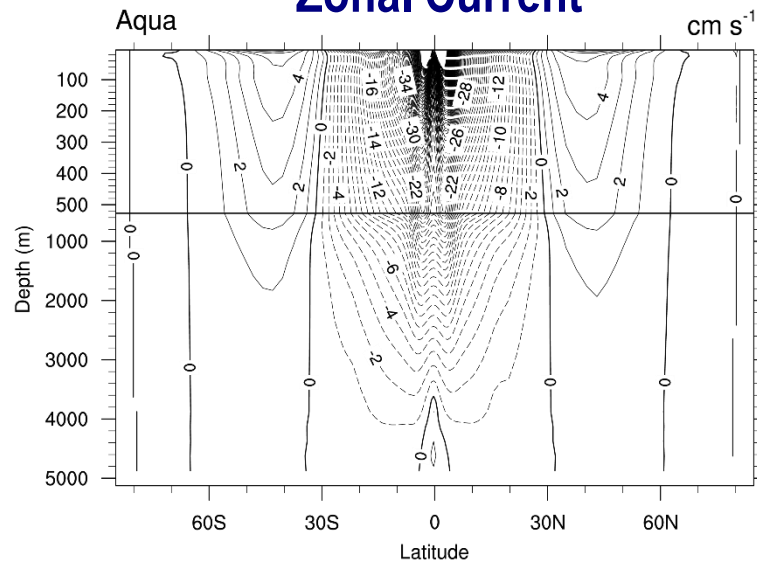
# Symmetric Ocean Circulation

Aqua

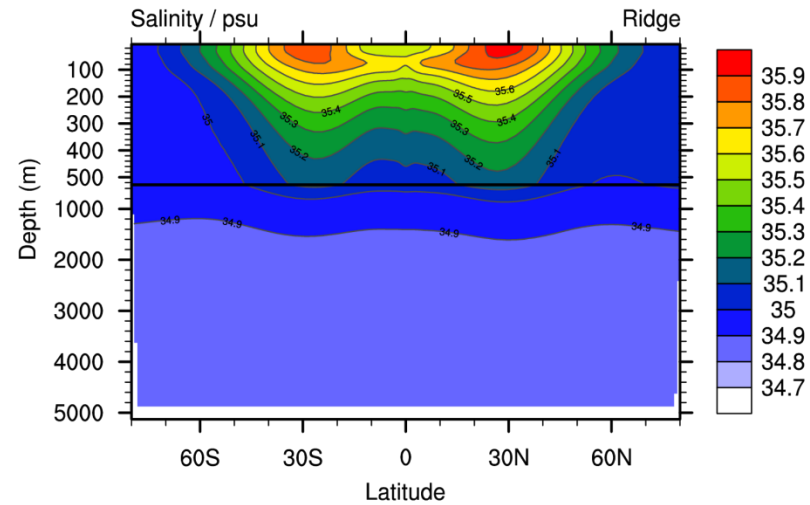
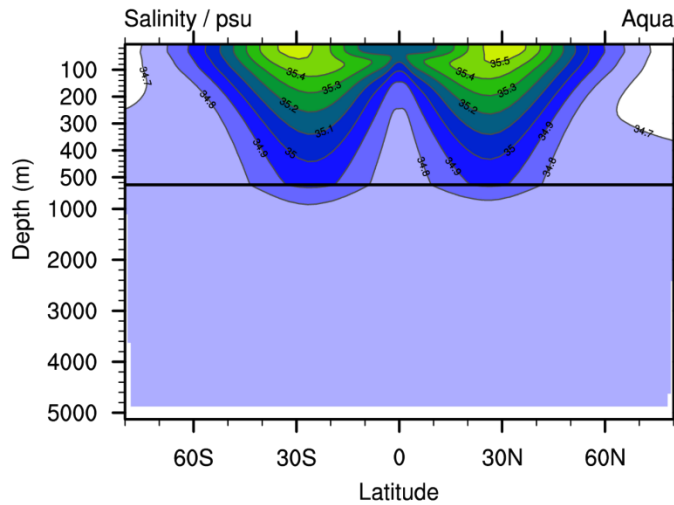
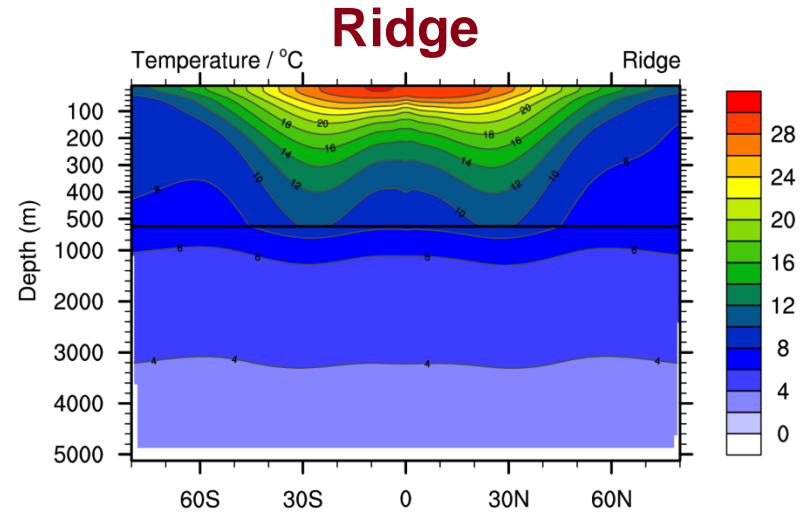
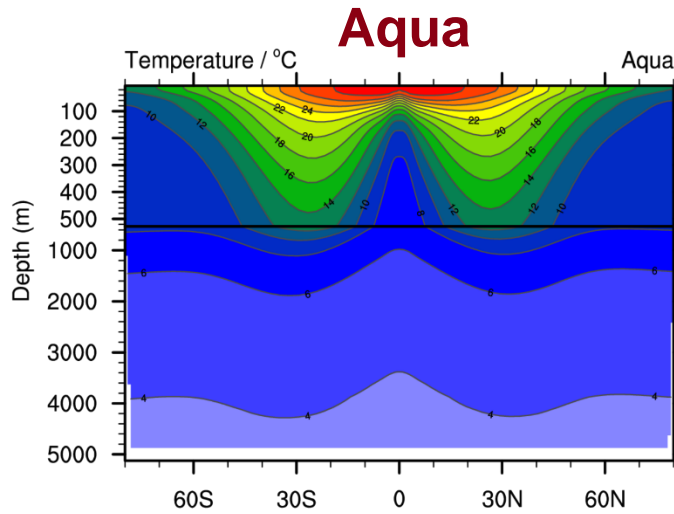
## Barotropic Streamfunction



## Zonal Current

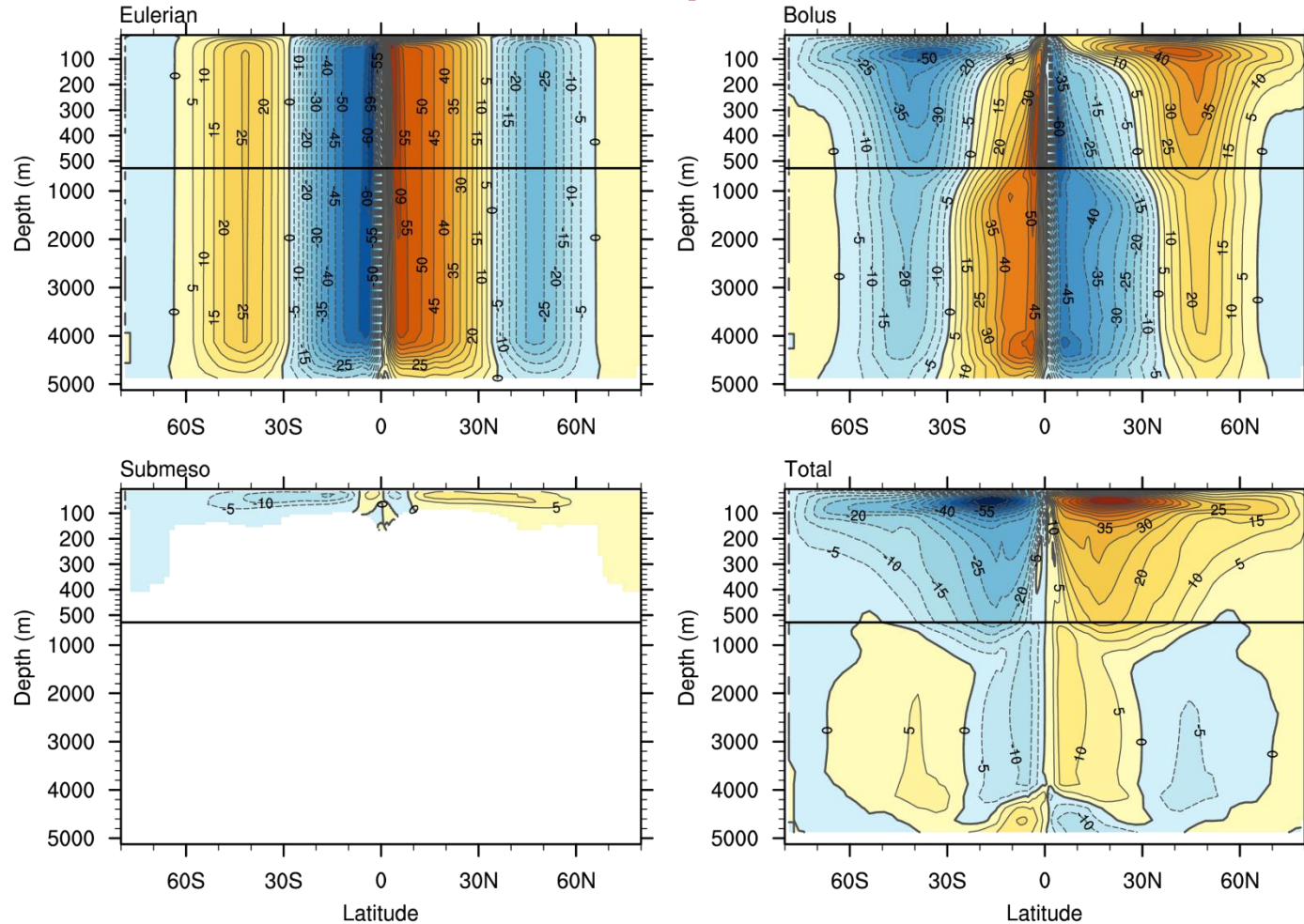


# Symmetric Ocean Buoyancy



# Symmetric Overturning Circulation

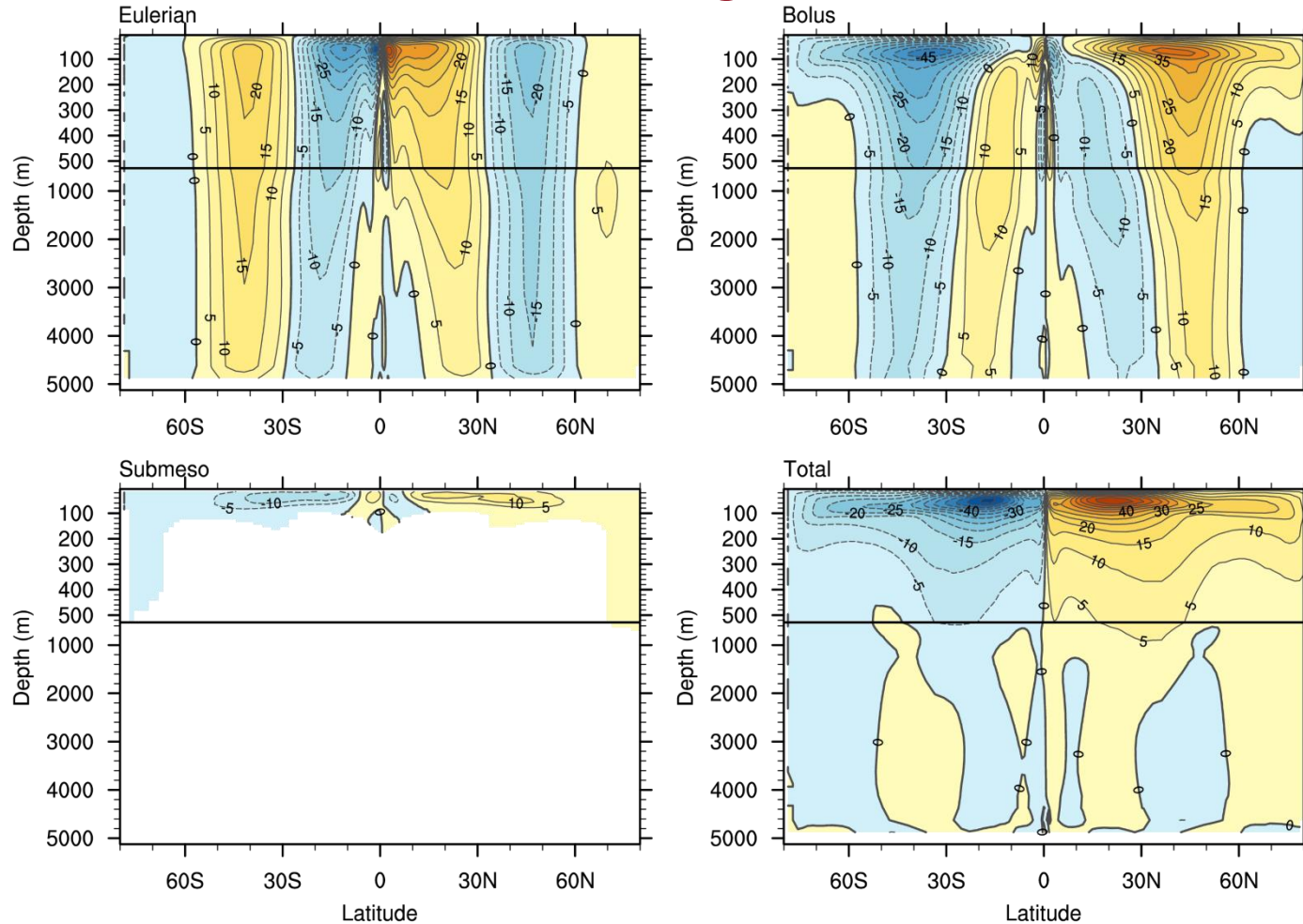
## Aqua



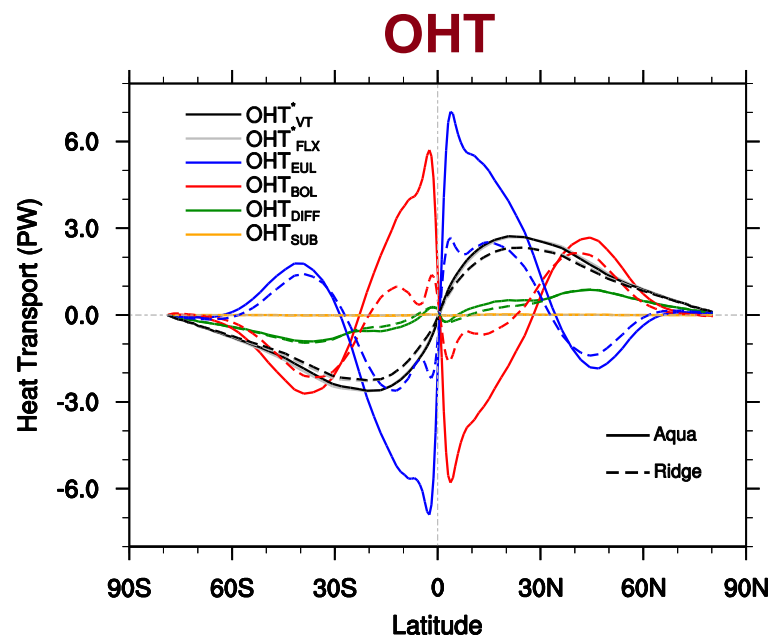
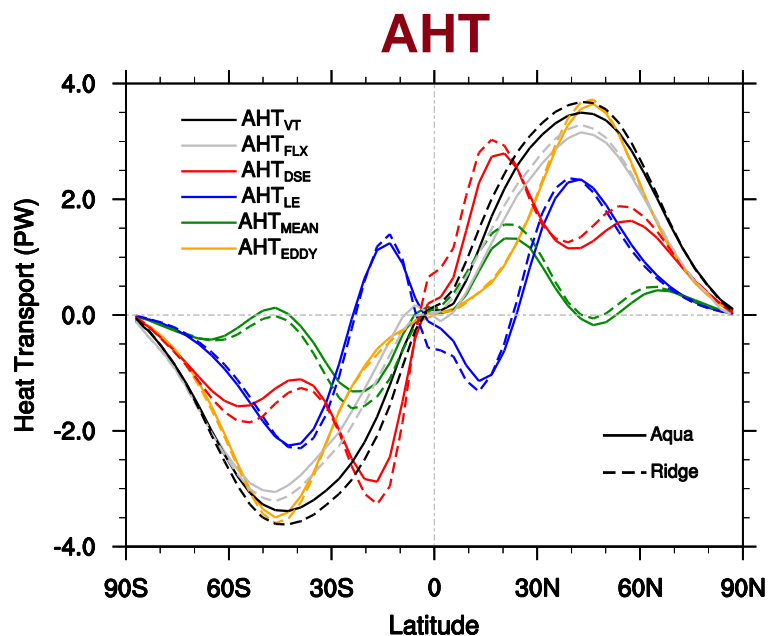


# Symmetric Overturning Circulation

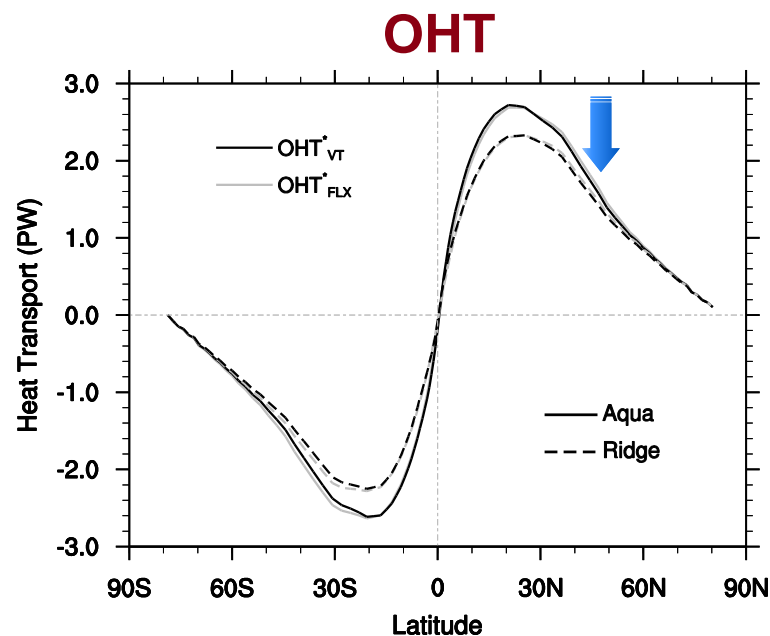
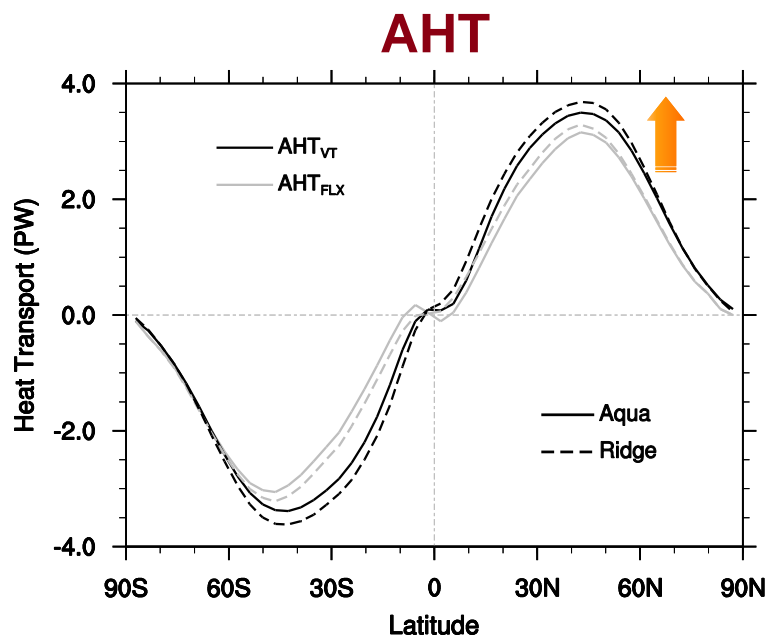
## Ridge



# Symmetric AHT and OHT



# Symmetric AHT and OHT



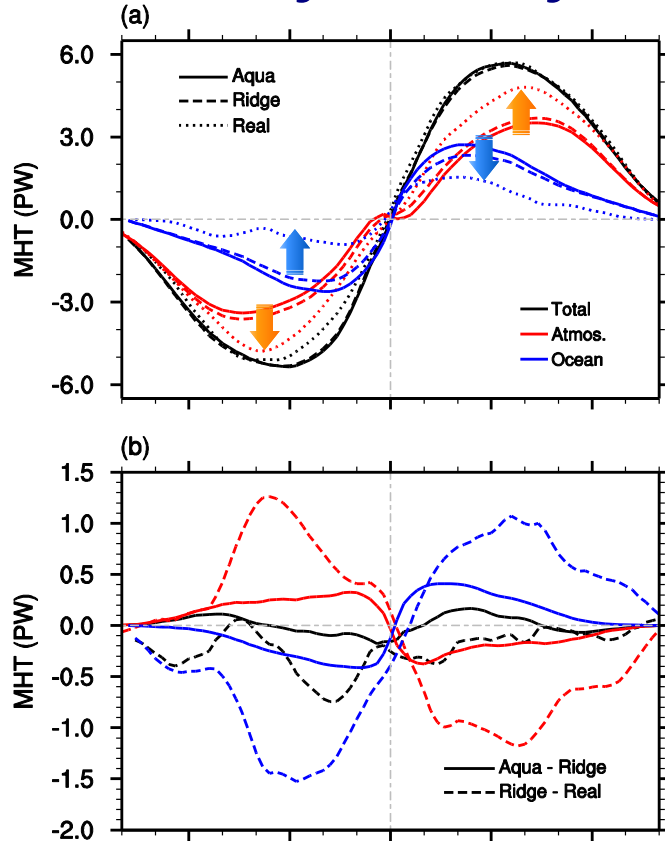
From *Aqua* to *Ridge* → OHT ↓ and AHT ↑

**Bjerknes Compensation**



# Aquaplanet → Real Earth

## Why anti-symmetric MHT? Answered



### From *Aqua* to *Real*

1. OHT ↓ and AHT ↑
2. OHT → asymmetric, NH>SH, AMOC + Weaker baroclinic
3. AHT → asymmetric, SH>NH, Stronger baroclinic  $dT/dy$  ↑

→ Total MHT *unchanged*

**BJC maintains antisymmetric MHT!**

# Summary and Discussion

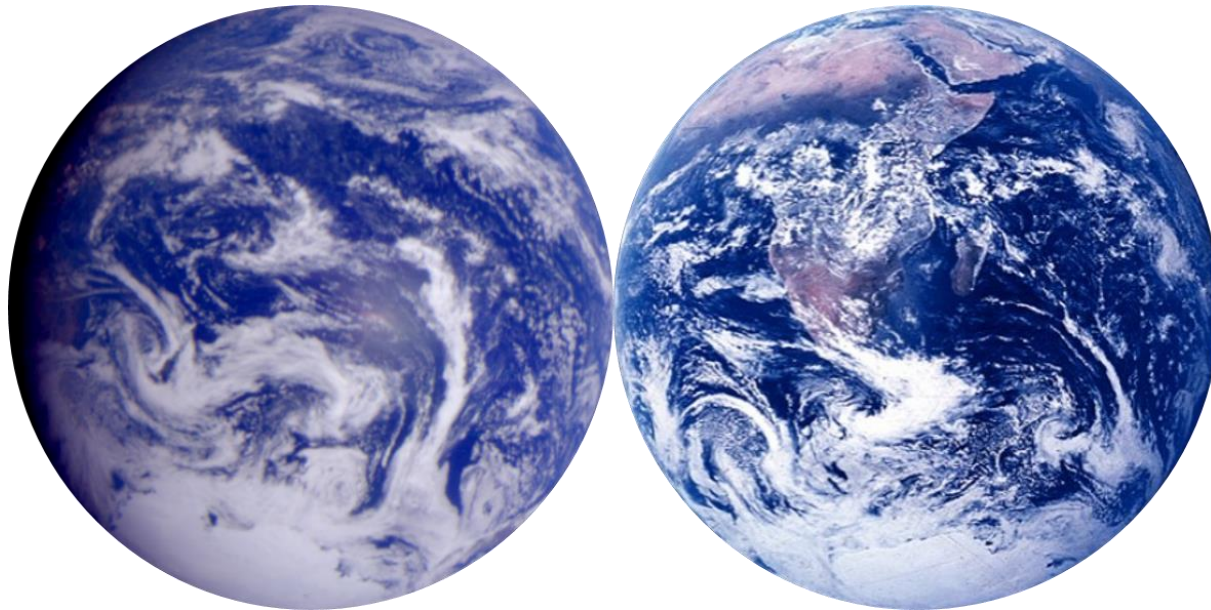
- ◇ **Bjerknes compensation**
  - ◇ Intrinsic mode
  - ◇ Atmospheric physics ↔ Physical oceanography
    - ◆ Climate feedback ↔ Thermohaline circulation
- ◇ **Self-constraint mechanism**
  - ◇ Climate didn't drift too much
- ◇ **If feedback → Reversibility of climate**
  - ◇ Invisible hand (?)



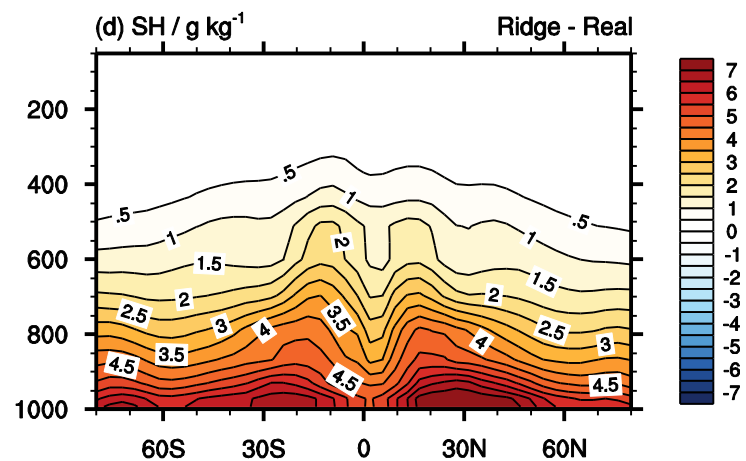
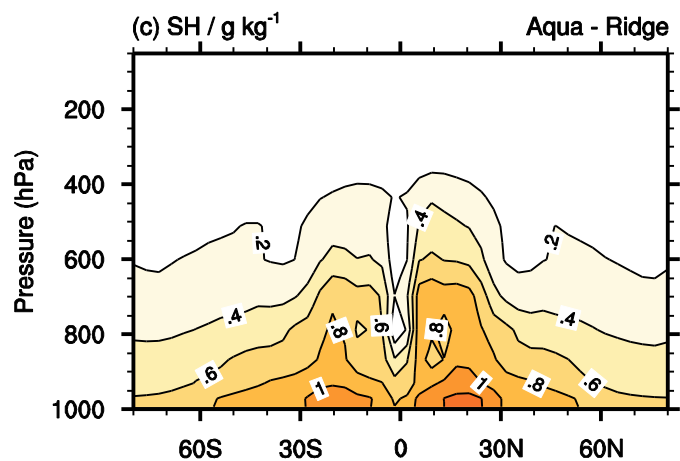
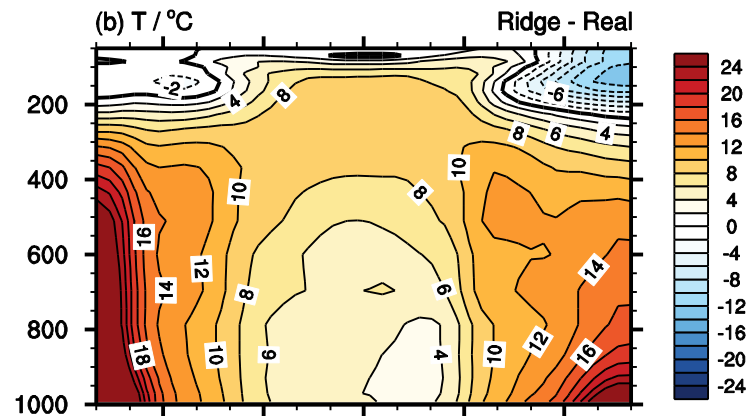
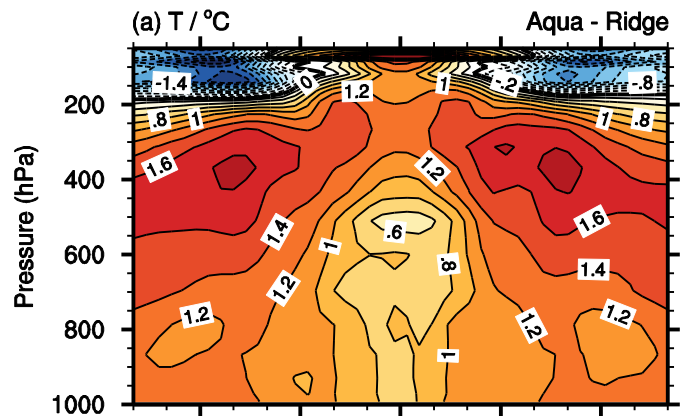
**LaCOAS**  
北京大学气候与海-气实验室

**谢谢**

# Aquaplanet → Real Earth



# Weaker Baroclinic and More Moisture



# Coupled Intrinsic Mode

Energy Compensation  $\Leftrightarrow$  Weight Management



Go to BJC for Climate Variability